

FACULTY OF ECONOMICS AND BUSINESS ADMINISTRATION

Addressing socioeconomic challenges with micro-level trace data





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Milan van den Heuvel

Dankwoord

tl;dr: Thanks to all the people that ever listened to my ramblings, guided me, made me laugh, and helped me think through things!

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Introduction

The work presented in this dissertation is part of an emerging specialism within economics. It can be positioned as a subfield within Applied Empirical Economics that leverages the data originating from the recent trend in digitalisation across public and private sectors. Herein, the focus is on employing new types of datasets to provide novel perspectives on enduring questions and to test hypotheses previously only existing in the realm of theory. This shift towards more empirical, data-driven styles of research has been well-documented [1] and was found to be occurring across rather than purely within multiple economic fields [2]. Apart from the types of data used and the new methodological skills necessary to handle and process such data, an epistemological theme stands central in this specialism, complementing that of classic, theory-driven economics [3].

In the forthcoming section of this introductory chapter we present a motivation for this specialism, the opportunities and challenges this offers to economic research, and set the stage for the ideas, concepts, and data sources used throughout the dissertation. In Section 1.2 we then sketch the outline of the upcoming chapters.

1.1 Introduction

1.1.1 The modern equivalent of the microscope

Economists have always strove to capture and understand how people behave in a plethora of socioeconomic situations (e.g. income changes, policy interventions,

job search). The desire of economists, interested in individual socioeconomic behavior, to progressively uncover new perspectives and details on enduring questions needed to be matched with the proper resources. As Prof. Alberto Cavallo (Sloan School of Management MIT, Harvard Business School, NBER) put it: "We [economists] have been using the same datasets over and over again, and since we wanted new answers, we have been developing new econometric techniques to try to transform the data, and get more meaningful information out of them. But it was reaching a point where there is nothing else you can do on that side, and just having a fresh, new dataset brings a whole new perspective, and I think people are starting to realise that, and gradually people are becoming more interested in data collection itself." [3] With classic surveys-based datasets for instance, it is notoriously difficult to collect consistent measurements over time for the same population [4] (e.g. reporting and recollection biases, motivations for misreporting, etc.). Even those that do are often limited in scale and can only cover a narrow scope to get sufficient response rates. This limits the research possibilities and caused the need for alternative data sources.1

Since the digitalisation of the public and private sector, collection of ever more extensive and intensive individual level data became commonplace. This trend gave rise to a new type of dataset. While the literature is littered with varying terms that all refer to such data in one form or another, e.g. Big Data, client data, behavioral data, we choose to use the term "Trace Data" here. The term Trace Data was chosen to definitively contrast the data we use in this dissertation from often used survey, or self-reported data, and is defined as: "data originating from the natural usage of (digital) products or services of which the collection does not interfere with the natural flow of behaviour and events in the given context". The inherent character and the way Trace data is recorded has several key advantages over classic types of (often self-reported) data on the side of the subjects. The data represent objective measurements, hence there is no reporting or recollection bias, no opportunity nor motivation to under- or over-report. There is also no contagion between different variables because of priming or other psychological factors during reporting [5, 6]. These features increase the reliability and ability to compare results across populations. We emphasise here that while such data are recorded in a consistent and unbiased matter, this does not exclude them from typical data limitations such as selection bias, recording errors, etc. Digital data also comes with new issues such as internet bots, spatial clustering, and censoring. For instance, when using client-data from a specialized financial website, the risk exists that the user-base is not representative of the entire population. A recent example is the use of Financial Aggregator Platforms (FAP) to study consumption dynamics. While the collection method solves recollection biases and eliminates any potential mo-

¹We note that the Nordic countries form an exception and have been collecting and providing administrative data to researchers (and often the general public) for many years.

tivations to misreport in surveys, concerns remain about selection bias [7]. This because it is thought that users of FAPs are generally more financially literate than the population at large.

Realizing the insights economists are after align with their own interest, firms and governments have been granting more and more researchers access to their data. An apt analogy was given by Erik Brynjolfsson, who likened the availability of such data to the invention of the microscope: "To grasp the potential impact of Big Data, look to the microscope. The microscope, invented four centuries ago, allowed people to see and measure things as never before - at the cellular level. It was a revolution in measurement... Data measurement is the modern equivalent of the microscope. Google searches, Facebook posts and Twitter messages for example make it possible to measure behaviour and sentiment in fine detail and as it happens." [8].

With the magnitude and detail of these new datasets comes a word of caution. While more granular data is undoubtedly a benefit, a lot of noise often resides in the measurements of such detail. Not unlike physics, it is important to keep in mind the scale relevant for the research question at hand. Just as one would not investigate the motion of celestial bodies with quantum electrodynamics, it would become unnecessarily complex to investigate interactions between countries by using data on individual inhabitants. Adding to this the finitude of data raises another issue. Data Aggregation might hide features and patterns, but selecting a overly specific subsample might spread the data thin and weaken the power of any statistical inference that can be done. Before doing any statistics, a researcher must thus be aware of which granularity is appropriate/most informative. This will be illustrated in Chapter 2.

Following [9], we note four features of *Trace data*: (1) data is often available in (near) real-time, (2) data is available at a larger scale, (3) data is available on previously unmeasured activities, and (4) data come with less structure. Our three sets of *Trace Data* are on banks in the Russian interbank loan market, Belgian clients of a large European bank, and players in a massive virtual world. With the exception of the Russian interbank data (Chapter 2), which has a regulatory origin and is on bank behavior, these datasets can be thought of as a by-product of everyday actions and behavior of individuals. Like a lot of *Trace datasets*, they are not generated with a specific research question in mind but rather originate from normal usage of a service or product, for instance from using a bank account (Chapter 3 and 4), or participating in a virtual world (Chapter 5). Such data has also been coined 'data in the wild' by Einav and Levin [3] and require a different approach to formulating research question as we will explain below.

Like most economic research currently, we approach research questions retrospectively, hence our research does not utilize feature (1). However, all datasets presented here could be updated in (near) real-time. In Chapter 5 we present some of the opportunities this would bring about.

1.1.2 Data: challenges and opportunities

The features that *Trace data* possess have led to many new opportunities and challenges for economists.

Many examples of novel types of questions and research designs can be found that exploit the different aspects of the data. Having the ability to regularly update the data's time frame (on a daily or an even shorter basis) has facilitated the construction of more precise economic indicators [10]. The larger scale of the data, often even covering a large portion of the population, has allowed researchers to perform detailed explorations of the cross-sectional and temporal variance [11, 12], even for very specific sub-populations [13–15]. Lastly, the availability of previously difficult to observe activities (e.g. geolocation data, item-specific consumption behavior, etc.) has brought about new theories and insights [16, 17], previously impossible to test.

New opportunities also bring about challenges. Since the private sector is weary of making their data public, simply obtaining access is a non-trivial challenge involving cumbersome meetings and elaborate contract negotiations. The data used throughout the chapters, detailed below, is no exception and is subject to NDA agreements and strict access contracts. Once obtained, as per feature (4), the data often comes with less or even no structure. Often a file dump from several sources, in different formats, with different legacy structures are provided that do not follow any standard formatting.

While economists have always been sophisticated data users, the sheer size of these data and the computational complexities that come with them sometimes hit the limits of the statistical packages traditionally used in econom(metr)ics. For instance, the STATA software package, well-known among economists, currently requires loading the complete dataset into memory to do operations or analytics, something that is often infeasible when working with Trace data. Recent computational developments such as NoSQL databases, distributed computing pipelines, and online or iterative approaches to calculations, are becoming more and more a part of the standard economic toolbox. Hal R. Varian, professor at UC Berkley and chief economist at Google says in his paper "Big Data: New Tricks for Econometrics" [18]: "In this essay, I will describe a few of these tools for manipulating and analyzing big data. I believe that these methods have a lot to offer and should be more widely known and used by economists. In fact, my standard advice to graduate students these days is go to the computer science department and take a class in machine learning.". As a result, it will become a valuable skill for future economists to be comfortable with these new data science tools to clean, standardize, and explore ever-larger amounts of unstructured data.

We would also like to mention the issue of privacy, which received a lot of attention in Europe with the new GDPR directive $[19]^2$. One of the challenges with these detailed datasets is that, with growing size and detail, they become more difficult to anonymize. This puts the privacy of the individuals contained in the data at risk. For instance de Montjoye et al. [20] showed for a dataset of 1.1 million individuals, for which they had just three months of credit card data, that just four datapoints was enough to identify a person within the crowd. The exact same was shown to be true for hourly location data like that from mobile phone records [21]. Researchers can thus access and perform research on these data (within the confounds of the company) but are often prohibited from sharing any of the detailed data in their publications. This has led to an ongoing discussion about journal's data policies and the effects this will have on replicability of studies using such proprietary data sources. Constructing privacy-preserving methods, which is part of the "differential privacy" literature, has received much attention because of it (see e.g. [22]). There is also the question of ethics behind combining and analysing such personal data. Especially in the way results are being utilized or capitalized upon (e.g. The Cambridge Analytica scandal [23]).

Apart from the computational skills, this data-driven paradigm-shift has extended the classic epistomological framing of economics. It does so by not solely relying on theoretical insights to steer the research, which then becomes mostly deductive, but rather working in complementary phases of induction and deduction [24]. Herein theories and hypotheses are constructed and refined by interacting with the data, often without a preconceived notion of what patterns to expect. The researcher often starts with just a general direction of interest. Then, by studying the existing patterns in the data, research questions, theories, and hypotheses can be constructed to test against the data. These results can again be used to generate or refine questions, theories, and hypotheses. This iterative process can continue till the researcher has found sufficient evidence for a theory explaining the patterns in the data. For instance, in Chapter 3, we were first interested in general economic behavior of individuals. It was only after getting to know the data that we saw the potential to investigate the subject of income mobility. Then by visualising income changes per wealth category, we found a remarkable difference in income performances between those with and without wealth. This eventually led to the research presented in Chapter 3. A prototypical structure of the workflow in this dissertation is drawn in Fig.1.1. This transformation is also not exclusive to economics but has been disseminating through all fields of social sciences. It was put forth in a well-known Google paper by Halevy et al. [25], "The unreasonable effectiveness of data" (the title of which is a parody on the seminal

²GDPR was put into law to protect the data generated by companies about their users/customers. It, among other things, prohibits companies from using or selling their customers' data without explicit consent.

paper by Wigner on "The unreasonable effectiveness of mathematics in the natural sciences" [26]) which reads: "... sciences that involve human beings rather than elementary particles have proven more resistant to elegant mathematics. ... we should stop acting as if our goal is to author extremely elegant theories, and instead embrace complexity and make use of the best ally we have: the unreasonable effectiveness of data.".



Figure 1.1: Simplified schematic of the typical workflow of the data-driven research projects in this dissertation.

Even though most of this section has underlined the transformative power data has and will continue to have on the field of (empirical) economics, I want to underline the importance of a solid economic framework. Extracting value from complex datasets on a purely experimental basis, by randomly looking for any type of pattern in the data, will rarely lead to insightful conclusions. As said by F. Mazzocchi: "The data-driven approach constitutes a novel tool for scientific research. Yet this does not imply that it will supersede cognitive and methodological procedures, which have been refined during centuries of philosophical and scientific thought. There is no "end of theory" but only new opportunities. Framing the issue of Big Data in terms of oppositions, that is, deduction versus induction, hypothesis-driven versus data-driven or human versus machine, misses the point that both strategies are necessary and can complement each other. As others have argued, the inductive and deductive phases should be seen as an iterative cycle of knowledge acquisition." [24] Economic theory thus provides the researcher with the organizing frameworks to better understand which mechanisms could be at play, which hypotheses to test, and which events pose natural experiments in the data. Herein we also agree with Einav *et al.* [9] who said: "Although the point is not usually emphasized, there is a sense that the richer the data, the more important it becomes to have an organizing theory to make any progress."

1.1.3 A hunt for data

Gathering and gaining access to sources of *Trace data* is not a trivial task. Here we describe the datasets used in this dissertation and explain, in short, the history and reasoning behind obtaining each dataset. All the datsets used in this dissertation can be classified as being of the *Trace data* type and thus carry the benefits and challenges as mentioned above.

Russian interbank lending

This dataset contains the full populations of contracts from the Russian domestic unsecured interbank lending market and is of the regulatory nature. It was provided by Schoors and Karas [27] and has been painstakingly assembled from public and private reporting sources. Originally it was collected with banking and finance questions in mind (e.g. importance of liquidity [28]) but was eventually also used for questions on its network features [29]. Due to the strict governmental regulatory oversight in banking, interbank literature has a long history of being very data-driven. The novelty of our data lies in the fact that it contains every issued loan together with their individual characteristics, in contrast to traditionally available monthly to yearly aggregated interbank exposures. This new level of detail enables a more precise investigation of the generative process behind loan issuance, what network structures this generates, and how this would influence risk. While leaving the latter for future research, we focus on the former in Chapter 2. This research thus situates itself in the class that leverages the extent and detail of the data to perform a detailed exploration of the cross-sectional variance.

The dataset covers the 55 month period from January 2000 until October 2004. This period contains a total of 2.4 million loans, each annotated with its lender, borrower, month of issuance, loan size, interest rate, and maturity class. The structure of the data follow the reporting standards of the CBR ³. Banks report loan

³While these loans do get reported by the banks involved, this dataset is available for the other banks to possibly check. Given the large risks and penalties (up to loosing their banking licence) for misreporting, this data can be categorized as *Trace data*.

issuances to the legislator on the first day of each month. The maturity classes that are included are: overnight (less than one day, (<1d), 2-7 days (2-7d), 8-30 days (8-30d), 31-90 days (31-90d), 91-180 days (91-180d), 0.5-1 year (0.5-1y), 1-3 years (1-3y), more than 3 years (>3y).

Given the specificity of the data, the cleaning and contextualizing required a large amount of expert economic knowledge on top of mastery of the Russian language. The time frame of the data is also littered with important economic events that directly affected the Russian banking system (e.g. the "1998 Russian default", the trust crises in the second half of 2003 and the summer of 2004). Knowledge of these events and their implications was very important to correctly design the research and interpret the results.

This dataset is a great example of the fact that, as mentioned before, interaction with the data can lead to new research questions, even after years of working on it. It also shows how expert knowledge and economic framing are what make the data useful.

Financial data on a European bank's Belgian clients

This dataset contains several million Belgian clients from a large European bank and covers their detailed individual financial information over an eleven year period (2006-2016). The contents range from personal characteristics, financial portfolio, to every monetary transaction going in and out of the clients' accounts. As mentioned above, this *Trace data* is a by-product of the services provided by a private firm (i.e. financial services by a bank). It was obtained through a collaboration with the bank led by Ken Bastiaensen, Benjamin Vandermarliere, and Koen Schoors. Its novelty lies in the scarce availability of such data, especially because of the proportion of the Belgian population it covers (Belgian had around 11.5 million inhabitants in 2018). Its contents such as transaction specific consumption and financial wealth enables novel perspectives on enduring question such as consumption dynamics, saving dynamics, and inequality. Data for such questions were (and often still are) mostly available from surveys, which only allows for aggregated views and not transaction specific as is possible here and allows for full control over the construction of variables (e.g. income and consumption). The main limitation of the data is that we only capture one bank and thus miss part of the financial behavior of people who are active at several banks. We leverage the dataset in Chapter 3 and 4 to investigate cross-sectional variance of specific subsets of the population and study the mechanisms behind income mobility (Ch. 3) and consumption dynamics (Ch. 4).

With this dataset, we started out having a general direction of interest, namely the motivation to investigate the financial behavior of individuals. Even before the data was fully available, a preliminary evaluation was performed into the viability and potential of several lines of research. Then, after about half a year of contract negotiations, bureaucracy for access codes and infrastructure, working with their data team to complete the data, merging several legacy systems, and dealing with an environment which is not as flexible as is commonplace in academia, we finally had access to the extremely valuable dataset. Given, because of privacy concerns, we only had access to perform research on it from within the bank, on laptops owned by the bank, via which we connected to a secure server on a non-disclosed location of the bank. This is not unlike the conditions Raj Chetty and his team faced when working on American IRS data [3] and are becoming more and more common in research.

The final dataset originated from two main sources which themselves were compiled from several other sources. The first source contained the personal characteristics of the individuals such as date of birth, civil state, gender, postal code, and nationality. This source is updated at least once per calendar year, per individual, not necessarily synchronized along individuals. The other source contained every single action that involved one or more of their accounts, updated continuously with every new action. Herein each transaction contained a flag regarding the action type, including whether the transaction comes from a point of sale in Belgium, a cash withdrawal, a payment via credit card, etc. From these 248 codes, we constructed relevant variables in order to adopt multiple definitions of individual income and consumption.

Here again economic knowledge was paramount in the construction of the final dataset. We started by performing an Exploratory Data Analysis (EDA) during which we found several interesting patterns in the data. With these patterns in mind, another literature search was performed which amounted to the formation of several novel research questions impossible to foresee before being familiar with the data. Chapters 3 and 4 are on two of these research questions.

EVE Online: a virtual world

A virtual world is defined as: "a computer-based online community environment that is designed and shared by individuals so that they can interact in a custombuilt, simulated world.". While these worlds originally greatly limited what players were able to do in them, they have more recently become complex and adaptive. Strict game boundaries implemented by the designers have made way for the possibility that users directly influence and drive what happens to and in the virtual world. For instance, earlier virtual worlds often had items that were sold by computer characters at a fixed price with unlimited supply, which is of course very unrealistic. Recent worlds have however become more realistic, allowing users to mine raw materials, manufacture items, and set their own selling price. EVE Online is a prime example of such a complex virtual world.

As described in [30–32], Eve Online (EVE) is an open-ended Massively Multiplayer Online Game set in a science fiction universe created by Icelandic company CCP Games (CCP) in 2003. More than 500,000 players compete for resources, territory, and power while engaging in a variety of professions and activities including mining, manufacturing, trading, diplomacy, leadership, exploration, and warfare, both versus the environment and against other players. As a sandbox game [33], EVE provides its players with a virtual world and the tools to explore, but players have the freedom to choose what, when, and how to approach the available content, including how they gather resources, what the goal is they want to attain, how they attain this goal, how they interact with other players, and on which activities they spent their time. Items and resources in the game are bought and sold with an in-game currency called the Inter-Stellar Kredit (ISK). Players earn ISK as a reward for engaging in activities such as playing against the environment (e.g. defeating non-player characters), selling resources gained through mining, selling goods made through industry, offering services like courier contracts or protection to other players, or by paying real-world money. Because ISK has both in-game and real-world value, and because losses in EVE are permanent, players tend to be risk averse, and this fosters realistic socioeconomic behavior.

The dataset contains detailed information on all aspects of life for players within EVE Online. This ranges from where they go, who they interact with, what kind of relationships they have with other players, to what they pay for which items, and how they manage their supply chains. Here again the data originates as a by-product from the services provided by the company. Access was granted because of a collaboration with CCP established thanks to large contributions by Kevin Hoefman, Koen Schoors, and Jan Ryckebusch.

This availability of complete information on previously impossible or hard to measure behavior and characteristics opens up possibilities for novel questions on individual behavior and group organisation/coordination. An important issue for businesses is for instance pricing. Because the characteristics of items (e.g. watches, houses) and their values to people are not explicit, it has been notoriously difficult to come up with pricing models. In a virtual world however, there is complete and transparent information, which allows to explore such pricing dynamics. This example was studied by Hoefman *et al.* [30] using EVE Online data (see Chapter 5). The main strength of this data, namely its digital nature and the ability to record everything because of it, is also the main limitation. Being a virtual world, it becomes indispensable to understand what behavior could be representative for that in the real-world and what is an artifact of the virtual nature of the world. As a result, great care was taken in the projects outlined in Chapter 5 to focus on virtual behavior which is guided by the same (economic) motivation as in real-life. To the extent possible, a comparison to real-world data was also made.

Apart from some of the largest digital multinationals (e.g. Amazon, Alphabet, Apple) most companies only know of one specific aspect of their customer's life. For instance the bank with which we collaborated only has information on the

financial aspect of a person's life. One could imagine that in the future, information about any and all aspects of an individual's life will be available somewhere through interaction with digital products and services. The ethics of such a possibility, if it is going to be centralized, and who will have ownership remains a very important open question. One take on this is the vision of Tim Berners-Lee, one of the founders of the world wide web. He and his team at MIT are working on what they think should be the new internet. It's called SOLID (Social Linked Data) [34] and with it they want to hand back ownership of data to the data subjects instead of keeping it in the hands of the multinationals. Every individual would have their own "SOLID Pod" which collects the data they have generated with their activity. People could then freely choose who has access to what parts of their data for which uses. Those willing could then for instance share a multi-faceted view of their life for research, something that could potentially be a treasure trove for the social sciences. In contrast with this vision, the Chinese government is planning to centralise a plethora of data on its citizens to observe and nudge their behavior (e.g. a social-credit system).

While a real-world multi-faceted view on individuals still lies in the future, these virtual worlds, in which detailed multi-faceted data on individual's activity is available, provide a novel opportunity for research. Literature using virtual worlds as online-laboratories has been fast-growing with over 35,000 papers⁴ using them. However, less than 3% of these are in an economics-related field⁵. EVE Online is currently one of the purest examples of a complex virtual world.

1.2 Outline

This PhD dissertation details four research projects on different socioeconomic questions. While the subjects may appear eclectic, they are all part of a growing data-driven specialism that has extended the classic epistemological framing in economics. We split up the projects along the data they employ. The first part covers an analysis of the Russian interbank lending market. Part two covers two contributions pertaining to the societal problems of inequality and marginal propensity to consume. The third and last part details the use of a virtual world (EVE) as a novel testbed for socioeconomic theories. To give an overview, a schematic in line with Fig. 1.1 will be given at the beginning of each chapter. Chapter 6 concludes with a summary and presents an outlook on future research within this specialism and its effects on the field of economics.

⁴Obtained from running a search on the SCOPUS database on papers using the word "Virtual World" in their title, abstract, or as a keyword.

⁵SCOPUS contained a little over 450 papers containing both "Virtual World" and "Economics" anywhere in their title, abstract, or keywords

Part I: The Russian interbank market

Chapter 2: Loan maturity aggregation in interbank lending networks obscures mesoscale structure and economic functions While having more details in data is often a benefit, this chapter shows that extra granularity only matters if it is informative for the research question. On the one hand, too much aggregation hides features and patterns in the data. On the other hand, introducing too many details on which the data is split (e.g. by looking only at individuals of a certain age, living in a certain place, and having a certain height) may spread the data thin and weakens the power of any statistical inference that can be done. An important question to ask before doing any statistics is thus which granularity is appropriate/most informative.

This chapter is co-authored with Marnix Van Soom, Koen Schoors, and Jan Ryckebusch and has been revised and resubmitted to Scientific Reports under the title "Loan maturity aggregation in interbank lending networks obscures mesoscale structure and economic functions".

We employ the complete interbank loan contract dataset from Russia, containing more maturity granularity than previously available, to investigate whether common data granularity limitations in the interbank literature obscures important structure and economic functions. The maturity information can be utilized to separate the loans into different layers according to their maturity. We apply the layered stochastic block model of Peixoto [35] and other tools from network science to the time series of bilateral loans. We find that disregarding maturity information, or completely collapsing the maturity layers into one layer, consistently obscures mesoscale structure. The optimal maturity granularity lies between completely collapsing and completely separating the layers and depends on the development phase of the interbank market, with a more developed market requiring more maturity layers for optimal description. Closer inspection of the inferred maturity bins associated with the optimal maturity granularity reveals specific economic functions, from liquidity intermediation to financing. Collapsing a network with multiple underlying maturity layers, common in economic research, is therefore not only an incomplete representation of the interbank lending network's mesoscale structure, but also conceals existing economic functions.

Part II: Belgian client data of a large European bank

In the next two chapters, we combine de-identified, client-level financial and demographic data on Belgian clients of a large European bank. We utilize the magnitude of the dataset to zoom in on a particularly interesting subset of the population, namely career starters. By carefully selecting a subset of the population, we are able to minimize confounding factors, increase comparability, and better focus on the research question at hand. **Chapter 3: The wealth origins of income mobility.** In the third chapter, zooming in on career starters enabled us to explore possible mechanisms contributing to wealth inequality perpetuation. To this end, we analysed drivers of early career performance in Belgium, one of the most equal countries in the world. We selected career starters because the start of a career stands as a major life event to study how and when wealth inequality interacts with income mobility.

This chapter was co-authored with Tarik Roukny, Benjamin Vandermarliere, Jan Ryckebusch, and Koen Schoors under the title "*The wealth origins of income mobility*".

The large economic gap between rich and poor continues to have a detrimental effect on societies. In this chapter, we propose and evaluate three possible mechanisms - social capital, innate ability, and job search conditions - behind the observed positive relationship between wealth inequality and income immobility. We find higher earning performances for individuals with higher financial wealth at the start of their careers. Neither social capital nor innate ability are able to fully explain this finding. However, evidence is found for a transmission channel via job-search conditions. Our result suggests that wealth mitigates budget constraints in job searches and leads to more optimal human capital allocations for those who can afford it, contributing to the perpetuation of economic inequality.

Chapter 4: Liquid wealth heterogeneity, asymmetric consumption dynamics, and myopic loss aversion In the fourth chapter, we leverage the comparability in certain financial aspects of career starters in Belgium. Specifically, that they have low (to no) debt and hold most (to all) of their wealth as liquid wealth. These similarities and the fact that we have transaction-level time-series data on income, consumption, and wealth allows us to exploit the remaining heterogeneity in consumption responses to income changes in more detail than has been possible in literature.

The idea is to study how people cope with changes in income and how this is reflected in their consumption. If an individual experiences a decline in income, does she changes her consumption by the same amount or only partially? If only partially, which financial characteristics determine this proportion? In literature, which has heavily relied on survey data, it was found that beyond personal characteristics, liquidity plays a large role in determining how individuals change their consumption in response to an income change. Multiple models have been proposed but none that cover all the different findings in literature. To this end, we empirically study the effect of liquid wealth on consumption dynamics in the absence of both illiquid wealth and debt.

We find an asymmetric consumption response to anticipated income changes, with a stronger response to income increases than to decreases. This asymmetry in consumption responses originates from the asymmetric consumption smoothing effect of liquid wealth. This indicates that people try to resist reducing consumption more than they resist increasing consumption. Rational models of consumption are unable to fully explain the results. These results are consistent, however, with the predictions of the behavioural model of myopic loss aversion which originates from a combination of present-bias or myopia (preference to spend now) and loss aversion (reluctance to lowering consumption). This suggests that there may be a link between a country's population structure and the effectiveness of its macroeconomic policies.

This chapter was co-authored with Benjamin Vandermarliere, and Koen Schoors and submitted to *the journal of economic behavior and organization* under the title *"Liquid wealth heterogeneity and the asymmetry in consumption dynamics"*.

Part III: A multi-faceted view on behavior in a virtual world

Chapter 5: Revealed behavior in a virtual world: the case of EVE Online In this last chapter, I present the potential of virtual worlds as a research tool. Due to the scarcity of access to detailed *Trace data* from industry and the often limited scope of such data, virtual worlds present a unique and novel opportunity to gain a multi-faceted view on individual-level behavior. These data can be used to investigate enduring socioeconomic questions if the motivations of the individuals inside the virtual world align with the motivations in the real world. For this reason, the most interesting among the virtual worlds are those of the "sandbox" type. This type of approach to constructing virtual worlds provides players with an environment and the tools to explore it but allows them to choose what, when, and how they approach the available content. Allowing players to make their own decisions and drive the experience of the virtual world fosters realistic economic behavior. Arguable the most advanced and complex open-ended sandbox game is EVE Online.

This chapter details the world of EVE Online and explains what design choices drive the realism of in-game behavior. I then describe the contributions I personally made for our team to acquire large amounts of data from EVE Online, enabling the construction of a multi-faceted view on the behavior of (groups of) players inside EVE. I further describe three published papers that utilized the collected data. Two of these examine and expand on the theory of structural balance [31, 32] and the third expands on the theory of hedonic pricing [30].

I end with a short description of work in progress and an outlook on future possibilities.

Computational setup

Because of the high computational requirements to perform the work presented here, several high performance computing resources were used. Chapter 2 was conducted using the computational resources (Stevin Supercomputer Infrastructure) and services provided by the VSC (Flemish Supercomputer Center), funded by Ghent University, FWO and the Flemish Government - department EWI. In total, over 3,000,000 hours of single-core CPU time were used to complete the calculations in this chapter. Chapter 3 and 4 were primarily conducted using one of the European bank's secured shared servers. This server had 64 cores and 512 GB of RAM, of which often the majority was needed to process the data. For Chapter 5, the extraction was done using CCP's hadoop cluster and MSQL server. The processing of the data was done on our group's own server which has 32 cores and 256 GB of RAM.

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Part I

The Russian interbank market

2

Loan maturity aggregation in interbank lending networks obscures mesoscale structure and economic functions

co-authored with: Marnix Van Soom, Jan Ryckebusch, and Koen Schoors.

2.1 Schematic overview



Figure 2.1: Schematic overview of the workflow of the project on Russian Interbank Networks.

2.2 Abstract

Since the 2007-2009 financial crisis, substantial academic effort has been dedicated to improving our understanding of interbank lending networks (ILNs). Because of data limitations (or by choice), the literature largely lacks multiple loan maturities. We employ a complete interbank loan contract dataset to investigate whether maturity details are informative of the network structure. Applying the layered stochastic block model of Peixoto (2015) and other tools from network science on a time series of unsecured bilateral loans with multiple maturity layers in the Russian ILN, we find that collapsing all such layers consistently obscures mesoscale structure. The optimal maturity granularity lies between completely collapsing and completely separating the maturity layers and depends on the development phase of the interbank market, with a more developed market requiring more layers for optimal description. Closer inspection of the inferred maturity bins associated with the optimal maturity granularity reveals specific economic functions, from liquidity intermediation to financing. Collapsing a network with multiple underlying maturity layers, or only focusing on one such layer, common in interbank network research, is therefore not only an incomplete representation of the ILNs mesoscale structure, but also conceals existing economic functions. This holds important insights and opportunities for theoretical and empirical studies on interbank market functioning, contagion, stability, and on the desirable level of regulatory data disclosure.

2.3 Introduction and overview

Interbank lending networks (ILNs) are complex network models of the interbank money markets, often called the plumbing of modern financial systems [1]. Banks make interbank loans on such markets to accommodate daily liquidity imbalances and manage their duration gap, defined as the maturity disparity between bank assets and liabilities [2]. For example, a bank holding more cash than desired may profitably lend this cash to other banks in need of cash [3].

The financial crisis of 2007-2009 has brought the interbank money markets in the public eye because their "drying up" (failure to lend cash to banks in need) was a major channel of financial contagion [4]. Since then, substantial academic effort has been dedicated towards improving our understanding of these markets. It turns out that representing the interbank money market as a network is a simple and powerful abstraction [5], that is arguably more realistic than modelling it as one representative bank, as is customary in traditional macro-finance [6]. Network analysis is therefore now one of the standard tools of financial stability experts worldwide, i.a. at the IMF [7] and ECB [8].

A thorough understanding of the interbank money market is vital to prevent
systemic meltdowns [9, 10], implying a need for ever more realistic models of ILNs. We contribute by studying an often unavailable and sometimes disregarded aspect of ILNs, i.e. the different loan maturities. The maturity of a loan, i.e. the period after which the loan must be repaid, is an important instrument for banks to organise their lending and borrowing activity in function of risk minimisation [2, 11, 12]. The vast majority of empirical financial network papers study the overnight interbank market [6]. This seems to partly originate from the widely held view that overnight lending makes up the majority of interbank exposure, a view that stands in contrast with recent results showing the average contract length in the German interbank market to be well over one year [2]. Sometimes however, empirical ILN literature is unable to include different loan maturities because of data limitations (see [13] for a recent overview of available interbank data). As a consequence agent-based models of ILNs that often either neglect loan maturities or limit it to a modelling detail [14, 15], even though maturity choices reflect bank risk strategies. For example, stress testing models would benefit from exposure data enriched with maturity information because different risk strategies can lead to different network structures, which in turn have different contagion processes. Excluding maturity layers can then lead to an underestimation of the likelihood of contagion [16]. Enabled by a particularly granular dataset, a panel of all lending contracts issued in the unsecured Russian ILN [17], we investigate qualitatively what kind of information is lost by not differentiating between the loan maturities. We further try to estimate the pitfalls of this common practice. The approach we take consists of explicitly modelling the Russian ILN by layered stochastic block models (SBMs). This allows us to determine to what extent the loan maturities are informative of the Russian ILN's mesoscale, i.e. the higher-level organisation of the banks into bank groups.

The dataset used in this work consists of 57 monthly ILNs constructed from the complete panel of contracts on the Russian domestic unsecured interbank lending market, one for each month in the period from January 2000 to October 2004, except for January 2003. There are a total of 2.4 million loans, each annotated with its lender, borrower, month of issuance, loan size and *maturity class*. The dataset is unusual in the sense that it is an loan issuance network rather than an exposure network, the latter being the typical ILN representation found in the literature [13]. The exposure network associated with a given issuance network can be derived by aggregating the loan sizes in the issuance network over time. The data originates directly from the bank reports to the Central Bank of Russia (CBR) and came preassigned into eight contiguous maturity classes, so that every loan can be assigned to a particular maturity class (e.g. 2-7 days). Fig. 2.2 shows the monthly number of active banks, loans issued, and outstanding loans per maturity class, together with a list of the eight maturity classes (further details on the dataset can be found in the Methods section). We look at the monthly ILNs as layered networks such that



Figure 2.2: Temporal evolution of the lending activity in the Russian interbank lending network. Month 1 corresponds with January 2000. (a) The number of active banks on the lending market per month. A bank is active whenever it is the originator or the beneficiary of at least one new interbank loan in the given month. (b) The number of loans issued per month and per maturity. Note the different scales on the vertical axis of the two panels: The majority of issued loans have "short" (≤ 30 days) maturities. (c) The number of outstanding loans, i.e. loans open on the last working day of each month. From this perspective the loans with longer maturities now play an equally important role as the short ones. Note that we have included loans issued before January 2000 for this panel (see Methods).

each maturity class corresponds to one *maturity layer*. By putting contiguous maturity layers into bins, they can be coarse-grained to achieve various levels of *layer granularity*, ranging from complete differentiation (eight bins, one layer per bin) to complete aggregation (all layers merged into one bin, the collapsed network).

First, we provide descriptive statistics of the monthly ILNs in a comparative framework. We characterise the network topology of each maturity layer separately using the typical network measures from ILN literature (listed in the leftmost column of Table 2.1) and compare the results across the maturity layers and across the literature. Broadly speaking and integrating over time, we find layer non-homogeneity for most topology measures. This means that, while stylised facts found in the literature were also found in some of the maturity layers, the topology measures do not take on similar values for all maturity layers simultaneously. Layer non-homogeneity points to the fact that complete aggregation or single layer focus involves the loss of the topological diversity present in the maturity layers, although some layers do share similar lending patterns in specific months (by lending pattern we mean a topological pattern in an ILN). For example the three most dense layers – the "short" layers, i.e. all maturities below 30 days – display a strong similarity throughout the full time period. The short layers'

topological similarity, together with their dominant share in the number of loans issued, could suggest that complete aggregation might not be harmful after all, irrespective of what the found layer non-homogeneity suggests. The question then becomes whether the information lost by complete aggregation is relevant for ILN structure and economic function. Because financial stability plays a central role in literature and policy, we are interested in the money markets' mesoscale organisation, which can effectuate the propagation of instability and risk [18], rather than individual banks' lending strategies. Relevant information is thus any set of information that allows for characterisation of the mesoscale structure rather than other, more specific, more "noisy", information about local lending patterns (e.g. clustering).

In order to characterize the effect of aggregating maturity layers on the ILN mesoscale, we explicitly model the monthly ILNs by layered SBMs. SBMs can infer statistically significant group structure in networks, without making informative prior assumptions about the type of mesostructure itself. SBMs model the mesoscale of a network by assuming that the nodes in a network behave "group-like" rather than on individual account. *Layered* SBMs generalize SBMs for layered networks by allowing the group structure to have a different topological pattern on each layer. As a concrete example, imagine a network with two layers representing the mating (layer 1) and conflict (layer 2) interactions in a population of deer (the nodes). One possible layered SBM of this network is the division of the deer into two groups, male and female, so that observed occurrences of mating and fighting between two deer are explained only by their sexes. Note that such a simple model – which does not take things like social status etc. into account to explain the observed interactions – could well suffice to infer the deer's sexes if these were unknown.

Layered SBMs formulated in a Bayesian setting can be extended to the *coarse-grained* layered SBM in order to infer the appropriate level of layer granularity (the optimal granularity, OG) along with the group structure. The bins in the OG correspond to lending patterns between the bank groups that differ from each other in a statistically significant way. We explain this in detail in the next section and give a simple illustration in Fig.2.3, but the essence of how an OG can be inferred can already be understood by a simple regularisation argument. The complexity and modelling power of a coarse-grained layered SBM is determined primarily by the number of groups and the degree of layer granularity, as these parameters simultaneously define the "resolution" available to model the observed layered network. To prevent overfitting (i.e. modelling noise), any increase in model complexity should be warranted by enough statistical evidence in the data. Thus the OG may be determined in general by any regularisation principle to balance model complexity and quality of fit; we use Bayesian model selection for this. One specific advantage of this approach is that there is formally no difference between inferring

the number of groups – and in fact the groups themselves – and the OG; both are determined as part of a single inference for each monthly ILN.

The inferred monthly OGs are displayed in Fig. 2.4(a). Each OG consists of a set of bins numbered from short to long maturity by the OG bin index (OGB index). We mention here two findings easily deduced from Fig. 2.4(a). First, we find that the OG always lies between complete differentiation and complete aggregation. This means that on the one hand the eight available maturity classes are partly redundant and that the lending patterns may be described more effectively by merging maturity layers into bins, as is indeed the case for the short layers mentioned before. On the other hand complete aggregation apparently discards important information needed to model the monthly ILN's mesostructure: The lending patterns between the bank groups depend significantly on the maturity classes of the loans. The lending patterns between the bank groups depend significantly on the maturity classes of the loans. This also illustrates the more general added benefit of statistically inferring the optimal maturity bins, instead of setting them manually based on some heuristic or prior: if one would set bin widths too narrowly, the data might be too thinly spread to detect any structure at all. Conversely, if one would set bin widths too widely, the different structures, and their economic functions, might be obfuscated. Second, the monthly number of bins in the OG correlate roughly with the known two phases in the Russian money market's development: early development (roughly before month 35) and emerging maturity (from month 35 onward) (see Methods). This points to a natural ordering in number and complexity of lending patterns emerging at different phases of market development.

To interpret the lending patterns, we take a closer look at the monthly OG bins at the network and individual bank level. (Note that this goes beyond the previously established network measures of the individual maturity layers, as these are now merged according to whether they form a statistically significant lending pattern.) The notable result here is that the bins may be characterised by a simple aspect of the most important banks' individual lending behaviour: At monthly time scales the important banks in "short" bins tend to both lend and borrow equal amounts of cash (indicative of financial intermediation), while the important banks in the "long" bins tend to either lend or borrow (indicative of financing). For the development phases, this suggest that patterns of financial intermediation are present at all phases of development, while patterns more in line with financing only appear at later phases.

Our coarse-grained layered SBM of the ILN thus uncovers a correlation between statistically significant lending patterns between groups of banks, the economic functions of important banks, and the maturity classes of the loans involved, showing that maturity information matters for the understanding of ILNs.

2.4 Results

The adopted notation is in line with the one of [19, 20]. An ILN at month t is denoted as $\{G_l\}$, with G_l the network for one of the eight maturity layers: $G_{<1d}, G_{2-7d}, G_{8-30d}, G_{31-90d}, G_{91-180d}, G_{0.5-1y}, G_{1-3y}, G_{>3y}$. As we analyze each month independently we do not attach a time label to $\{G_l\}$. The G_l are directed weighted multigraphs. In addition to the asymmetrical adjacency matrix $A_{ii}^l \in \mathbb{N}_0$ of layer l, the G_l possesses the unordered edge covariates x_{ijk}^l $(k \in [1, A_{ij}^l]$ for $A_{ij}^l > 0$). Thereby, each kth parallel edge between banks i and j represents a loan lent from bank i to bank j with a maturity in maturity class l and of size x_{ijk}^{l} . The collapsed network G_c corresponds to complete maturity aggregation. Its adjacency matrix $A_{ij} = \sum_{l} A_{ij}^{l}$ and the edge covariates x_{ijk} are constructed by flattening (i.e. collapsing) the x_{ijk}^l along the k, l axes. We denote a level of granularity by the maturity bin set $\{\ell\}$ where ℓ specifies a set of merged layers. For example, the OG of month 58 (see the last month in Fig. 2.4(a)) corresponds to $\{\ell\} = \{\{<1d, 2-7d\}, \{8-30d\}, \{31-90d\}, \{91-180d, 0.5-1y, 1-3y, >3y\}\}$. The ILN $\{G_{\ell}\}\$ representing the level of granularity specified by $\{\ell\}\$ is constructed from $\{G_l\}$ by merging maturity layers according to $\{\ell\}$.

Descriptive statistics of the Russian ILN in a comparative framework

We start by characterising the maturity layers and the collapsed form of the Russian ILN in terms of monthly (and occasionally yearly) time series of several ILN measures typically used in the literature. Layer analysis of layered ILNs has been performed for the interbank money markets of several countries, e.g. Mexico [21] and the UK [22]. The layers in those works, however, do (or can) typically not differentiate between maturity classes [6, 13]. The maturity classes per layer of those that did are shown in Appendix G. The work by Bargigli et al. [1], which is related to this work, separates overnight loans, loans up to 1y and loans >1y in a three layer end-of-year exposure network representation of the Italian ILN. They find that the structures of the three maturity layers are not representative of each other. The measures that we analyse are: density, degree distribution, clustering coefficients, average shortest path length, degree mixing (as a proxy for bank size mixing), loan activity, and loan size. The results are compared to the stylised facts found in literature. A summary of this analysis is given in Table 2.1, while details of the analysis can be found in the Supplementary Material, Appendix 2.A.

The stylised facts describing prototypical ILNs are often deduced from exposure networks with only one maturity class. Looking at the maturity layers separately, we also find layer non-homogeneity for all measures in Table 2.1 except for the distribution of degree and transaction volumes. This means that variations of the ILN measures across the maturity layers are observed. While the stylised

ILN measure	Value	Layer homogeneity	Selected studies
density	sparse	No	[1, 6, 23, 25–27]
degree distribution (in and out degrees)	heavy-tailed	Yes	[1, 6, 23–25, 28]
topological structure	scale-free / core-periphery		[1, 29, 30]/ [6, 25–28]
clustering coefficients	low / high	No	[23]/ [1, 6, 25, 30]
average shortest path length	small / "small world"	No	[25, 27]/ [6, 23, 30]
bank size mixing	disassortative	No	[6, 21, 23, 25, 27, 29]
distribution of transaction volumes	heavy-tailed	Yes	[23, 24]

Table 2.1: Stylized network properties of interbank lending networks (ILNs) according to selected studies. For some ILN measures conflicting values are reported, in which case we separate them by a backslash. For example, low clustering coefficients are reported by [23]. The values for the ILN measures in bold apply to the collapsed Russian ILN (see [24] and Appendix 2.A). With the layer homogeneity we indicate whether the quoted ILN measures apply to all maturity layers of the Russian ILN.

features are valid for the short maturity layers ($G_{<1d}$, G_{2-7d} , G_{8-30d}) and for the collapsed network (G_c), they become progressively invalid with growing loan maturities. As a matter of fact, we find that the stylised facts of the collapsed Russian ILN do not hold over all maturity layers. Given the similarities in the stylised facts across countries, we anticipate a similar behaviour for the ILNs of other countries. The short layers $G_{<1d}$, G_{2-7d} , G_{8-30d} contain 97% of all issued loans. Upon merging those we more or less retrieve the collapsed Russian ILN with all the loan issuances. The longer maturity loans represent a few percent of the issuance but they are of sizeable economic relevance due to their specific turnover and their weight in the outstanding loans (see Fig. 2.2(c)). During times of turmoil the short-term loans are often not renewed, but the long-term ones remain on the books till maturity, making them important for the stability of the ILN. This is reflected in the interest rate spreads shown in Appendix 2.H.

Core-periphery (CP) structure has been observed in many real-world networks [31] and in ILNs [5, 6]. The seminal work of Craig and von Peter [28] introduced an economic foundation for its occurrence in ILNs, i.e. the elementary function of economic intermediation performed by banks. CP structure breaks with traditional theoretical banking literature where the interbank money market is modelled as a centralised exchange in which banks smooth out liquidity shocks. In contrast to

the centralised exchange model, an ILN with CP structure gives rise to a sparse network. Thereby, a group of densely connected "core" banks perform the economic function of financial intermediation between numerous smaller, sparsely connected "periphery" banks. Formally, an ILN has CP structure if the lending patterns can be fully explained by grouping the banks into either "core banks" or "periphery banks". In the ideal situation, the bilateral relations between the banks define the bank group memberships (i.e. whether a bank is core or periphery) by the following set of rules: (i) core banks lend to each other; (ii) periphery banks do not lend to each other; (iii) core banks lend to periphery banks; (iv) core banks borrow from periphery banks. For real-world ILNs with imperfect CP structure, several algorithms have been proposed (e.g. [28, 32]) to detect CP structure and to determine the group memberships. We believe however that the proper way to establish CP structure in networks is by Bayesian inference of SBMs as these are ideally suited to parametrise the CP two-group structure and the four rules mentioned above, rather than minimising an objective function that might detect spurious CP structure, as shown by some recent literature [1, 33, 34]. Inferring CP structure by Bayesian inference of SBMs has been proposed in [35] and applied to the Italian e-MID ILN in [36, 37] where depending on the time scale and SBM model extension, a bipartite or CP structure was found. We find some indications supporting a CP structure in the Russian ILN for G_c and $G_{<1d}$, G_{2-7d} , G_{8-30d} . As explained in Appendix 2.A these indications stem from the heavy-tailed degree distributions, disassortative degree mixing and the small average shortest path length.

Modelling the Russian ILN with the coarse-grained layered SBM

The idea of banks behaving in groups with respect to lending and borrowing because of trading relationships in the interbank money market has been posited in various forms in the literature [6, 12, 26, 28, 38-42], though not often explicitly in the form of SBMs [5, 36, 37]. Such group structure, also called network mesoscale structure, is abundant in real-life complex networks [43], notably social networks [44]. In the Russian interbank money market, there are several reasons to anticipate that the group structure is important: relationships are a way to solve problems with asymmetric information, a pervasive problem in the Russian banking sector and economy at large [45]; fragmentation of the Russian financial market due to the country's size (i.e. eight time-zones); the presence of institutions controlled by the state to various degrees [46]. The most important advantages of using SBMs to detect the group or mesoscale structure are [47]: (i) Theoretical guarantees against overfitting; (ii) They can be extended easily when formulated in a Bayesian setting; (iii) The ability to describe a wide variety of lending patterns (e.g. ILNs modelled by community structure, bipartite structure, CP structure or Erdős-Rényi graphs). As mentioned before, the SBM flavor we use to model the monthly ILNs is the coarse-grained layered SBM, which extends the layered SBM, itself an extension of the standard SBM. With "coarse-grained layered SBM" we refer to an extension to the layered SBM developed in [19] which allows one to infer the OG along with the bank groups and other SBM parameters. We shortly introduce the SBM, the layered SBM and the rationale behind its coarse-grained extension in a qualitative setting before discussing the coarse-grained layered SBM for the Russian ILN. A comprehensive discussion about SBMs in a Bayesian setting can be found in [47] and the coarse-grained layered SBM used in this work is presented in [19, 20].

Introduction to the SBM, the layered SBM and the coarse-grained layered SBM

SBMs are canonical models to study clustering and perform community detection [48, 49]. SBMs model topological patterns by assuming that the nodes "behave group-like" rather than on individual account, i.e. for a network G with Nnodes modelled by $B \leq N$ groups, one assumes that the amount of connections between any two nodes $1 \leq i, j \leq N$ depends only on their group memberships $1 \leq b_i, b_j \leq B$, where b_i is the group assignment of the *i*th node. When formulated in a Bayesian setting, the basic goal of SBMs is to determine the posterior probability distribution of all possible group assignments $\{b_i\}$ (where $B = \max_i b_i$ given the observed network G, a quantity written as $p(\{b_i\}|G)$. Because this is intractable for networks with more than a few nodes and edges, one is typically content with the maximum a posteriori probability (MAP) estimate, i.e. $\operatorname{argmax}_{\{b_i\}} p(\{b_i\}|G)$, to which one refers to as "the fit" to the observed network G. Maximising the posterior $p(\{b_i\}|G)$ in search for the MAP estimate equivalently minimises the information-theoretic description length (DL) of the data G, i.e. $\Sigma = -\log p(G, \{b_i\}) = S + \mathcal{L}$ with $S = -\log p(G|\{b_i\})$ and $\mathcal{L} = -\log p(\{b_i\})$. Choosing the base of the log to be 2, S is the number of bits needed to describe the data (G) given the model parameters $\{b_i\}$ and \mathcal{L} is the number of bits necessary to describe the model parameters. In other words, the best fit to the data is the one that *compresses* it most, i.e. yields the shortest DL. This is the minimum description length principle (MDL).

Though MDL as a regularisation device is fully equivalent to Bayesian model selection [50, 51], we invoke the MDL principle in our qualitative discussion as it provides an arguably more intuitive explanation to how SBMs formulated in a Bayesian setting achieve robustness against overfitting when the model and the prior probabilities accurately represent our (lack of) knowledge [47, 52]. In the case of SBMs the primary parameter that controls the model's complexity is the number of groups *B*. Increasing *B* improves the maximum likelihood fit $p(G|\{b_i\})$ monotonically, as new groups become available to account for any possibly insignificant deviation from the group's behaviour. More complicated mod-

els (larger *B*) are only preferred if there is sufficient evidence available in the data to compensate the extra degrees of freedom. This is achieved in the Bayesian formalism by specifying a prior $p(\{b_i\})$ and subsequent model selection based on integrated likelihoods and statistical significance. From the MDL view this robustness against overfitting is achieved in the following manner: If *B* becomes large, it decreases *S* but increases *L*. The latter functions as a "penalty" that disfavours overly complex models [53]. The optimal choice of *B* minimises the DL Σ , which induces a proper balance between *S* and *L*. In other words, the optimal choice of *B* and $\{b_i\}$ corresponds with the model that compresses the data most.

Layered SBMs are extensions of SBMs that additionally allow the group behaviour to depend on the network layers. In this work we use a specific layered SBM known as the independent layers SBM for all monthly ILNs. The independent layers SBM assumes that a layered network $\{G_l\}$ can be modelled as one group structure which exhibits a topological pattern in each layer. In other words, each layer G_l is modelled by an independent SBM constrained by the fact that the group memberships of the nodes $\{b_i\}$ are the same across all layers. Thus the model complexity of a layered SBM is now additionally controlled by the number of layers L present in the observed layered network $\{G_l\}$ $(1 \le l \le L)$, next to the number of groups B. The increased model power relative to the standard SBM again raises the question of overfitting: given the group structure $\{b_i\}$ of the layered network $\{G_l\}$, is it necessary to posit L different topological patterns for each layer G_l , or can some layers be explained equally well by just one topological pattern and hence be merged? The layered SBM itself cannot provide an answer to this question, as L is determined by $\{G_l\}$ and is thus simply a fixed component of the model complexity.

The coarse-grained layered SBM extends the layered SBM by assuming that the observed "high resolution" layered network $\{G_l\}$ may be explained by an underlying "lower resolution" layered network $\{G_{\ell}\}$ consisting of the merged G_{l} according to $\{\ell\}$, a set of layer bins which specifies the level of granularity of $\{G_{\ell}\}$. The optimal level of granularity (OG) is inferred simultaneously with the number of groups B and the group structure $\{b_i\}$ by searching for the layered SBM that most compresses the *lower resolution* layered network $\{G_{\ell}\}$, while taking into account the inevitable information loss incurred due to the lower degree of granularity (i.e. decrease in quality of fit). When the OG for a given layered network $\{G_l\}$ is complete aggregation, this indicates that the layer divisions in $\{G_l\}$ do not correlate with the mesoscale of its associated collapsed form $\{G_c\}$. By contrast, an OG that is different from complete aggregation points to a mesoscale structure that is too complicated to be understood at the collapsed network level. The OG merges layers such that the layer bins in $\{\ell\}$ "acquire meaning" so that at the bin interfaces the topological patterns between the groups change in a statistically significant way.

The coarse-grained layered SBM for the Russian ILN

We approach the Russian ILN as a time series of monthly ILNs and model each month separately with the coarse-grained layered SBM introduced in the previous section. Note that this choice does not make any assumptions on nor excludes the existence of temporal correlations throughout the months. The specific flavor of the underlying layered SBM that we use is the microcanonical independent layers weighted DCSBM, which takes the following features (above the expected group structure captured by the standard SBM) into account:

- Edge directedness and the possibility of parallel edges, i.e. multiple loans can be made between two banks in a given month.
- Heavy-tailed degree distributions (see Appendix 2.A). This is captured by the degree-corrected SBM (DCSBM) [54].
- Heavy-tailed loan size distributions [24]. This is captured by extending the DCSBM to the weighted DCSBM [20] where the sizes of the loans between bank groups are modelled by log-normal distributions. In this way each ordered pair of bank groups has a lending pattern modelled as consisting of loans whose size's magnitude has a characteristic scale [52].
- Maturity classes, modelled as network layers. This is captured by the independent layer SBM. The lending pattern in each layer is modelled by an independent weighted DCSBM with the constraint that the bank groups are identical in each layer.

Because of computational limitations, we do not explicitly take into account variables such as balance sheets, bank ownership, and interest rates. We deem, however, that this does not severely impact the ability of our model to capture the structural variability in the network. Indeed, structural features originating from the omitted variables can be effectively captured by the model. First, while balance sheets are not explicitly taken into account, we include degree distribution, which correlates to bank size, and loan size distribution (see Appendix 2.A). Second, if bank ownership drives significantly different lending- and borrowing behaviour, these patterns can still be captured by the SBMs without explicitly including the information. It would be interesting to study if and how bank ownership correlates to the function banks fulfil in the different maturity layers. This falls outside the scope of this work. A study of the term structure of interest rates is included in Appendix 2.H. In line with the expectation theory of interest rates [55], the yield-curve is upward sloping for longer maturities. Longer loan maturities lead to higher interest rates through averaging expected future short-term rates and adding a premium for liquidity- and default-risk. The introduction of maturity layers effectively captures the fact that differing risk patterns manifest themselves through differing loan structures in the layers. Recent work on the generative processes of risk in ILNs has shown that information such as interest rate and Credit Default Swap (CDS) spreads [56, 57] play a central role in contagion dynamics. We note that securitised products, CDO, and CDS play a very marginal role in the Russian ILN in our period under study. In this way the Russian ILN provides a natural lab where the control parameter of risk derivatives can be effectively set to zero. In the forthcoming discussion on possible future research directions those opportunities will be highlighted. Local structures such as dense subgraphs fall beyond current SBMs' potential to capture mesoscale structure [47]. In the Methods section we motivate the choice to treat the maturity layers of the monthly ILNs as independent.

The coarse-grained layered SBM augments the parameter set of the layered SBM $\{\theta\}$ by the maturity bin set specifying the level of granularity $\{\ell\}$. Thus its parameters are denoted as $(\{\theta\}, \{\ell\})$. The coarse-grained layered SBM of a monthly ILN $\{G_l\}$ is a generative model given by [19]

$$p(\{G_l\}, \{\theta\}, \{\ell\}) = p(\{G_l\}|\{\theta\}, \{\ell\}) \times p(\{\theta\}) \times p(\{\ell\}).$$
(2.1)

Expressions for the model likelihood $p(\{G_l\}|\{\theta\}, \{\ell\}) \propto p(\{G_\ell\}|\{\theta\})$ and prior probabilities $p(\{\theta\})$ and $p(\{\ell\})$ can be found in [19, 20] where $p(\{G_\ell\}|\{\theta\})$ and $p(\{\theta\})$ are defined by the layered SBM and $p(\{G_l\}|\{\theta\}, \{\ell\})$ and $p(\{\ell\})$ are defined by the coarse-grained extension. As the underlying maturity classes are inherently ordered, the uninformative prior probability for the maturity bin set $p(\{\ell\})$ is determined by the constraint that only contiguous layers may be binned. In Appendix 2.B we infer the OGs under the more general non-contiguous binning assumption (with a different prior $p(\{\ell\})$) and find qualitatively similar results as in Fig. 2.4.

The posterior probability of the parameters $\{\theta\}, \{\ell\}$ is proportional to Eq. 2.1:

$$p(\{\theta\}, \{\ell\}|\{G_l\}) = \frac{p(\{G_l\}, \{\theta\}, \{\ell\})}{p(\{G_l\})},$$
(2.2)

where $p(\{G_l\})$ is independent of $\{\theta\}$ and $\{\ell\}$. We may infer the bank groups $\{b_i\} \in \{\theta\}$ and the OG as the maximum a posteriori probability (MAP) estimate by searching for the mode of Eq. 2.2 (or equivalently Eq. 2.1) with the inference algorithm explained in the Methods. In addition, we can compare the *posterior odds ratio* (POR) Λ between two coarse-grained layered SBMs $\mathcal{M}_a, \mathcal{M}_b$ representing two different levels of granularity $\{\ell\}_a, \{\ell\}_b$ by evaluating the ratio:

$$\Lambda = \frac{p(\{\theta\}_a, \{\ell\}_a, \mathcal{M}_a | \{G_l\})}{p(\{\theta\}_b, \{\ell\}_b, \mathcal{M}_b | \{G_l\})} = \frac{p(\{\theta\}_a, \{\ell\}_a | \{G_l\})}{p(\{\theta\}_b, \{\ell\}_b | \{G_l\})} = \frac{p(\{G_l\}, \{\theta\}_a, \{\ell\}_a)}{p(\{G_l\}, \{\theta\}_b, \{\ell\}_b)},$$
(2.3)

where the constant $p(\{G_l\})$ and the prior beliefs $p(\mathcal{M}_a), p(\mathcal{M}_b)$ for the coarsegrained layerered SBMs \mathcal{M}_a and \mathcal{M}_b have cancelled out, as we had no prior preference with regard to the degree of granularity (i.e. $p(\mathcal{M}_a) = p(\mathcal{M}_b)$). Values of $\Lambda > 1$ indicate that according to the data, $\{\ell\}_a$ is preferred over $\{\ell\}_b$ with a degree of statistical significance given by the magnitude of Λ [20]. The model selection implicit in the POR can be illustrated as follows. Given that Σ_a (Σ_b) denotes the DL of $\{G_l\}$ according to model \mathcal{M}_a (\mathcal{M}_b) the above equation implies that $\log \Lambda = \Sigma_b - \Sigma_a$ and one recovers the MDL principle. Indeed, the preferred model is the one that achieves the most optimal compression of the data. Accordingly, the POR is a model selection criterion that operates similarly to alternate information-based "goodness-of-fit" criteria such as BIC [58] and AIC [59]. The POR criterion, however, is "exact" for the coarse-grained layered SBMs at hand while BIC and AIC rely on specific assumptions about the asymptotic shape of the model likelihood which are known to be invalid for the SBM [47, 60].

We use $\log_{10} \Lambda$ to determine confidence levels for rejecting complete differentiation and complete aggregation as OG for the monthly ILNs. This is achieved by setting in Eq. 2.3 $\{\ell\}_b$ to the OG inferred from the algorithm and $\{\ell\}_a$ to either complete differentiation or complete aggregation. Note that these confidence levels of rejection give rise to values $\log_{10} \Lambda \leq 0$. Large negative values of $\log_{10} \Lambda$ point to strong evidence for rejecting complete differentiation and/or complete aggregation.

Example for a small layered network

As an illustration, we determine the OG for a small network of 50 nodes with three generic interactions (A, B and C) drawn in bundles (Fig. 2.3(a)). Instead of specifying the individual interactions, one can describe the network in a more parsimonious way by specifying the "wiring patterns" between groups of nodes. The nodes are grouped in circles, squares and triangles, so as to encode a specific high-level description of the network. For example, interaction type A does not occur between two squares and between two triangles. Interaction A gives rise to circle-triangle and circle-square interactions. There are no circle-circle interactions of the C type, and circle-circle interactions of the types A and B are sparse. This is the kind of higher-level organisation into groups of nodes that SBMs can infer.

The results of the fits with the coarse-grained layered SBM for three levels of granularity are displayed in Fig. 2.3(b). Comparing the DL Σ for the three fits, the preferred model is the OG {{A,B},C} with $\Sigma = 1687$ bits ≈ 211 bytes. The network in Fig. 2.3(a) can be saved to disk in graph-tool's [61] native binary format as a file with a size of approximately 3,400 bytes, while the OG coarse-grained layered SBM can compress this (e.g. using arithmetic coding) down to $\Sigma \approx 211$ bytes (excluding the bytes needed for storage of practicalities [62] such as the file header). We use the POR Λ of Eq. 2.3 to determine the confidence levels. The model {A, B, C} that stands for complete differentiation is rejected with $\log_{10} \Lambda \approx -80$, indicating that it is an overly complicated model of the



Figure 2.3: Illustration of inferring the optimal granularity (OG) for a small network with the coarse-grained layered SBM. Images created with the graph-tool Python library [61].
(a) An undirected and unweighted network with three types of edges (representing three generic interactions of type A, B, C) and three types of nodes (circle, square, and triangle). The interaction types define the network layers. Their network structure can be described as: perfect core-periphery (CP) (layer A), imperfect CP (B), and community structure (C).
(b) The network is shown with three levels of granularity. From left to right, these are: complete differentation {A, B, C}; merging of layers A and B with a lonestanding C {{A, B}, C}; and the merging of layers B and C with a lonestanding A {A, {B, C}}. The nodes are coloured according to the group index b_i inferred by the coarse-grained layered SBM. The description length \$\sum [bits]\$ and posterior odds ratio \$\Lambda\$ relative to the OG for each representation are also indicated. The OG for this network is {{A, B}, C}. This can be understood by realising that both layers A and B have CP structure so that the merged layer {A, B} can be described more efficiently by just one CP model.

group structure. Indeed, the wiring patterns in layers A and B can be summarised neatly by merging them, since the inferred groups in $\{A, B, C\}$ and $\{\{A, B\}, C\}$ are identical. In contrast, merging layers B and C induces a change in group structure where the distinction between the squares and triangles is lost and these two groups are aggregated into one with many internal interactions. It is worth mentioning that the $\{A, \{B, C\}\}$ model is still a more appropriate description of the





network than the $\{A, B, C\}$ one.

Fitting the coarse-grained layered SBM to the monthly ILNs

For each monthly ILN $\{G_l\}$ we fit the coarse-grained layered SBM by the MAP estimate of its parameters $(\{\theta\}, \{\ell\})$. From this we obtain a time series of the OGs and the bank groups $\{b_i\}$.

The monthly OGs

Fig. 2.4 shows the monthly OGs together with the PORs relative to complete differentiation and complete aggregation. As noted before, each OG consists of a set of bins numbered from short to long maturity by the OG bin index (OGB index). The most important result is that complete aggregation is always rejected as the appropriate level of granularity for $\{G_\ell\}$. The maturity layers are thus informative of the monthly ILN's network structure in the sense that including them in a layered SBM yields an improved description compared to a layered SBM of the collapsed monthly ILN $\{G_c\}$, because the lending patterns between the bank groups depend significantly on the maturity classes of the loans. In other words, the lending patterns in the monthly ILNs $\{G_l\}$ correlate with the maturity classes in a way that cannot be captured completely by just considering the loans alone, i.e. without maturity information. This is also indicated by the fact that complete differentiation is seen to yield substantially better fits to $\{G_l\}$ than complete aggregation. The $\log_{10} \Lambda$ of Eq. 2.3 that measures the degree of rejection, tends to increase until roughly month 50 (February 2004), after which the degree of rejection becomes weaker. This aligns with the timing rumours surfaced about a large scale government investigation into money laundering by banks. This eventually caused several bank licenses to be withdrawn, see Appendix 2.F for a timeline.

The eight maturity classes reflect the CBR's reporting standards. One may therefore ask whether all eight classes also have an economic function in the actual lending and borrowing between banks. Interestingly, the OGs are always different from complete differentiation, which means that the maturity classes as defined by the CBR are partly redundant and that the lending patterns may be described more effectively by merging maturity layers into bins according to the OG. The OGBs are indicative of the fact that lending patterns between the bank groups can be combined in a more comprehensive form. For example, the short layers ($G_{<1d}$, $G_{2.7d}$, $G_{8.30d}$) which are characterised by the ILN stylised features in Table 2.1 are almost always merged together. We emphasise that this does not necessarily indicate pointwise similarity between these layers; rather the merging of the layers in the OGB induce a new lending pattern between the bank groups that is significantly different from the other OGBs.

Figure 2.4(a) shows that the number of OGBs increases with time, which points to a developing interbank money market as more significantly differing lending patterns emerge between the bank groups. An additional argument is that the OGs differ more and more from the complete aggregation (see Fig. 2.4(b)). Indeed, the monthly number of bins in the OG correlate with the known two phases in the Russian money market's development: early development (before month 35) and emerging maturity (from month 35 onward) (see Methods). This indicates that the market's emerging maturity phase is characterised by a more complex layered SBM with up to four statistically significantly lending patterns between the bank groups. This is in contrast with the early development phase, where mostly only two lending patterns are discerned (maturities up to 30 days and maturities longer than 30 days). In other words, the interbank market can be characterised during the early development phase by the existence of only two distinct lending strategies between the bank groups.

The bank groups

In Fig. 2.5(a) we display the number of groups B ($1 \le b_i \le B$) inferred for each monthly ILN. As B > 1 across time, the monthly ILNs do contain group structure.

Second, B follows the same upward trend as in Figs. 2.2(a),(b); 2.4(b), indicating that the increase in the number of groups goes hand in hand with the development of the Russian ILN into a more mature phase as the months in our dataset pass.

We now gauge the time correlations between the inferred monthly group structure by looking at the similarity between the inferred bank groups $\{b_i\}$ in consecutive months. Fig. 2.5(b) shows the normalised mutual information (NMI) between the $\{b_i\}$ in a given month t and the previous month t - 1. In the Russian ILN, one discerns non-important banks. They display little activity over time and volume, and accordingly they are inclined to fluctuate between groups. To account for this, we condition the NMI on q, a measure to control which bank strengths [63] are included. The strength s_i^l of a bank i is defined by the total amount it borrows and lends in a layer l during a certain month:

$$s_i^l = s_i^{l,\text{in}} + s_i^{l,\text{out}} = \sum_{j,k} x_{jik}^l + \sum_{j,k} x_{ijk}^l .$$
(2.4)

We also define the size of a maturity layer $S^l = \sum_{i < j,k} x_{ijk}^l$ as the total amount borrowed or lent during a certain month. The size of the monthly ILN is given by $S = \sum_{l} S^{l}$. To construct Fig. 2.5(b), we calculate for each month t the relative strength of each active bank $s_i = \sum_l s_i^l / 2S$. Then we create a list of banks by adding one bank at a time, starting out with the strongest bank and proceeding in order of decreasing bank strength, until the cumulative relative strength reaches q, and we include only the banks on this list in the analysis. In this way, we exclude banks that are only responsible for an insignificant amount of lending and borrowing in the network. We intersect the included banks with those at time t-1 and calculate the NMI from the two intersected bank group memberships for q = 0.95, 0.99, 1. Figure 2.5(b) shows that with decreasing q the NMI grows, pointing to increasing similarity between the inferred bank groups at consecutive months. It is hard to draw conclusions from the NMI without a reference. By excluding the "5% least important banks by strength" $(q = 1 \rightarrow q = 0.95)$ a considerable increase in correlations between the inferred bank groups in consecutive months is observed. This is indicative of the temporal stability of the inferred groups. This temporal stability emerges from the analysis without explicitly imposing intertemporal correlations in the algorithm. The temporal stability of the inferred groups is indicative for the robustness of the findings and corroborates the role of relationship lending in interbank markets. Explicitly modeling intertemporal correlations by means of a dynamic layered SBM model [19, 64] turned out to be computationally prohibitive when applied to our data. Another advantage of the adopted "static" layered SBM methodology is that it can be applied to both time series of ILN data and ILN data covering a specific time period. In addition, treating the monthly data independently provided an additional robustness check as the anticipated intertemporal correlations are recovered by the algorithm. Inversely,



Figure 2.5: Information about the bank groups $\{b_i\}$ for the monthly Russian interbank lending networks as inferred from the optimal granularity (OG). (a) Temporal evolution of the number of different bank groups. The number of groups roughly increases until t = 50. This indicates that the mesoscale structure of the monthly interbank lending networks becomes progressively more complex as more bank groups are needed to fit the lending patterns. (b) The temporal evolution of the normalised mutual information (NMI) between the OG group memberships of the set of banks active in two consecutive months (t, t - 1)for three strength fractions q. For example, for q = 0.95, banks responsible for 95% of the network's lending and borrowing are included. In many fields, including community detection, the NMI is a popular quantity to measure the similarity between two partitions of a set [65].



Figure 2.6: Correlations between aggregate loan sizes and lending patterns: the size of the optimal granularity bins (OGBs) through time. The size of an OGB is defined as the total amount of issued money in the interbank lending network defined by the OGB. The OGB indices and colours correspond to those of Fig. 2.4(a).

our results also indicate that intertemporal correlations can be exploited to reduce the computational complexity of the modelling of "current" ILN data by using the inferred structure of the ILN in preceding months as a reasonable initial estimate for the underlying structure.

2.4.0.1 Characterisation of the OGBs

The OGBs can be interpreted as corresponding with statistically significant differing lending patterns between the bank groups. For consistency, we numbered the bins in the OG with an OG bin index (OGB index) from short to long maturity.



Figure 2.7: The time-integrated distribution of the strength and the instrength/strength ratio of the monthly "important banks" for the four optimal granularity bins (OGBs). As in Fig. 2.5(b) we gauge a bank's importance by its strength: For a given month a bank is deemed important if its strength lies in the top 10%. With growing OGB index, the important banks increasingly tend to either lend or borrow. Banks in OGB 1 and OGB 2 tend to balance lending and borrowing. This suggests that the economic function of the important banks in the various OGBs changes from financial intermediation (short maturity bins) to financing (long maturity bins) on a monthly time scale.

Even though their actual content can vary considerably through time, we find that this numbering scheme reveals surprisingly consistent patterns.

At the *network level*, Fig. 2.6 displays the OGB sizes $S^{\ell} = \sum_{l \in \ell} S^{l}$ throughout time. We see that the order of magnitude of the OGBs corresponding with the shorter maturities stays consistent across time, even though the composition of the OGBs (i.e. the maturity layers in the OGBs) changes considerably through time. This is especially so for OGB 2 (see Fig. 2.4(a)): it contains the long maturity layers during the early development phase but not during the emerging maturity phase. It is interesting to note that while the sizes of the "longer" OGBs are much smaller than the short ones, these are not merged in the emerging maturity phase of the Russian ILN. This points to lending patterns that are sufficiently different from those in the short OGBs. (This still holds, except in one month, for the noncontiguous binning in Appendix 2.B.)

Finally, we look at the *bank level*, i.e. the lending behaviour of individual banks. Again we use the bank strength to single out the "important" banks. In Fig. 2.7 we have shown the time-integrated distribution of $s_i^{\text{in},\ell}/s_i^{\ell}$ of the top 10% most important banks of each month, separately for each OGB ℓ . (Note that the conclusions hold for other cutoffs – see Appendix 2.E.) The instrength of a bank *i* in maturity bin ℓ during a certain month is $s_i^{\ell,\text{in}} = \sum_{l \in \ell} \sum_{j,k} x_{jik}^l$, and the strength s_i^{ℓ} is defined analogously as in Eq. 2.4. At monthly time scales the important banks in "short" bins tend to both lend and borrow equal amounts of cash, while the important banks in the "long" bins tend to either lend or borrow, i.e. act either as sources or sinks of liquidity. Together with the indications for CP structure in the short layers, this suggests that the economic function of the important banks changes from financial intermediation (short bins) to financing (long bins). The

apparent patterns in the short bins are indeed reminiscent of the functions in CP structures, while those in the long bins have, to the best of our knowledge, not often been included in the literature. Thus our coarse-grained layered SBM of the ILN uncovers a correlation between statistically significant lending patterns between the bank groups, the economic functions of the important banks, and the maturity classes of the loans involved.

Discussion

In this paper, we investigate the importance of loan maturity information in interbank lending networks towards understanding its mesoscale structure, i.e. the higher-level organisation of the banks into groups. We do this to better understand the possible diversity in lending and borrowing patterns between bank groups in ILNs and their accompanying economic functions. We find that the representation of ILNs common in the literature, where either one maturity layer is studied or an aggregated view on the maturity layers is used, is unable to fully uncover information on the diversity in structures and underlying functions of interbank loans. Even after introducing multi-directedness, degree distribution, and loan size distribution, the economic functions carried out by banks are obscured by aggregating maturity information in the ILN representation.

We employ the complete population of all Russian unsecured interbank lending contracts over a 57 months period (January 2000 - October 2004, except January 2003) containing uniquely granular loan maturity classes as defined by the CBR. Descriptive statistics on the associated maturity layers uncover non-homogeneity in network measures along loan maturity layers, indicating a diversity in lending and borrowing patterns.

To investigate the optimal maturity granularity, we apply a coarse-grained layered stochastic block model [19] to the data. The subsequent analysis confirms the suboptimality of complete maturity aggregation for our dataset, as it obscures the existence of four maturity layer bins that contain significantly distinct lending- and borrowing patterns with various underlying functional economic interpretations. We find, for example, a consistent shorter term maturity layer bin that behaves in line with the theory around tiered banking, with important banks intermediating liquidity. We also detect another layer bin that aligns with long-term financing of bank activities, with the important banks acting either as sources or sinks of liquidity.

These findings immediately imply that the common practice of complete maturity collapse or focus on a single maturity layer, by choice or for data limitations, obscures important information about the functions banks perform in an ILN. This leads potentially to unrealistic ILN models and misguided policy conclusions about systemic stability, especially so in times of liquidity crunches when the short term layer of the ILN issuance network collapses. These insights also align with and add to recent findings that banks use the different loan maturities to manage their duration gap, providing a direct link from interbank markets to financial stability and the allocative efficiency of the economy at large [2].

The lending patterns between the bank groups depend not only on the loan maturities but also on the phase of development of the interbank money market. The longest maturity loans, for example, only show structure related to interbank financing at later phases of market development. This makes economic sense since long-term loans entail greater counter-party risk and counter-party trust is only established over time through engagement in long term relationships.

Our analysis builds on the strand of interbank literature that leverages the network representation of interbank systems. Thereby, one often starts from the topology of exposure networks while largely disregarding loan maturity and other meta-data on the banks and their connections. Our work conclusively illustrates that after accounting for distinct loan issuance and degree- and loan size distributions, loan maturity is still informative of structure and economic functions. Alternate approaches have specifically focused on systemic risk and contagion and concluded that funding risk and CDS spreads play a central role in the mechanisms of risk propagation. It remains an open question how the structural information in maturity layers could complement these approaches. The trust crisis in Russia has indicated that the occurrence of a non-fundamentals crisis is clearly reflected in both the interest rates and the mesoscale structure of the maturity layers. This connection offers opportunities for future research.

All in all our results imply that theoretical and empirical research can neither adequately grasp the generative process of ILNs nor arrive at reliable policy conclusions from ILN modelling and simulation in the absence of appropriate granular maturity information. This underlines the importance for policy and regulatory bodies to collect maturity information on interbank loans if they desire to arrive at reliable insights into the health and systemic stability of the interbank lending market. It should also stimulate further theoretical and empirical research that incorporates loan maturity in modelling of the ILN generative process, its dynamics and its occasional transition to phases of instability or collapse.

Methods

Dataset

Overview

The interbank data analysed in this work offers a rich and unique account of Russian commercial bank activities over a six-year timeline (August 1998 - October 2004). The data is provided by Schoors and Karas [17] and has been painstakingly

assembled from public and private sources. It originates directly from the information reported to the CBR about interbank contracts. The dataset used in this paper can be retrieved on demand from the authors. To the best of our knowledge the dataset is unique [13] in quite a number of aspects. We mention the availability of information about the issuance months of loans (most often only the derived exposure is available) and rather detailed granular information about the maturity (see Appendix 2.G). The fact that the Russian interbank market went through many stages of development during 1998-2004 adds an additional layer of dynamics. Note that the CBR is not included as a node and that we do not have information about any of its transactions. A classification of the banks together with a recent description of the money market can be found in [46]. On average, about half of the Russian banks are active on the interbank market [24]. The dataset starts a few weeks before the so-called "1998 Russian default" [66], which caused a complete collapse of the interbank money market. In response the CBR imposed to little avail several extraordinary measures to stabilise the market. These exceptional circumstances greatly disrupted the workings of the interbank market and because of this we have restricted our analysis to the period of 57 months from January 2000 until October 2004. In our numbering scheme month 1 corresponds to January 2000, month 13 to January 2001, and month 58 to October 2004. As can be inferred from Fig. 2.2, during months 1-35 the market is developing. We refer to this period as the early development phase. Roughly starting from month 35 (December 2003) the interbank market enters an emergent maturity phase: the amount of active banks stabilises and the share of overnight loans declines in favour of longer-maturity loans. The emergent maturity phase includes the trust crises in the second half of 2003 and the summer of 2004 caused by a money laundering scandal (see Appendix 2.F for more details). As compared to the Russian default of 1998, the crises of 2003 and 2004 were less disruptive for the interbank lending market.

Contents

The data consists of the issuance of domestic unsecured interbank loans, annotated by lender bank ID, borrower bank ID, month of issuance, loan size, interest rates and maturity class. As noted earlier, the loan interest rates are not incorporated into the coarse-grained layered SBM; we discuss them in Appendix 2.H. The loan issuances are reported to the legislator on the first day of each month throughout August 1998 up until November 2004 in one of the following eight maturity classes: overnight (less than one day, <1d), 2-7 days (2-7d), 8-30 days (8-30d), 31-90 days (31-90d), 91-180 days (91-180d), 0.5-1 year (0.5-1y), 1-3 years (1-3y), more than 3 years (>3y). Because of this reporting standard, the precise issuance month of the loans is known. For January 2003 (month 36) there is no data available. Whenever possible, we interpolate the missing month in the time series. For some

variables (Figs. 2.4(a) and 2.5(b)) this is not feasible and this is at the origin of the missing data point in the time series.

Aggregation window

Loans are aggregated by issuance month into monthly ILNs (as in [24]) for two reasons. First, monthly aggregation is the most granular time scale available in the data. Second, monthly compliance with regulatory requirements for banks (e.g. for liquidity and capital) induces a monthly periodicity in the data.

Implementation

Inference algorithm with agglomerative hierarchical clustering

We infer the OG for a layered network using an agglomerative hierarchical clustering heuristic as suggested in [19]. At the start of the procedure each layer is put in its own bin. In the next steps, bins are merged so as to reduce the overall DL. The overall DL consists of the DL of the layered SBM plus an "SBM extension term" that accounts for the model selection between the possible levels of granularity (Eq. 17 in [19]). With contiguous binning only contiguous bins are merged, while for non-contiguous binning any pair of bins may be merged at each step. In this way a series of layered networks is generated, starting with the original layered network and ending with the collapsed network. The layered network with the smallest overall DL defines the OG.

We use the efficient inference algorithm [67] implemented in the graph-tool library [61] to fit the layered SBMs to the monthly ILNs. The algorithm employs an agglomerative heuristic to fit the layered SBM and a multilevel Markov Chain Monte Carlo to sample the posterior distribution. We used High Performance Computing resources to perform four runs of numerical calculations: Two of those used contiguous binning and two of those used non-contiguous binning for the maturity layers. In each run we used agglomerative hierarchical clustering to fit the layered SBM and to sample the posterior for the levels of granularity generated for each of the monthly ILNs. The number of samples were set to 10,000 and 25,000 for both the contiguous and non-contiguous runs. All runs (including the test runs) yielded similar results for each monthly ILN which alludes to the stability of the posteriors. The layered SBMs with smallest DLs were gathered from both runs.

Appendix

2.A Maturity layer analysis

Here we give a detailed description and network analysis of the Russian interbank lending network to compare to other interbank networks used in research. We divide the Russian interbank loan network $\{G_{\alpha}\}$ by maturity class α into separate layers consisting only of the loans with loan maturity inside each maturity class. (Note that in the main text we use the symbol l instead of α .) We evaluate the properties per maturity layer (often also referred to as layer for simplicity) to show the differences between them. We denote the eight maturity layers as: $G_{<1d}$, G_{2-7d} , G_{8-30d} , G_{31-90d} , $G_{91-180d}$, $G_{0.5-1y}$, G_{1-3y} , $G_{>3y}$.

2.A.1 Activity and volume

One expects that the number of banks participating in a given loan maturity layer decreases as the loan maturity lengthens. Table 2.A.1 shows that this is approximately correct. More importantly, one sees that the number of active banks becomes very small for G_{1-3y} and $G_{>3y}$. We define an active bank as a bank that has lent or borrowed at least once in a given time window and maturity layer. We will always only consider active banks to deal with the death and birth of banks in the Russian interbank market over the course of time [68]. For the layers with long loan maturity, this results in an exceedingly high average lending activity per bank, comparing to layers with shorter loan maturity. It seems that $G_{>3y}$ is occupied by a small club of banks that trade relatively intense.

Table 2.A.2 lists the yearly, and average monthly lending activities by loan maturity class, where we define the *lending activity* simply as the number of loans recorded during a certain period. A crucial observation is that the lending activity sharply decreases for longer maturities, which is also reported for other interbank markets in [1]. We see that the overnight segment ($G_{<1d}$) is the most active, together with G_{2-7d} .

Table 2.A.3 lists the total loan volumes (i.e. loan sizes) by loan maturity layer and year. We observe that the relative importance of each maturity segment, as measured by the total volume of loans traded within it, follows the ranking of the loan maturity lengths. The loan volumes are log-normally distributed [24],

	1998	1999	2000	2001	2002	2003	2004
<1d	610	810	878	954	1,022	1,027	983
2-7d	589	907	953	1,026	1,074	1,098	1,058
8-30d	375	849	920	980	1,018	1,054	986
31-90d	166	535	648	698	706	775	686
91-180d	63	203	265	310	321	429	378
0.5-1y	49	120	132	169	204	258	259
1-3y	24	64	80	60	58	113	107
>3y	11	45	29	38	33	23	20
	1998	1999	2000	2001	2002	2003	2004
<1d	13	118	187	258	286	337	225
2-7d	7	57	108	161	183	229	147
8-30d	3	15	32	43	44	59	43
31-90d	1	5	10	11	15	18	12
91-180d	1	2	3	4	5	7	5
0.5-1y	1	2	2	4	4	7	7
1-3y	2	3	3	3	3	8	8
>3y	5	3	6	10	78	74	44

Table 2.A.1: (top panel) The number of active banks involved in loans by maturity layer and year. A total of 1,040 banks are present in the data. (lower panel) The number of loans per active bank by maturity layer and year, obtained by dividing the top panel of

Table 2.A.2 and the top panel of this Table element-wise. Care must be taken when interpreting; this is not indicative of an 'average' bank since the degree distributions are heavy-tailed (as will be discussed below). Also note that the columns '1998' and '2004' are biased because they are incomplete in the data (respectively 5 and 10 months missing months).

especially for shorter loan maturities. Because of the considerable variance on a linear scale, these averages may be interpreted only as rough order of magnitude estimates. In general, log-normal distributions are reasonable descriptions for observers that only know the order of magnitude of the mean and the variance of a random variable [52].

	1998	1999	2000	2001	2002	2003	2004
<1d	7,917	95,389	163,855	245,840	292,048	346,22	21 220,979
2-7d	4,325	51,673	103,376	165,602	196,765	251,00)6 155,834
8-30d	958	12,914	29,250	42,067	45,204	62,19	42,18
31-90d	245	2,770	6,365	7,939	10,606	14,18	8,443
91-180d	82	460	742	1,189	1,754	2,79	97 2,010
0.5-1y	63	237	307	593	886	1,90)1 1,899
1-3y	52	207	279	202	180	91	4 845
>3y	55	128	180	367	2,588	1,71	2 890
	199	8 1999	2000	2001	2002	2003	2004
<1d	1,58	3 7,949	13,655	20,487	26,550	28,852	22,098
2-7d	86	5 4,306	8,615	13,800	17,888	20,917	15,583
8-30d	19	2 1,076	2,438	3,506	4,109	5,182	4,218
31-90d	4	9 231	530	662	964	1,182	844
91-1800	d 1	6 38	62	99	159	233	201
0.5-1y	1	3 20	26	49	81	158	190
1-3y	1	0 17	23	17	16	76	84
>3y	1	1 12	15	31	235	143	89

Table 2.A.2: (top panel) Lending activity, defined as number of of loans, by loan maturity class and year. Note that 1998 and 2004 are incomplete years in the data, counting 5 and 10 months respectively. (lower panel) Monthly average lending activity by loan maturity layer. Time series of the lending activity can be found in Fig. 1 in the main text.

	1998	1999	2000	2001	2002	2003	2004
<1d	226.3	2,674.4	5,984.3	8,855.9	10,306.4	13,844.6	13,040.1
2-7d	83.1	1,030.4	2,910	5,114.7	6,104.6	9,058.1	7,880.2
8-30d	15.9	220.7	620.8	1,103.1	1,102.9	1,871.8	1,833.3
31-90d	4.4	31.9	105.2	205.3	318.3	415.4	253.6
91-180d	1.7	5.3	9.6	23.4	46.9	73.6	73.7
0.5-1y	3.2	2.4	8	20.2	24	50.8	69.9
1-3y	2.2	5.5	6	6	3.3	10.1	11
>3y	2.6	0.8	1.2	1.4	1.3	0.8	2.5

Table 2.A.3: Total loan volumes by loan maturity and per year in billions of rubles.

2.A.2 Maturity layer activity of banks

A node *i* is defined as active on layer α if it has at least one connection on this layer, i.e. its degree $k_i^{\alpha} > 0$. In symbols,

$$b_i^{\alpha} = \begin{cases} 1 & \text{if } k_i^{\alpha} > 0, \\ 0 & \text{otherwise.} \end{cases}$$
(2.5)

The total activity B_i measures the number of layers the node participates in, i.e. $B_i = \sum_{\alpha} b_i^{\alpha}$ [9]. Figure 2.A.1 shows the distribution of B_i on monthly time scales. We see that the average total activity grows steadily as the network develops, finally settling around at a value of about three. Almost no banks make use of more than six maturity layers on a monthly basis. The distribution of the total activity is quite broad and relatively unpeaked, especially during the stable phase of the network. This has been reported as a typical quality of real-world multiplex network [69].



Figure 2.A.1: For a given month, the area between the thick lines is proportional to the relative number of active banks with a certain B_i value, which is indicated on the right. The dashed lines make up the moving coordinate system of $\langle B_i \rangle$, in relation to which the average total activity indicated by the thick purple line must be understood. For example, $\langle B_i \rangle$ is about 2 (3) for month 1 (75). The summer of 2004 crisis is mirrored by the drop in $\langle B_i \rangle$ during the last months.

2.A.3 Density

Real-world interbank networks are typically *sparse*, meaning that in directed and undirected views of the network only a small fraction of all possible edges exist. One can then ask how the edges are distributed among the banks. To this end, we define the *degree* of a node. For undirected networks, this is the number of edges connected with a given node, i.e. the number of the bank's counterparties. For directed networks, the in-degree (out-degree) of a node is the number of incoming (outgoing) edges. The in-degree (out-degree) of a bank is then simply the number of loans borrowed (lent) by it.

The above seen differences in lending and bank activity per loan maturity layer is reflected in the directed density of the layers, shown in Fig. 2.A.2. All layers can be considered sparse, except for G_{1-3y} and $G_{>3y}$, which have respectively moderate and an extremely high density [70]. We also observe that the density in almost all layers grows steadily as the network develops, pointing to an increasing interconnectedness with increasing development of the market [71].



Figure 2.A.2: The yearly density per loan maturity layer in the directed Russian interbank lending network. The directed density for a simple graph with N nodes and E edges is defined as $d = \frac{E}{N(N-1)}$.

2.A.4 Degree distribution

Interbank networks, like many real-world networks [43], exhibit heavy-tailed degree distributions. In a nutshell, this means that *few nodes have many links and many nodes have few links*. In general, many typical distributions are heavy-tailed – in fact, they abound in descriptions of natural events like avalanches, earthquakes, turbulent flow and rainfall [72, 73]; another example in economics are the non-Gaussian return distributions in financial markets. Early work in the previous decade tended to postulate power laws for the degree distributions. Networks whose degree distributions follow a power law (at least asymptotically) are called *scale-free* networks. However, while agreeing on the heavy-tail character, recent literature has cast serious doubt on the idea that power laws are the best candidate for the degree distributions, and thus on the scale-free character of interbank networks. In our case, power laws have been decisively rejected as best fit candidates for the heavy-tailed degree distributions of the ¡1d and 2-7d loan maturity by Vandermarliere et al. (2015) [24].

We plot the heavy-tailed degree distributions with complementary cumulative distribution functions (ccdfs) [73] with doubly logarithmic scales. If we denote the degree and its distribution by k and p(k) respectively, the ccdf is given by

$$\operatorname{ccdf}(k) \equiv 1 - \operatorname{cdf}(k) = P\left(k \le k'\right) = \int_{k}^{\infty} p(k') \,\mathrm{d}k', \qquad (2.6)$$

where cdf(k) is the usual cumulative distribution function.

The degree distributions are shown per loan maturity layer in Figures 2.A.3 and 2.A.4. Each loan maturity layer exhibits fat-tailed in- and out-degree distributions, with the maximum degrees separated some 5 ($G_{>3y}$, in-degree) to 18 (G_{8-30d} , in-degree) standard deviations from the mean. Vandermarliere et al. (2015) [24] established that stretched exponentials of the form

$$f(d) = Cd^{\beta-1} \exp\left(-\lambda d\right)^{\beta}$$
(2.7)

provide the best overall fit for the bulk+tail multi-directed in- and out-degree for monthly and yearly time windows. In Eq. 2.7, d is the in-degree or out-degree, C a normalization constant and λ , β distribution parameters. The stretched exponential can be understood as a Weibull distribution, with β being the shape parameter, and $1/\lambda$ the scale parameter. If $0 < \beta < 1$, the distribution has a fat tail, with a smaller β putting more weight towards smaller d. $1/\lambda$ widens the distribution, the mean of f being proportional to it.

We fitted f to the degree distributions to see if the result by Vandermarliere et al. (2015) [24] can be extended to longer maturities. The conclusions are identical for the in- and out-degrees. First, the stretched exponential fit does seem to describe the time-aggregated degree distributions of $G_{<1d}$, G_{2-7d} and G_{8-30d} . Then the leap in residual sum-of-squares suggests that G_{31-90d} and longer maturities can not be satisfactorily described by the stretched exponential. This is confirmed by visual inspection. While (parts of) the bulk distributions of the longer loan maturities are reasonably well captured by f, the fits systematically underestimate the ccdf in the tail; put differently, they underestimate for a given large degree d how many nodes exists with an even larger degree d'.

To investigate whether frequent lenders are also frequent borrowers, we first rank the banks with regard to in- and out-degree, then we calculate Kendall's coefficient of concordance W, which measures the rate of agreement 0 < W < 1



Figure 2.A.3: In-degree distribution with attempts to fit the bulk+tail with stretched exponentials, drawn as piecewise linear functions connecting each predicted value. The correspondence with this distribution seems to break down for layers with loan maturity longer than 8-30d. Inferred (λ, β) parameters for $G_{<1d}, G_{2-7d}, G_{8-30d}$ are (2.6e - 3, 4.3e - 1), (3.4e - 3, 4.8e - 1), (1.0e - 2, 5.8e - 1) respectively, with all standard errors below 1%.

between two rankings, per loan maturity layer. The significant results together with the joint degree distributions are shown in Fig. 2.A.5. We conclude that lending and borrowing are highly correlated for $G_{<1d}$, G_{2-7d} , and G_{8-30d} ; in other words, the dominant lenders are likely to be dominant borrowers, and vice versa. This correspondence breaks down markedly for the layers with longer loan maturity, with orderly decreasing W but insignificant test results. This can also be seen in the shapes of the contour plots in Fig. 2.A.5: high in-degree - out-degree correlation is marked by squeezed contours around the plot diagonal, which does not hold for maturity longer than 31-90d. G_{1-3y} and $G_{>3y}$ even display modest anticorrelation for the degree tails, meaning that the most frequent lenders (borrowers) area unlikely to be among the most frequent borrowers (lenders).



Figure 2.A.4: Out-degree distribution with with attempts to fit the bulk+tail with stretched exponentials, drawn as piecewise linear functions connecting each predicted value. It is clear the correspondence with this distribution breaks down for layers with loan maturity longer than 8-30d. Inferred (λ, β) parameters for $G_{<1d}$, G_{2-7d} , G_{8-30d} are (1.5e-3, 5.3e-1), (2.3e-3, 5.7e-1), (8.3e-3, 6.1e-1) respectively, with all standard errors below 1%.



Figure 2.A.5: The time-aggregated joint degree distribution for each layer, drawn as density contour plots with almost transparent data points. For the first four maturity bins, a highly significant Kendall W was obtained and put in the top left corner of the panel. Note that all scales are equal for easy comparison.

2.A.5 Average shortest path length

The average shortest path length (denoted from here on as just 'average path length') *D* is defined for the largest connected component of the undirected view of interbank networks. It indicates the typical distance between two randomly chosen nodes, i.e. the smallest number of edges needed to reach one node from the other. *Small-world networks* are characterized by high clustering and small average path length. Both should be compared to their mean values in an ensemble of random networks with the same number of nodes and edge [74].

Most studies find that D is small for interbank networks, which indicates compact network structure, but not all conclude that they are small-worlds. Hubs tend to lower the average path length; scale-free networks are ultra-small-worlds. D is a measure of the typical length of intermediation chains that are taking place among the market participants (at least in the largest connected component). Longer intermediation chains arise when D is large, which effectively contribute to slowing down the market transactions between participants and consequently harming the liquidity allocation between financial institutions. In contrast, when D is small, the information between the market participants flows quickly in the network, giving rise to a well-functioning liquidity allocation in the market [27].

In the case of the Russian interbank network, the average path length peaks at times when the network is in crisis, and decreases gradually when the network is maturing. The same patterns have been reported in other empirical literature, such as in [26].

Figure 2.A.6 shows that exclusively for the layers with loan maturity ;90d the average path length D decreases roughly linearly when the size of the largest connected component (LCC) increases *logarithmically*. Herein the LCC covers the vast majority of the active banks within yearly time windows, see Fig. 2.A.7. Thus we see that core-periphery structure, which we expect in these layers from our analysis in the Topology section, is extremely effective in channeling and intermediating liquidity; of course this comes at the cost of systemic risk in the core hubs.

The remaining layers display the familiar pattern: the size of the largest connected component shrinks for longer maturities, while simultaneously the network becomes increasingly fragmented as the number of unconnected components increase, relative to the number of active banks (Fig. 2.A.8) – both tend to suppress D.



Figure 2.A.6: The average (shortest) path in function of the size of the largest (weakly) connected component. For the four shortest loan maturity layers, the points lying astray from the dense cloud all occur during the first five months. Note that the number of banks in the largest connected component for these layers is notably larger than those of the remaining layers.



Figure 2.A.7: The relative size of the largest connected component, given the weak or strong requirement, is calculated by dividing the number of banks in the largest connected component by the total number of active banks in a specific layer and year. The fat (thin) lines indicate the weak (strong) version.



Figure 2.A.8: To compare the number of (weakly) disconnected components with the number of active banks per year, consult Table 2.A.1 on page 48. The relative size of the largest weakly connected can be found in Fig. 2.A.7.

2.A.6 Clustering coefficient

Clustering coefficients measure to which extent banks form triangles. Put differently, they measure the tendency of connected nodes to have common neighbors in undirected views of interbank networks.

According to Bargigli et al. [1], an inverse relationship between the degree and the clustering of a node is observed quite commonly. In the core-periphery picture, low clustering values of core nodes indicate that they essentially behave as star centers. A star graph exhibits zero clustering, as the periphery nodes are unconnected amongst themselves. Consequently, deviations from the star graph, which has idealized core-periphery structure, can be probed by measuring the local clustering coefficients of the periphery nodes. One can identify these heuristically by simply considering the nodes with low degree, so the aforementioned inverse relationship hints that the core-periphery structure may exhibit considerable complexity. A second and more robust implication is that the clustering coefficient of the complete interbank network is dominated by the clustering of low-degree nodes if this inverse relationship is observed together with heavy-tailed degree distributions.

High clustering has obvious implications for systemic risk [24] and therefore clustering coefficients are of interest to the interbank network literature. Table 1 in the main text shows, that at least a few studies claim opposite 'typical' values for clustering coefficients. This may be due to the fact that the clustering tends to increase with longer time windows [1], or that the coefficients may not have been compared to the mean clustering coefficient obtained for random networks of the same size and number of edges.

The *local* clustering coefficient [43] of a node *i* is defined in function of triangle motifs in undirected networks:

$$C_i = \frac{\text{number of of triangles connected to }i}{\text{number of triples on }i},$$
(2.8)

where a triple on i means an unordered pair of nodes connected via i, and possibly connected directly. If that is the case, the triple is counted as a triangle, ending up in the nominator of Eq. 2.8 as well. Thus C_i expresses the degree of connectedness among the neighbors of i [75]. The (*global*) clustering coefficient of an undirected (N, E) network is then simply the average of the local coefficients:

$$C = \frac{1}{N} \sum_{i} C_i. \tag{2.9}$$

To assess whether an observed network possesses a non-random clustering structure and thus a significant clustering coefficient C_0 , we generate n random networks of the same size, i.e. the same number of nodes and edges, having clustering coefficients $C_{\text{rand}} = \{C_1, C_2, \dots, C_n\}$. Then we can calculate the z-score of the observed C_0 as

$$z = \frac{C_0 - \langle C_{\text{rand}} \rangle}{\text{sd}(C_{\text{rand}})}.$$
(2.10)

Large z indicates a significant value of C_0 , the sign indicating more (+) or less (-) clustering than a random network of the same size.

We have calculated clustering coefficients and z-scores for the undirected view of the loan maturity layers using yearly time windows which are displayed in Fig. 2.A.9. A clear pattern can be seen: the clustering varies from significantly high to moderate (in order $G_{<1d}$, G_{2-7d} , and G_{8-30d}), via moderately low to insignificant (in order G_{31-90d} , $G_{91-180d}$, and $G_{0.5-1y}$), to significantly low (G_{1-3y} and $G_{>3y}$). Since all layers exhibit heavy-tailed degree distributions, the sum in Eq. 2.9 is dominated by the (local) clustering coefficients of banks with small degree. We can use C to proxy the clustering of the periphery banks

Within that approximation, one sees that the core-periphery structure expected in the short maturity layers deviates considerably from the idealized star network, at least when looked at with yearly resolution. Notwithstanding the strong presence of intermediation found earlier, the lower-tier banks still trade extensively with each other, indicating that contagion risk is not located entirely in the hightier banks.

In contrast, the two longest maturity layers, where source-sink structures are expected, exhibit considerable star-like structure, low degree nodes and periphery banks being equivalent in most cases. In addition to the low clustering, we recall the modest anticorrelation between in- and outdegree; these observations lead us to believe that G_{1-3u} and $G_{>3u}$ behave as a sort of *source-sink star layers*. These layers have star-like hub structure, but hardly any intermediation occurs in the hubs. They act simply as sources and sinks, generating and dissipating excess liquidity in the interbank network. Of course, one could argue that for loans with maturities of at least one year, no intermediation is possible within the scope of one year. Looking at Fig. 2.A.5, which completely aggregates time, however, we see that the banks with the largest degrees tend to be either sinks or sources, especially in $G_{>3y}$. Thus the tendency of the hubs to be either sink or source, but not an intermediary, holds for time scales longer than one year. The next question is whether the star centers in the source-sink star layers are connected, or rather at the center of disconnected components. Disconnected components are plentiful compared to the number of active banks per year (see Fig. 2.A.8 and Table 2.A.1), and less than half of the latter participate in the largest (weakly) connected component, as Fig. 2.A.7 shows. Furthermore, we report that in the two source-sink star layers the average shortest path length is between 2 and 3 (see Fig. 2.A.6, which shows the average path length for G_{1-3y} and $G_{>3y}$ on a monthly basis as being typically 2), which, together with the proven existence of
hubs, indicates a compact star-like structure. In a nutshell, the source-sink star layers G_{1-3y} and $G_{>3y}$ are composed in general of many disconnected 'islands', of which the largest exhibit an almost perfect star-like structure around a sink or source hub.

All results are highly significant, except for $G_{91-180d}$ and $G_{0.5-1y}$: these layers do not possess any structural clustering structure on their own. As always, the clustering in the aggregated network resembles mainly the first two layers. We further note that clustering is most volatile in times of crisis, and increases during the growing phase of the network [24].



Global clustering coefficients of maturity layers and random networks of the same size.

Figure 2.A.9: Time series of clustering coefficients for the loan maturity layers and the aggregated network, together with a ribbon centered around $\langle C_{rand} \rangle$ of total width $2 \times sd(C_{rand})$. Following the methodology in [1], a total of 100 Erdős-Rényi networks were generated to test the significance of the observed C's.

2.A.7 Bank size mixing as degree size mixing

Many studies point to *disassortative mixing* with respect to the bank size, meaning that small banks trade mainly with large banks and vice versa. Given the coreperiphery picture in these studies, one expects that the core banks are the large banks. Indeed, it is found that total bank assets are significant in explaining core membership [28]. As bank size correlates with total degree, we would also expect disassortative mixing of the banks with respect to the (total) degrees, i.e. high (low) degree nodes tend to be connected to low (high) degree nodes [43]. In fact several studies report this as an additional stylized fact [1, 25].

Figure 2.A.10 shows the assortativity with respect to the total node degrees on yearly basis, which is also called the total degree correlation. The layers with short maturity show a clear preference for the low-degree nodes to attach to the high-degree ones. This preference weakens when we look at longer maturity layers. The assortativity or the long maturity layers is pushed up by the large number of disconnected clusters, in most cases simply isolated pairs of trading banks. The disassortative degree mixing in the larger clusters is present, caused by their star-like structure. As the number of unconnected components grows drastically, we would expect that the same mechanism is behind the high assortativity for $G_{91-180d}$ and especially for $G_{0.5-1y}$. Interestingly, this expectation turns out to be false: evaluating the degree assortativity only in the largest connected component results in lower values for all layers (notably in those where star-like structures were expected based on the clustering coefficient), but it remains strongly positive for $G_{91-180d}$ and $G_{0.5-1y}$ during the stable phase of the network (Fig. 2.A.11).



Figure 2.A.10: The degree assortativity measures to which extent nodes with a given degree associate preferentially with other nodes of similar degree – see Equation (2) in [76] for the formal definition. In this case the type of degree considered is the total degree, i.e. the sum of the in- and outdegree. A yearly resolution was chosen because monthly aggregation suffered from bad statistics starting from $G_{91-180d}$.



Yearly total degree assortativity of the largest connected component.

Figure 2.A.11: The degree assortativity for the total degrees throughout the years. The degree assortativity is also called degree correlation [43].

2.A.8 Summary

A summary of the results of this maturity layer analysis can be found in Table 1 in the main text. While certain features here are indicative of known structures in the interbank lending network literature, we refrain from making any such claims. Rather we report the findings here as is and only make claims about function and structure in the main text where steps have been taken to gather statistical evidence for both the construction of the layers as the occurrence of structure in such layers.

2.B OG inference with non-contiguous binning

Here we present the results of the OG inference where non-contiguous binning was allowed in Fig. 2.B.1 (as opposed to the contiguous binning in the main text). This allows for partitionings where short maturity loans are merged with very long maturity loans. One should keep in mind that the algorithm only makes a new bin in the OG when there is enough statistical evidence that it contains a different structure than the other bins. It is thus possible that in those cases where very long maturity loans are merged with short maturity loans, there is just hardly any actual structure (and thus not enough statistical evidence) in the long maturity layer. It then makes sense that such layer is merged with the densest layer available since this merger will cause the least amount of new connections to be introduced. This is corroborated by the fact that this kind of merging only happens in the early stages of market development and at the moment the trust crisis hit the interbank market in the summer of 2004 at the end of the data period.

Comparing Fig.3 in the main text to Fig. 2.B.1 shows the results to be qualitatively the same.

As mentioned in the main text, for comparability the partitionings are again always numbered according to the shortest maturity class in the bin.







2.C Number of active banks per group

Figure 2.C.1: The number of active banks per group is obtained by dividing the number of active banks by B, i.e. the number of groups in the inferred bank groups $\{b_i\}$.

2.D Activity characteristics per OGB

We investigate the OGBs and their typical characteristics. Fig. 2.D.1 shows the distribution of the log group strengths across time and per OGB. We discern three types of group strength: outstrength, instrength and internal strength. The group outstrength in a certain month of bank group b is the total amount lent by all banks belonging to b to banks belonging to another group $b' \neq b$. In symbols,

$$s_{b}^{\text{out}} = \sum_{l} \sum_{i,j,k} x_{ijk}^{l} \delta_{b_{i},b} (1 - \delta_{b_{j},b})$$
(2.11)

The two other strength types and the constraint that the maturity layer l must be in a given OGB are obtained likewise from this definition.



Figure 2.D.1: The time-integrated cumulative density functions (CDFs) of the group instrengths, outstrengths and internal strengths for each OGB. Zero group strengths are represented by non-vanishing CDFs at the origin.

We see that the groups show anti-community characteristics, they hardly lend or borrow internally. Looking at the group strengths, each OGB also seems to function on its own magnitude scale.

2.E Other percentiles for instrength/strength of important banks

We look at the lending behaviour of individual banks. As in the main text we again use the bank strength to single out the "important" banks. We show that the conclusions from the main text hold for different bank strength cutoffs. Each row of subplots in Fig. 2.E.1 uses a different cutoff, respectively with the bank strength (s) not limited, limited to the top 10 percentiles, top 5 percentiles, and the top 1 percentile of bank strengths. At monthly time scales the important banks in "short" bins tend to both lend and borrow equal amounts of money, while the important banks in the "long" bins tend to either lend or borrow.





important if its strength lies in the top X percentiles, with X here differing and given per row of subplots. With growing OGB index, the important banks increasingly tend to either lend or borrow. Banks in OGB 1 and OGB 2 tend to balance lending and borrowing. This suggests that the economic function of the important banks in the various OGBs changes from financial intermediation (short maturity bins) to financing (long maturity bins) on a monthly time scale.

2.F Timeline of the announcement crisis

The trust crises consist of the announcement crisis in the second half of 2003 and the summer of 2004 crisis. This Appendix has been compiled from [66, 71, 77, 78].

Investigations of money laundering led the CBR to deprive Sodbusinessbank of its license in May 2004. The following mutual suspicion led to a drying up of liquidity on the interbank market in the summer of 2004. Roughly one year earlier, this investigation was announced, which caused a smaller trust crisis (i.e. the announcement crisis).

end of July 2003	Start of announcement crisis. Decline in reciprocal bank interactions.				
September 2003	The network starts to fall apart because of the distrust among banks.				
December 2003 - January 2004	Back to normal liquidity.				
March	Peak of interbank lending market recovery from early trust crisis. The bank lending reciprocity, however, does not regain pre-crisis levels.				
following weeks	Three stages of the summer of 2004 crisis.				
First stage: April	Volatility on the interbank market with even higher lending rates than later stages but without significant outflow of individual's deposits. Demand for liquid- ity was caused by policy changes and statements of the CBR; no perception of crisis by the banks them- selves, yet this financial instability undoubtedly im- pacted the crisis to come.				
Second stage: May	CBR deprives Sodbusinessbank of its license.				
May 19-21	Several conflicting statements from authorities about the deposit insurance for the clients of Sodbusiness- bank make the depositors increasingly uneasy.				
Third stage: June 3	Crisis now definitively developed beyond Sodbusi- nessbank alone. Banks start to introduce additional control measures; several suspend lending activities on the interbank market.				
June 11	CBR changes policy rates to accommodate the banks, officially for the low liquidity on the interbank short-term market.				
June 21-22	Peak of the crisis.				
July 13	Interbank market starts to stabilize.				
July 16	The 'crisis of confidence' is declared to be at an end.				

Investigations of money laundering led the CBR to deprive Sodbusinessbank of its license in May 2004. The following mutual suspicion led to a drying up of liquidity on the interbank market in the summer of 2004. Roughly one year earlier, this investigation was announced, which caused a smaller trust crisis (i.e. the announcement crisis). In May 2004, a crisis on the Russian interbank market was triggered. In particular, on May 13 the Central Bank of Russia recalled the license from Sodbiznesbank on accusations of money laundering and sponsorship of terrorism. It was the first bank to be closed on these grounds in Russia. This unexpected closure caused panic on the interbank market since banks suspected other banks would follow suit, but they had no reliable information on who these banks might be.

On May 16 the head of Federal Financial Monitoring Service, Viktor Zubkov, announced publicly that his agency suspected another ten banks of similar violations. Because this announcement was not accompanied by the actual list of suspected banks, it just fuelled the hysteria on the interbank market. Rumours about the identities of these ten banks started to spread rapidly. Soon several inconsistent blacklists were circulating in the banking community as bankers tried to guess which banks were officially suspected of money laundering. Anecdotal evidence suggests that banks were actively helping to spread the rumour by removing themselves from the list and adding competitors in an attempt to escape the carnage. By consequence, The union of all the blacklists circulating in the banking community expanded in a few days to include dozens of banks, including several market leaders.

In the presence of total uncertainty about the quality of their counterparties, banks began to reduce limits on each other, which reverberated into an acute liquidity drought on the interbank market [79]. The turnover volume on the interbank market dropped spectacularly. Later the original source of the panic, Viktor Zubkov, shockingly announced that "the Federal Financial Monitoring Service has no blacklist". The deputy Minister of Internal Affairs similarly announced that "the Interior Ministry has no such list. We have no plans to persecute any banks."For further descriptions (in Russian) of this episode in Russian history see [80, 81]. Up till now it remains unclear whether an official list actually existed. Important for us is that the 2004 meltdown on the Russian interbank market was based on rumours and unrelated to shocks to the fundamentals of Russian banks or the Russian economy at large.

This non-fundamental and exogenous mutual trust crisis provides a great example of what structural changes occur during a shock to the non-fundamentals of the ILN. The advantage of the trust crisis compared to the 2007-2009 financial crisis is that, while the financial crisis was caused elsewhere and only indirectly found its way into Russia (via oil-prices, etc.), the trust crisis had its epicenter inside of Russia.

2.G Maturity classes in the ILN literature

An overview of the ILN literature using multilayer approaches and how their granularity compares to the current dataset.

	<1d	2-7d	8-30d	31-90d	91-180d	0.5-1y	1-3y	>3y
Central Bank of Russia [82]	instant	shor	t term		long	g term		
Bargigli et al. (2015) [1]	overnight	short term			long term			
Aldasoro and Alves (2016) [25]	short term long te				erm			
Montagna and Kok (2016) [16]	short term				long term			

Table 2.G.1: Classifications of loan maturity in terms of our maturity classes used by the Central Bank of Russia and several studies that have included multilayered ILNs.

2.H Term structure of interest rates and loan volumes in the interbank loan market



Figure 2.H.1: (top panel) The global categorical yield curve is the median interest rate over time per term. An alternative characterization is the interest rate per average ruble lent/borrowed, defined as the average interest weighed by the loan volumes. This statistic is robust to whether one excludes or includes the interest rate outliers. (lower panel) The average loan interest received/paid per term in millions of rubles and average loan volume (size) lent/borrowed in tens of millions of rubles.

The global categorical yield curve

The yield curve is obtained after "averaging" interest rates r over time and by maturity class. The averaging technique chosen is the median due to extreme outliers which disproportionately affect the mean: the standard deviation of the complete r population (including outliers) is $\sigma \approx 40\%$, yet 99% of the population is contained in $[0, \sigma]$. Within that interval the standard deviation is about 7%, which is a more sensible measure of the interest rate dispersion. By using the median, we avoid choosing any cutoff.

Yield curves are usually considered with *continuous* maturities ranging from one day to several years, but the available data only records maturity *classes*. Although methods exist to estimate the continuous yield curve from discrete data [83], we will only consider interest rates (and interests etc.) per category, i.e. per maturity class.

The solid line in the top panel of Figure 2.H.1 exhibits a typical stylized fact of the yield curve. It is upward sloping and has a convex shape, except for the >3y

maturity, i.e. maturities three years or longer. The unusual steepness of the curve in Figure 2.H.1 is an artifact caused by the term categories; as they progress, they bucket a growing amount of maturities, so a continuous yield curve would be horizontally stretched with respect to the categorical yield curve. The upward slope is usually explained by classical expectations theory (ET). According to ET, interbank lending rates dynamics are determined by the structure of liquidity supply and demand [84]; the long-term interest rate is an average of expected future shortterm rates, plus a term premium that increases with longer terms to compensate risk-averse lenders for the interest risk, which arises for lenders from fluctuating interest rates with respect to the base deposit policy rate. One can also extend ET by including separate premiums for liquidity risk (selling loans on the secondary market tends to be harder as their maturities lengthen) and default risk, also called counterparty risk, which is in theory governed by the credit rating of the borrower. Normally the short-end (long-end) of the yield curve is dominated by the liquidity (default) risk; both are considered components of interbank lending risk [55, 85]. Each risk contributes to the upward slope of the yield curve given normal market conditions.

The interest per average ruble is also displayed in the top panel of Figure 2.H.1. Loans with longer maturities are the most profitable for lenders. The drop for the >3y maturity could point to the fact that these contracts may be made on more amicable (flexible) terms; this would imply lower perceived interbank risk which could explain the negative slope between the 1-3y and >3y categories.

To illustrate the dynamics that underlie the global yield curve, Figure 2.H.2(a) plots the categorical yield curve for each of the last 16 months in the data. In this period the by now mature interbank network deals with the trust crises which are explained in more detail in Appendix 2.F. Figure 2.H.2(b) contains the (*yield*) *spread*, which we define as the difference in average yield between "long" maturities and "short" maturities. We define these maturities as two classes: the "long maturity" class consists of maturity classes (1-3y, >3y) and the "short maturity" class consists of maturity classes (<1d, 2-7d, 8-30d). The general shape of the curve is not sensitive to the definition of the "long maturity" class" is based on Basel recommendations and is also used in [1, 25].

In normal times, interbank markets are among the most liquid in the financial sector: banks prefer to lend out excess cash since the central bank's interest rate on excess reserves is smaller than rates available in interbank markets [86]. During trust crises, the perceived default risk grows, which inflates interest rates according to ET. Riskier banks, i.e. banks at risk of being in financial distress, exert an externality on safer banks who subsidize their liquidity [86]. If the crisis gets worse, this externality on safer banks is so costly that they leave the unsecured market, and liquidity rich banks may prefer to hoard liquidity instead of lending it



Figure 2.H.2: Monthly categorical yield curves (i.e. aggregated by maturity class; top panel) together with the spread (bottom panel) from July 2003 (month up until November 2004. This period is embedded in the emergent maturity phase of the network and includes the announcement and summer of 2004 crises (these are the trust crises – see Section 2.F), both shaded in grey on the bottom panel. The first shaded region spans the period from August 1st 2003 until January 1st 2004. The second shaded region spans the April 1st 2004 until July 16th 2004. The CBR lowered the overnight rate from 16 to 14% on January 15, 2004 and again to 13% on June 15, 2004. The yield curve is the median interest rate per maturity class, as in Figures 2.H.1; the spread is defined in the text.

out to an adverse selection of borrowers; the interbank lending market dries up.

We see that this mechanism is indeed captured by the spread curve in the bottom panel of Figure 2.H.2: low spread seems to indicate abnormal market conditions with low liquidity because the short term interest rates increase quite relatively fast. Note in the upper panel that the long term interest rates stay almost constant during the crises and drop slightly during the recovery in between (roughly from January until April 2004). This suggests that we cannot make an analogy with the typical *inverted yield curves* of e.g. treasury securities that are associated with (predicting) recessions. Indeed, according to ET these are yield curves with negative slopes because investors have poor expectations of future interest rates. In contrast, we see for our data that the short term interest rates rise quickly during the trust crisis while the long term rates hardly change.

Characteristics of loan volumes and interests

The lower panel of Figure 2.H.1 shows the average interest and volume per term. The loan volumes are log-normally distributed [24] and this holds remarkably well for the interest too, especially for shorter terms. Because of the considerable variance on a linear scale, these averages may be interpreted only as rough order of magnitude estimates. With this in mind, Figure 2.H.1 shows that interest rate and

volume are roughly negatively correlated: except for the bump at 0.5-1y and the case >3y, the volumes decrease as the interest rates increase. This can also be seen in the slowly varying average interest for the first five term categories.

Table 2.A.3 lists the total loan volumes by term and per year. As stated there (p. 49), we observe that the relative importance of each term segment, as measured by the total volume of loans traded within it, follows the ranking of the loan terms. This, together with the typical volumes and interest rates in Figure 2.H.1 and the lending activity in Table 2.A.2 (p. 49), supports the conclusion that the Russian interbank network exhibits a distinct hierarchy with respect to the loan maturities, which we could summarize by saying that *banks lend greater volumes at lower interest rates more often for shorter loan terms*.

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Part II

Belgian client data of a large European bank

3

The wealth origins of income mobility

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3.1 Schematic overview



Figure 3.1: Schematic overview of the workflow of the project on the wealth origins of income mobility.

3.2 Abstract

The social costs of wealth inequality and lack of income mobility have become a central focus of both public and academic debate. In this paper, we study the interaction between financial wealth and income growth using client-level data on career starters in Belgium, obtained from a large European bank. We find higher income performances for individuals with higher financial wealth at the start of their careers. This effect holds as early as three years into a career. While the roles of social capital and innate abilities appear limited, evidence is found for a transmission channel via job search conditions. Our results suggest that individuals with higher disposable wealth are more likely to find a job matching their human capital, in turn, boosting their chances of higher performance. Policies addressing an individual's capacity to accommodate frictions in the market for first jobs could therefore substantially promote economic mobility.

3.3 Introduction

The stagnation of income mobility combined with the increase of wealth inequality in recent times has become a central focus in both public and academic debate [1– 3]. Concerns over the related social costs, ranging from reduced health [4, 5] to lower economic growth [6–8], have triggered calls for dedicated policy action [1, 9]. However, designing adequate policies requires a careful understanding of the micro-mechanisms at play.

In modern economies, the start of a professional career stands as a major life event and offers unique opportunities to study how and when wealth inequality interacts with income mobility. Would an individual with more financial support achieve a greater income performance during the first years of her professional career? Would more financial support instead disengage an individual from income performance at early stages? Through which transmission channel and how early does the relationship materialize? We address these questions by studying the impact of financial wealth accumulated before the start of an individual's professional career on her income performances over a window of up to seven years after job market entry.

In general, countries with more inequality are also associated with less earning mobility across generations, as exhibited empirically by the so-called "Great Gatsby Curve" [10, 11]. Over the last decade, the increase of granular data has boosted research on the micro-mechanisms at play in *inter*-generational transfers and income mobility [12, 13]. Large drivers of *inter*-generational income mobility include parental income [14–17], parental health [18], geographical location in childhood [16, 19], access to and quality of education [20, 21] – which in turn also relates to parental income [16], and wealth transfers [22–26].



Figure 3.1: Economic equality in Belgium. A: The Gini coefficient of disposable income (post taxes and transfers) for 12 OECD countries for the mid-1980s and for 2016 or the latest available year. Belgian and the OECD average incomes are highlighted. Note that a Gini of 0(1) stands for complete (in)equality. B: The observed median income per municipality in the data for all clients (aged 18–60) in 2006. C: The observed median financial wealth per municipality in the data for all clients (aged 18–60) in 2006.

At the *intra*-generational level, upward income mobility is usually promoted by professional performances and career opportunities [27]. In essence, an individual's level of income is driven by a combination of human capital, financial wealth, and learning capabilities [28]. The contribution of each of these dimensions results from both innate abilities and socioeconomic variables (e.g., family, neighborhood, school, etc.) [12]. In particular, initial conditions at the moment of entry in the labor market can substantially impact lifetime earnings, wealth, and utility [28]. Such conditions include budget constraints (e.g., rate of depletion of financial wealth) and optimal allocation of human capital in the form of search and matching dynamics in the job market [29, 30]. However, little is known about the short-run materialization of the transmission channel between wealth inequality and income mobility. This paper seeks to fill this gap.

We study the effects of three transmission channels between financial wealth inequality and early career income performance: social capital, innate ability and job search conditions. We combine data from all financial transactions, financial wealth and demographic characteristics of several million Belgian clients of a large European bank between 2006 and 2016. As a result, we identify career starters as individuals exhibiting a transition to a wage income during the time window of the dataset. We then create an annual account of the financial progress of each career starter from a year before their start to seven years into their careers. In our setting, social capital is assessed via the demographic and geographic characteristics of an individual; innate abilities are reflected by an individual's own capacity to generate financial wealth before the start of her career; and job search conditions are captured by the economic pressures to secure a job.

First, we find consistently and significantly higher early career income perfor-

mances for individuals with higher financial wealth at the start of their careers. For example, the \in 5,500 difference in initial financial wealth between the 25th and the 75th percentiles produces a 4% difference in income growth three years into a career. This effect holds after controlling for demographic and geographical variables such as age, gender, and postal and neighborhood codes. Next, we address innate abilities by separating financial wealth into two sources: self-generated financial wealth (e.g., accumulated through student jobs) and transferred financial wealth (e.g., parental wealth transfers). We construct instruments to extract transferred financial wealth using the transactions data We construct instruments to isolate transferred financial wealth using the transactions data. Therefore, by focusing on this source of financial wealth, we exclude sources of wealth related to innate abilities. The results show that transferred financial wealth contributes to early career income performance with economic significance comparable to the original effects of financial wealth. Henceforth, the contribution of financial wealth originating from external transfers to early career income performance applies beyond the effects of social and innate advantages.

Finally, we address the interaction between job search conditions and human capital allocation in the market for first jobs. While timing and initial conditions are critical in job markets [28, 31], first-time jobseekers are particularly constrained by the length of the period they can sustain without income. We hypothesize that an individual entering the job market with more financial wealth possesses a higher capacity to sustain an extended absence of income, irrespective of the origin of her financial wealth. In turn, such an individual would be more likely to find a job matching her human capital, thus increasing her chances of stronger early career performances through higher productivity [32]. In order to test the job search condition hypothesis, we construct a measure of "thriftiness," that is, an individual's share of financial wealth that is not consumed before the start of a career. Intuitively, thriftiness generates higher savings and should therefore compensate for lower financial wealth transfers. We find that higher thriftiness is indeed consistently associated with higher early career income performances. While thrift and financial wealth are found to have comparable effects on income growth, they exhibit substituting effects on each other: benefits from financial wealth transfers before the start of a career are not boosted by higher individual thrift or vice versa.

In the absence of any compensating behavior such as thriftiness, less financially wealthy individuals face larger budget constraints when entering the job market for the first time. In turn, they exhibit lower income performances early in their career. Stronger pressure when entering the job market for the first-time may push jobseekers to accept job offers promptly at the cost of a low match thus reducing their expected income performances. In particular, this result offers evidence of adverse selection in the inequality distribution for early contracting [31].

Overall, our findings suggest that differential frictions in the hlsearch for first

jobs due to financial pressure may contribute to the perpetuation of economic inequality at least on par with other more classic factors such as social capital and innate abilities. Policies addressing this precise issue may be key to promoting income mobility.

While the data used in this paper covers a relatively small country with 11 million inhabitants, Belgium has consistently ranked as a top-tier country in terms of economic equality and mobility [8, 33]. Figure 3.1.A shows that Belgium's Gini index of income inequality is listed as one of the lowest among the OECD countries. Additionally, Belgians do not rely on debt to finance their graduate studies, in contrast with other countries like the US and the UK [34]. Most likely, student debt adds pressure on the budget constraints of a first-time jobseeker. All together, these considerations indicate that the results from this paper provide a lower bound for the effects of wealth transfers and savings behavior on income mobility and early career income performances. For illustrative purposes, Figure 3.1.B and Figure 3.1.C also show median income and financial wealth per municipality, respectively, for all work-eligible individuals in the dataset.

Data

We use anonymized data for the Belgian customers of a large European bank between 2006 and 2016. The full dataset contains more than 3 million clients (only retail individuals) and covers detailed information about personal characteristics, financial portfolio, and every monetary transaction (incoming and outgoing) from their accounts. All monetary variables are deflated to 2006 money values.

Each transaction contains a flag indicating whether it refers a point of sale in Belgium, a cash withdrawal, a payment via credit card, etc. From those codes (see Supplementary Information (S.I.) for an overview), we construct relevant variables in order to adopt flexible definitions of an individual's imputed income and consumption. Table 3.1 reports all the variables used in this study.

In addition to transactional information, we include data on personal characteristics covering date of birth, civil state, gender, postal code, neighborhood code and nationality. The neighborhood code is a statistical sector variable constructed by the Belgian statistical office (Statbel) and constitutes the most granular geographical subdivision for government data collection [35].

Finally, using complementary data on every client's financial assets held at the bank, we construct a measure of financial wealth aggregating saving deposits, checking deposits, trading account deposits, pension savings, and financial insurance.

Our analysis is exclusively concerned with active clients starting their career between 2006 and 2016 and remaining active through the full time window of the study data. In the following we provide a brief overview of the identification

Variable	Definition
Consumption (Yearly)	Debit card payments at P.O.S., cash withdrawals, written cheques, credit card payments, outgoing electronic transfers below a $\in 10,000$ single transaction value.
Income (Yearly)	Incoming electronic transfers below a given single transaction threshold during a year. If not stated otherwise, the cut-off value is $\in 5,000$.
Financial wealth (Yearly)	Saving deposits, checking deposits, term account deposits, trading account deposits, pension savings, and financial in- surances.
Married	Dummy variable equal to 1 if an individual is married.
Female	Dummy variable equal to 1 if the individual is female.
Belgian	Dummy variable equal to 1 if the individual is Belgian.
Start age	Age when individual started working (imputed as a categori- cal variable).
Start year	Year when individual started working (imputed as a categor- ical variable).
Region	Region where an individuals lives. There are 3 distinct re- gions in Belgium.
Postal code	Postal code where an individuals lives. There are almost 3,000 distinct postal codes in Belgium.
Neighborhood code	Neighborhood or statistical sector where an individuals lives. There are around 20,000 distinct statistical sectors in Bel- gium with on average 540 citizens per sector in 2008.

Table 3.1: Overview of all variables extracted from the data and their definition.

procedure (see S.I. for a detailed description).

Conditioning on the presence of regular client activity (i.e., no inactivity lasting longer than 3 months), we are left with 852, 331 individuals who are eligible to work for the full sample period. The next step is to identify career starters and homogenize their starting point. Our identification consists of a series of thresholds based on consumption surveys used for living standards statistics in Belgium [36]. Throughout the procedure, we adopt a conservative approach: cleaning decisions are driven by the need to avoid false positives at the potential cost of losing false negatives.

The following conditions distinguish between 'active and not working' and

'active and working' for an individual in year y. An individual *i* is 'active and not working' in year y if their $Consumption_{i,y} > \in 300$ and their $Income_{i,y}$ $< \in 6,000$. If their $Consumption_{i,y} > \in 2,400$ and $Income_{i,y} \ge \in 10,000$, they are categorised as 'active and working'.

The upper income bound for 'non-working years' ($\leq 6,000$) is meant to account for the student worker earning limits in Belgium. The lower income bound for 'working years' ($\leq 10,000$) is based on minimum wage statistics in Belgium. Further analyses of our main results with varying values of income bounds are provided in the S.I. and show no qualitative effects. Individuals with a yearly income between $\leq 6,000$ and $\leq 10,000$ are excluded from the sample. This condition excludes individuals who experienced discontinuous job experiences in their first year or started working late in the year. Using public statistics on first jobseeking individuals in Belgium, we assess that our sampling strategy covers the majority of the population (see S.I.). To control for outliers, we also trim those in the top 1% of starting wealth and the top 1% of income growth (other choices presented in S.I.).

Our framework identifies a career starter as a person for which there is exactly one persistent switch from 'active and not working' to 'active and working'. Their starting year is then the first calendar year in which they are categorized as 'active and not working'. To further reduce possible false positives, we focus on starting years between 2009 and 2014. Doing so ensures that at least three consecutive working and non-working years are observable. Since individuals have different starting years, we synchronize them on a working-years timeline. Finally, we restrict the starting age to a window between 18 and 30 years old. This window covers all the standard starting ages for individuals completing basic or higher education in Belgium.

Our final dataset consists of 17,576 career starters with an observed income performance coverage between three and seven years into their careers. While the reduction in size from the original dataset is significant, the final population sample contains a unique level of granularity and reliability to study the effects of financial wealth on income mobility in the first years of a career.

In order to capture those exposed to a common environment, we filter out isolated individuals by dropping locations for which we have too few datapoints: the threshold is set to more than or equal to 10 and 3 career starters in the same year for postal codes and neighborhoods to be included, respectively.

3.4 Results

We first assess whether the data show evidence of differential income mobility for individuals with higher financial wealth.

To this end, let $T_{\Delta t} \left(i \to j | q \right)$ be the share of the population starting in the q^{th}



Figure 3.2: Observed income mobility over three years for individuals starting in the highest quintile of financial wealth relative to those starting in the lowest financial wealth quintile, read from row to column. A: calculation based on the work-eligible sample. B: calculation based on the career-starter sample.

quintile of the financial wealth distribution at t_0 , moving from the i^{th} income quintile at t_1 , to the j^{th} income quintile over Δt years. Further let $\alpha_{q5,q1}$ be the ratio in this conditional transition probability between the highest (5^{th}) and lowest (1^{st}) financial wealth quintile, such that $\alpha_{q5,q1} = T_{\Delta t} (i \rightarrow j | q5) / T_{\Delta t} (i \rightarrow j | q1)$. Intuitively, this ratio indicates the comparative performance in income mobility between individuals with the highest and the lowest financial wealth. Note that financial wealth here is computed with a one-year lag. We motivate this choice below. Figure 3.2 reports values of $\alpha_{q5,q1}$ for all combinations of income quintile mobility for $\Delta t = 3$. Figure 3.2.A includes all work eligible individuals, whereas Figure 3.2.B is restricted to the population of career starters (synchronised on starting year t_1). The results indicate that over a relatively small timespan of three years, upward income mobility is dominated by individuals from the top financial wealth quintile (i.e., almost all right triangle cells are larger than one). Furthermore, the best possible income transition, $T_{\Delta t} (1 \rightarrow 5)$, is achieved by up to 2.3 times (1.75 times) more individuals from the top financial wealth quintile than individuals from the bottom financial wealth quintile for all work-eligible individuals (career starter-individuals). While the results for the career starters (Fig. 3.2.B) are less pronounced, they provide evidence at first glance of a positive relationship between financial wealth and early career income performance.

We report summary statistics on the sample of career starters in the S.I. Most career starters are Belgian, unwed, and around 22-23 years old in their first work-
ing calendar year. Gender is almost equally divided between males and females.

In the following, we unpack the relationship between financial wealth owned in the last non-working year (henceforth *start wealth*) and early career income performance. The reason we lag financial wealth by one year is driven by a specific Belgian rule, according to which first-time jobseekers (e.g., new graduates) have a legal waiting period of one year before being eligible for unemployment benefits. As such, a one-year lag ensures that the level of financial wealth we use is captured at the beginning of the waiting period or earlier. Our *start wealth* measure is therefore not affected by potential desaving or financial depletion during the waiting period.

Our first analysis quantifies the association of growth in income and *start wealth*. The baseline model is defined as follows:

$$\log(income_{i,t_{0+x}} + 1) = constant + \alpha_1 \log(income_{i,t_1} + 1) + \alpha_2 \log(start \ wealth_i + 1) \\ + \alpha_3 married_{i,t_{0+x}} + \alpha_4 female_i + \alpha_5 start \ age_i + \alpha_6 start \ year_i \\ + \alpha_7 location_{i,t_0} + \alpha_8 Belgian_{i,t_{0+x}} + \alpha_9 married_{i,t_{0+x}} : female \\ + \alpha_{10} \log(income_{i,t_1} + 1) : start \ age_i + \epsilon_i.$$

$$(3.1)$$

The parameter x is the year horizon, t_1 is the first working year, and t_0 the last non-working year. Note that *start age* and *start year* are not lagged and thus taken at time t_1 . The *location* variable controls for environmental factors, including location-based social capital and available amenities. It covers three different levels of geographical granularity: region, postal code, and neighborhood code. This ensures that the individuals were exposed to the same environmental influences. We note that while education and job occupation is not explicitly known, we control for *start age* and its interaction with starting income $(income_{i,t_1})$. This should largely capture the heterogeneity in education and the linked occupations within the sample. The model parameters are estimated using OLS methods with robust standard errors. The estimation for Eq. 3.1 is reported in Table 3.1. An extended version of the table, which explicitly shows the estimates for the control variables is presented in the S.I.

The results confirm that financial wealth in the last non-working year has a significantly positive effect on income performance during the first working years. More importantly, the granularity of the location controls has a limited effect on the main result. This indicates that social capital variables, as proxied by fixed effects for increasingly granular bins of living location, hold a restrained role in the transmission channel between financial wealth and early career income performance. In the case of Belgium, most social interactions take place at the neighbouring municipalities level [37]. Using location as a measure of social capital therefore allows to include both strong and weak social ties [38, 39]. All levels of

e included	controls ar	cates that the	√indi				
arentheses	errors in p	bust standard	(0.01 and rol)	(0.05; *** p<	*p<0.1; **p<		
0.080	0.140	0.161	0.102	0.148	0.150	0.190	.158

				Dep	endent varia	uble:	c		
	log(inco	me after 3	y + 1)	log(inco	me after 5y	+1)	log(incc	me after 7y	+ 1)
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
log(start income + 1)	0.225^{***}	0.230^{***}	0.061	0.097^{*}	0.067	-0.107	0.124^{*}	0.316^{**}	0.069
	(0.041)	(0.088)	(0.208)	(0.054)	(0.098)	(0.246)	(0.068)	(0.151)	(0.275)
log(start wealth + 1)	0.012^{***}	0.013^{***}	0.016^{***}	0.013^{***}	0.014^{***}	0.018^{***}	0.011^{***}	0.015^{***}	-0.004
	(0.001)	(0.002)	(0.004)	(0.001)	(0.003)	(0.005)	(0.002)	(0.003)	(0.009)
Constant	7.575^{***}	7.526^{***}	9.269^{***}	8.896***	9.085***	10.884^{***}	8.794^{***}	6.955^{***}	9.242^{***}
	(0.395)	(0.836)	(1.984)	(0.515)	(0.932)	(2.351)	(0.651)	(1.436)	(2.618)
Personal controls	٢	٢	م	م	م	م	٩	٢	٢
Region	م			م			م		
Postal code		<			ب			<	
Neighborhood code			<			٢			<
F Statistic	76.73***	6***	5.37***	57.34***	5.13^{***}	4.26^{***}	36.55^{***}	4.32***	7.91***
Observations	17,576	4,856	1,416	12,573	3,761	1,090	6,682	2,121	609
···?	0 150	0 158	n 105	0 150	0 1/8	0.102	0.161	0.146	0.086

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location precision except the seven-year horizon with neighborhood controls are consistent. The drop in this case comes from the fact that sample size per neighborhoods in the seven-year horizon becomes too small. For this reason we do not include neighborhood controls in the remainder of the paper.

Absent social capital as the main driver of the positive impact of financial wealth on income mobility, we study the effect of innate ability as our second hypothesis. In fact, a high level of *start wealth* might originate from hard work and other innate abilities which could, in turn, translate into faster-rising income in the early stages of a career. In order to address this concern of endogeneity, we construct instrumental variables using categorized transactional data in the non-working years. Using said variables allows to distinguish between transferred financial wealth and self-originated financial wealth. The former is an exogenous transfer from another account (e.g., from parents) whereas the latter captures the financial wealth earned by the individual herself (e.g., from student jobs).

The first dummy instrument indicates whether an individual is the recipient of a large amount on her trading account (*financial boost*). The second and third instruments indicate whether an individual is the recipient of a transfer on a savings and/or current account (*cash boost*). These instruments mainly differ in the magnitude of the transfer and do not require the money to remain present on the respective account until t_0 . Here, we set limits for the two *cash boosts* at respectively $\leq 5,000-10,000$, and above $\leq 10,000$; for the *financial boost*, the limit is set to $\leq 5,000$ or more. In the S.I., we report several other settings and show that the related results produce qualitatively similar outcomes. Finally, we also construct a merged dummy variable (*recipient*) which is equal to 1 if an individual has been subject to at least one of the above mentioned transfers in their non-working years.

We classify the population of career starters according to the *recipient* dummy variable and report the complete summary statistics of each resulting sample (recipients and non-recipients) in the S.I. Personal characteristics of the two samples do not vary by more than 3% in the median. Income after five years however, is larger by almost 6% for the *recipient* sample compared to the *non-recipient* sample.

The *IV* columns in Table 3.2 report the estimates of the model, where *start wealth* is instrumented with the three dummies, at different horizons and with different location controls. Instrumenting with these variables effectively excludes other sources of starting wealth including the ones related to innate abilities. The *Dummy* columns report the results where the *start wealth* parameter is replaced in the model by the merged *recipient* dummy variable. Directly using this dummy variable captures the effect of transferred financial wealth, independent of the amount of *start wealth* that was saved. Apart from column (8), all results from Table 3.2 maintain the sign and significance of the effect of *start wealth* from Table 3.1. The estimates for the control variables are presented in the S.I.

(columns 9–12) into a career using OLS regressions. The effect is estimated in two ways: first, in the **IV columns** by instrumenting start wealth with three dummies indicating the presence of different kinds of financial wealth transfers (± 65 financial boost, $\pm 5-10$ k cash boost, and ± 10 k cash Table 3.2: The effect of transferred financial wealth on income performance three years (columns 1–4), five years (columns 5–8), and seven years

levels of location controls. The estimates for the used control variables (Married, Female, Start age, Start year, Region, and Belgian) are given in the received ($+ \in 5k$) financial wealth transfer and replacing the start wealth parameter by it. The columns within each estimation model have different boost); secondly, in the Dummy columns by combining the aforementioned dummies into one Recipient dummy indicating at least one kind of

S.I.

$\log(\text{income after } 3y + 1)$ $\log(\text{income}$ IV IV $Dummy$ $Dummy$ IV IV .
IV IV Dummy Dummy IV IV
(1) (2) (3) (4) (5) (6)
log(start income + 1) 0.220*** 0.228*** 0.228*** 0.230*** 0.094* 0.063 (0.041) (0.088) (0.041) (0.087) (0.054) (0.098)
$ \begin{array}{llllllllllllllllllllllllllllllllllll$
(+5k) Recipient Dummy 0.037*** 0.037***
Constant 7.567*** 7.477*** 7.617*** 7.607*** 8.902*** 9.105***
(0.394) (0.843) (0.396) (0.827) (0.514) (0.931)
Personal controls 🗸 🗸 🗸 🗸 🗸
Region 🗸 🏑 🗸
Postal code 🗸 🧹 🗸
Observations 17,576 4,856 17,576 4,856 12,573 3,761
Adjusted R ² 0.156 0.153 0.155 0.152 0.150 0.147
Weak instruments 0 0 0 0
Wu-Hausman 0 0.06 0.3 0.65
Sargan 0.37 0.97 0.36 0.49
E Statistic 79 56*** 5 66***

 \checkmark indicates that the controls are included.

Furthermore, Table 3.2 shows a consistently larger effect of transferred financial wealth, thus suggesting the limited explanatory power of innate abilities for the observed relationship between *start wealth* and income mobility. This result holds over all time horizons considered. The typical instrumental variable regression test statistics finds no complications with the validity of these results. Moreover, the Wu-Hausman test, which tests for endogeneity and thus for the consistency of ordinary least squares, does not find sufficient evidence of endogeneity beyond the three-year horizon. Interestingly, the results suggest that recipients experience higher income performance irrespective of whether they save or spend their transferred financial wealth.

Table 3.1 and 3.2 highlight that social capital and innate abilities do not fully cover the mechanisms driving the positive relationship between financial wealth and early career income performances. We now turn to a third candidate mechanism: the effect of *start wealth* on improving the search conditions of first-time jobseekers. Recall that Table 3.2 has shown that financial wealth transfers positively correlate with income mobility irrespective of the consumption behavior. Such finding supports the claim that recipients of financial wealth transfers may be less economically pressured to rush into securing their first job. As a result, these individuals might find opportunities which would match better their human capital and aspirations, therefore increasing their chances of higher productivity and higher income growth [32].

In order to test the validity of this job search condition hypothesis further, we explicitly estimate the effects of savings behavior. We proceed by constructing a *thrift* variable for the population and adding it to the model. An individual's level of *thrift* is computed as the share of the total incoming and available financial wealth that is consumed in a given time frame. Let this measure be $Thrift \in [0, 1]$, with 0 representing no saving and 1 complete saving of income.

In principle, saving more extends the capacity of an individual to sustain themselves during periods without an income. Relaxing the budget constraints should provide a first-time jobseeker with less economic pressure. This alternative scenario should then also increase job matching quality in turn generating higher expected income performances for individuals exhibiting higher thrift [29, 30, 32]. By the same token, thrift should only have an effect on individuals whose external sources of financial wealth are limited. In the following, we test this hypothesis.

It is important to note that lower budget constraints do not need to translate into more time on the job market [40, 41]. In general, matchings in the optimal job market stopping problem is relative to both the sequence of job offers and the increased risk of running out of liquidity. Individuals with more financial wealth seeking a better match benefit from the lower costs of rejecting a job offer. Formally, we have the following definition:

$$thrift_{i,y} = \frac{financial \ wealth_{t_0}}{financial \ wealth_{t_0-y} + \sum_{x=1}^{y} (incoming \ financial \ wealth_{t_0-x})}$$
(3.2)

where

incoming financial wealth_t = financial wealth_{t+1} - financial wealth_t (3.3)

and y is either equal to two or three years as we only consider the years before the start of the waiting period. Limiting the analysis to this period avoids reverse causality with income. It also treats *thrift* as a personal characteristic resulting from personal and family endowment, in line with the literature [12, 42]. Complete summary statistics on *thrift* are reported in the S.I. In the median, recipients save almost half of their incoming financial wealth, while only the top quartile of nonrecipients match the same level of *thrift*. The combination of *thrift* and *recipient* can be used to re-assess the *start wealth* parameter in Table 3.1 according to two dimensions: one capturing the origin of *start wealth* (i.e., how much of the initial wealth results from transfers) and the other one capturing the savings behavior (i.e., how much of the wealth is saved or spent).

Table 3.3 shows the estimates for the model where wealth is replaced by the two- and three-year thrift variable and the recipient dummy variable. Table 3.3 also includes several horizons with different *location* controls. Note that only the 2y (two-year) thrift can be shown for the seven-year horizon due to the extra year required (see Eq. 3.2). Once again, the estimates for the used control variables are presented in an extended version of Table 3.3 in the S.I. The results confirm a significant positive effect of being the recipient of transferred financial wealth on early career income performance. Furthermore, the results show a comparable positive effect of thrift on early career income performance. This suggests that financial wealth frugality before the start of a career is associated with greater income performance. Importantly, the negative interaction term between *thrift* and recipient shows that the marginal effect of thrift diminishes when an individual is simultaneously recipient of transferred financial wealth. The benefits of thriftiness and financial wealth transfer thus tend to substitute each other: a lack of transferred financial wealth can be compensated by more thriftiness but the effects do not add up. This substitutability also confirms the importance of budget constraints: being subject to large financial wealth transfers may indicate access to financial resources (e.g., parents) to support any absence of income thus alleviating pressure on the job market independently of the way such transfers are consumed. Overall, the results confirm the positive relationship between financial wealth, job search conditions, and early career income mobility.

Table 3.3: The effect of transferred financial wealth and thrift on income performance three (columns 1–4), five years (columns 5–8), and seven years	(columns 9–10) into a career using OLS regressions. Thrift is measured over the last two (2y thrift) or over the last three non-working years	(3y thrift). The columns within each estimation model have different levels of location controls. The estimates for the used control variables	(Married Female Start age Start age Start age and Belgian) are given in the SI
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ven in the S.I. Ξ larriea, ren

	lo	g(income al	fter 3y + 1)		lc	g(income a	fiter $5y + 1$)		log(income a	(fter 7y + 1)
	Ξ	0	(3)	(4)	(2)	(9)		(8)	(6)	(10)
		Ì								(01)
log(start income+1)	0.219^{***}	0.286^{***}	0.217^{***}	0.361^{***}	0.160^{**}	0.165	0.189^{**}	0.211^{*}	0.101	0.381
	(0.049)	(0.105)	(0.058)	(0.125)	(0.063)	(0.121)	(0.078)	(0.123)	(0.114)	(0.233)
(151) Daviniant Dummu	0.045^{***}	0.044^{**}	0.041^{***}	0.041^{**}	0.051^{***}	0.045^{**}	0.051^{***}	0.028	0.048^{**}	0.097^{***}
(TUR) NCOLPIENT UNITED	(0.010)	(0.019)	(0.010)	(0.018)	(0.012)	(0.020)	(0.014)	(0.024)	(0.019)	(0.037)
2y thrift	0.051^{***}	0.073^{***}			0.066^{***}	0.082^{***}			0.063^{***}	0.100^{***}
	(0.008)	(0.016)			(0.011)	(0.019)			(0.016)	(0.032)
3y thrift			0.051^{***}	0.079^{***}			0.067^{***}	0.084^{***}		
			(0.010)	(0.020)			(0.014)	(0.028)		
(+5k) Recipient Dummy	-0.042^{**}	-0.054			-0.074^{***}	-0.096^{***}			-0.074^{**}	-0.153^{**}
:2y thrift	(0.018)	(0.033)			(0.019)	(0.028)			(0.034)	(0.069)
(+5k) Recipient Dummy			-0.038^{**}	-0.047^{*}			-0.064^{***}	-0.043		
:3y thrift			(0.018)	(0.028)			(0.023)	(0.035)		
Constant	7.703^{***}	7.081^{***}	7.737^{***}	6.323^{***}	8.389^{***}	8.253^{***}	8.139^{***}	7.778***	9.107^{***}	6.485^{***}
	(0.468)	(0.997)	(0.556)	(1.189)	(0.600)	(1.154)	(0.750)	(1.182)	(1.079)	(2.205)
Personal controls	>	>	>	>	>	>	>	>	>	>
Region	>		>		>		>		>	
Postal code		>		~		>		>		~
F Statistic	68.14^{***}	5.8^{***}	53.38^{***}	4.73^{***}	50.28^{***}	4.74^{***}	35.45^{***}	3.83^{***}	32.55^{***}	8.3^{***}
Observations	17,109	4,735	13, 382	3, 547	12, 103	3, 640	8, 383	2,458	6, 216	2,001
Adjusted R ²	0.155	0.155	0.153	0.144	0.145	0.141	0.140	0.132	0.162	0.147

WEALTH ORIGINS OF INCOME MOBILITY

3.5 Discussion

The major contribution of this paper is to show a substantial effect of wealth distribution on income mobility as early as three years into a career. We find a limited contribution of social capital and innate abilities to fully explain this effect. Finally, we find evidence that a channel of transmission exists when wealth inequality translates into differential economic conditions among first-time jobseekers.

Financial wealth, by extending an individual's capacity to remain without income, relaxes search frictions in the job market. More precisely, it alleviates the optimal stopping problem in labor markets resulting from the tradeoff between job opportunities and the uncertainty in the job search sequence [29]. Less economic pressure increases the expected quality of the achieved match with a job seeker's human capital. A better match, in turn, increases the likelihood of higher productivity and income performance in the early stages of a career [30, 32]. In contrast, less financially wealthy individuals face higher economic pressure and will tend to accept job offers at the cost of a low match, thus reducing their expected income mobility. This interplay provides a channel of transmission between intergenerational financial wealth transfers and income mobility at the earliest stage. Additionally, the interaction between financial wealth and job search conditions also offers evidence of adverse selection in the wealth inequality distribution for early contracting and market unraveling [31, 43]. Policies addressing these issues may be key to promoting income mobility.

Our analysis was limited to a seven-year time frame and had limited knowledge of parental affiliation, educational background and job occupation for each career starter. Future work featuring a longer time horizon, with explicit intergenerational mapping and a full knowledge of the career path is necessary to assess the scope of our findings and assess potential heterogeneous effects in education background and job occupation cross sections. Such results would help guide policy designs to support relevant segments of the population.

While testing the robustness of our results for other economies is paramount, the case of Belgium already provides interesting insights for three main reasons. First, Belgium ranks high in both equality and mobility worldwide (see Figure 3.1). Second, in contrast with several other developed economies, Belgium has a very low rate of consumer debt [34]. In particular, the Belgian educational system is mainly public and affordable (e.g., Belgium does not have a student debt system). Finally, according to Belgian law, an individual with no income record must wait for one year before being entitled to unemployment benefits, thus providing a suitable test-bed with a one-year lag between initial financial wealth and early career income performances. Overall, these remarks suggest that our results should provide lower bar estimates for the interaction between wealth inequality and income mobility. Countries such as the United States featuring higher wealth inequality and larger sources of budget pressure, including large tuition fees and student debts will likely exhibit more-pronounced effects.

Appendix

3.A Detailed cleaning procedure

Here we describe the procedure used to construct the variables and extract the subset in detail from the raw financial data.

For clarity the data is subdivided in two parts. One part contains every single financial transaction of all the clients, henceforth 'the transaction dataset'. The other part contains a yearly snapshot of the personal characteristics, henceforth 'the characteristics dataset'. The time frame of both datasets is from 2006 to 2016.

The characteristics dataset contains an individual start-of-year snapshot of personal as well as financial characteristics. The personal characteristics are: age, civil state, and location of domicile on the level of region, postal code, and neighbourhood code (government defined statistical sector). The financial characteristics are the balances of their savings, checking, term, and trading accounts, as well as their pension savings and any financial insurances they might have at the bank. These financial characteristics are aggregated into the variable *Financial wealth*.

In the transaction dataset, every transaction contains a flag to describe its type. Table 3.A.1 gives an overview of the utilized flags from the transaction dataset and how they were categorized. Because the characteristics dataset only provides a yearly start-of-year snapshot, we aggregate the transaction over one calendar year.

The total amount of clients included in these datasets is over three million (exact number redacted due to confidentiality). However, among these are also inactive clients, clients with only a savings account, etc. To exclude these individuals, we condition on the presence of a current account and on account activity in a three month rolling window over the complete time frame of the data. Since we are interested in career performances, we also limit the age between 15-50 in 2006 such that the subsample is work-eligible throughout the whole time frame. This active, work eligible subsample contains 852, 331 individuals and is used in Fig. 3.1.B, 3.1.C, and 3.2.A in the main text.

In light of the literature however, as explained in the main text, we further focus on career starters. Two conditions are used to categorize each person-year as 'active and working' or 'active and not working':

Transaction flag	Explanation
Consumption	The flags below sum to the consumption of an individual.
outgoing cash	Cash withdrawals.
outgoing cheque	Consumption cheques. Cheques commonly used for large purchases (e.g. houses) are excluded.
credit card purchase	
P.O.S. purchase	Purchases paid for at point of sale.
Trans. out -1k	Outgoing electronic transfer below $\in 1,000$ value.
Trans. out 1-2k	Outgoing electronic transfer between $\in 1,000$ and $\in 2,000$ value.
Trans. out 2-5k	Outgoing electronic transfer between $\in 2,000$ and $\in 5,000$ value.
Trans. out 5-10k	Outgoing electronic transfer between $\in 5,000$ and $\in 10,000$ value.
Trans. out +10k	Outgoing electronic transfer above $\in 10,000$ value.
Income	Depending on the definition used, (some of) the flags below make up the income of an individual. The 'Narrowplus' definition includes all flags below, the 'Narrow' definition excludes cheque and cash deposits, and the 'Supernarrow' definition further excludes Trans. in +10k. Note that none of the income definitions includes rents, interests, or divi- dends coming from financial wealth (neither in liquid form nor stocks or bonds).
Cash deposits	
Cheque deposit	
Trans. in -1k	Incoming electronic transfer below $\in 1,000$ value.
Trans. in 1-2k	Incoming electronic transfer between $\in 1,000$ and $\in 2,000$ value.
Trans. in 2-5k	Incoming electronic transfer between $\in 2,000$ and $\in 5,000$ value.
Trans. in 5-10k	Incoming electronic transfer between $\in 5,000$ and $\in 10,000$ value.
Trans. in +10k	Incoming electronic transfer above $\in 10,000$ value.

Table 3.A.1: Overview of all utilized flags extracted from the transaction dataset (indented), the category under which they fall (not indented), and extra explanation where the meaning of the flag is not self-explanatory.

Condition 1: Individual *i* active and Not Working in year y

 $Consumption_{i,y} > \in 300$ and $Income_{i,y} < \in 6,000$

Condition 2: Individual *i* active and Working in year *y*

 $Consumption_{i,y} > \in 2,400$ and $Income_{i,y} \ge \in 10,000$

The upper income bound for 'not working years' ($\leq 6,000$) is meant to account for the student worker earning limits in Belgium. The lower income bound for 'working years' ($\leq 10,000$) is loosely based on minimum wage in Belgium A career starter is then identified by having one persistent switch from 'not working' to 'working' within the time frame. The year in which this switch occurs is called the *Start year*. To have at least three consecutive 'working' and 'not working' years available, we only keep individuals with *Start year* between 2009-2014. Lastly, to limit false positives further, we restrict the age of individuals in their *Start year* between 18-30. This choice also excludes the underage career starters (-18). This is done because minors still have part-time compulsory attendance at school and need to comply with special requirements before they are allowed to start working. We are left with 17,576 career starters with an observed income performance coverage between three to seven years into their careers. This subset is used for the regressions and results in the main text.

3.B Summary statistics

Here we present summary statistics for our starters sample. Table 3.B.1 presents the summary statistics for the general career starter population. Table 3.B.2 shows the same summary statistics but now for the (+5k) recipients and non-recipient career starters separately. Lastly, Table 3.B.3 gives insights into the distribution of the *Thrift* parameter, as defined in Eq.2 in the main text.

	count	mean (€)	std (€)	min (€)	25p (€)	median (€)	75p (€)	max (€)
variable	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
	10 570	15 059 91	1 095 90	10,000,00	11 000 00	14 047 50	17 000 00	C0 700 05
Start income	12, 573	15,053.31	4,035.20	10,000.22	11,899.90	14, 347.53	17,208.00	03, 709.25
Income after 5y	12,573	23,407.27	7,335.20	10,000.01	18,746.72	22,070.37	26,588.98	80,557.07
Start wealth	12,573	4,584.54	7,135.48	0.00	302.26	1,670.50	5,801.79	52,637.47
Married	12,573	0.08	0.26	0.00	0.00	0.00	0.00	1.00
Female	12,573	0.48	0.50	0.00	0.00	0.00	1.00	1.00
Belgian	12,573	0.97	0.17	0.00	1.00	1.00	1.00	1.00
Start age	12,573	22.15	2.35	18.00	21.00	22.00	23.00	30.00
Start year	12,573	2010.42	1.10	2009	2009	2010	2011	2012
Consumption	12,573	12,952.35	5,849.63	2,402.16	9,455.14	12, 143.73	15,440.74	106, 833.38
Start inhabitants (neighborhood code)	12,573	1.42	0.74	1.00	1.00	1.00	2.00	6.00
Start inhabitants (postal code)	12,573	7.93	6.36	1.00	3.00	6.00	11.00	36.00

Table 3.B.1: Summary statistics for all career starters that have worked for five years within the dataset's time frame. Timing of the variables is as specified in the model (Eq.1 main text).

	count	mean (€)	std (€)	min (€)	25p (€)	$\text{median} \ (\textcircled{\in})$	75p (€)	max (€)
variable	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
(+5k) recipients								
Start income	1,571	15,589.04	4,829.58	10,001.60	12,001.14	14,781.93	17,896.22	61,040.13
Income after 5y	1,571	24,550.76	8,093.06	10,094.53	19,338.51	23, 166.11	28,259.18	67,366.46
Start wealth	1,571	13,180.25	12,059.68	0.00	3,173.45	10,090.58	19,511.21	52, 537.42
Married	1,571	0.09	0.29	0.00	0.00	0.00	0.00	1.00
Female	1,571	0.49	0.50	0.00	0.00	0.00	1.00	1.00
Belgian	1,571	0.98	0.14	0.00	1.00	1.00	1.00	1.00
Start age	12,573	22.54	2.36	18.00	21.00	22.00	24.00	30.00
Start year	1,571	2010.50	1.10	2009	2010	2010	2011	2012
Consumption	1,571	13,732.65	8,451.55	2,482.81	8,937.25	12,271.92	16,460.64	106, 833.38
Financial boost (+€5k)	1,571	0.35	0.48	0.00	0.00	0.00	1.00	1.00
Cash boost (€5-10k)	1,571	0.48	0.50	0.00	0.00	0.00	1.00	1.00
Cash boost (+€10k)	1,571	0.36	0.48	0.00	0.00	0.00	1.00	1.00
(+5k) non-recipients								
Start income	11,002	14,976.81	3,902.88	10,000.22	11,884.39	14,299.50	17,178.03	63,769.25
Income after 5y	11,002	23, 243.99	7,206.10	10,000.01	18,690.14	21,941.95	26,364.64	80,557.07
Start wealth	11,002	3,357.14	5,037.09	0.00	252.62	1,316.26	4,431.52	52,637.47
Married	11,002	0.07	0.26	0.00	0.00	0.00	0.00	1.00
Female	11,002	0.48	0.50	0.00	0.00	0.00	1.00	1.00
Belgian	11,002	0.97	0.17	0.00	1.00	1.00	1.00	1.00
Start age	11,002	22.16	2.34	18.00	21.00	22.00	23.00	30.00
Start year	11,002	2010.41	1.10	2009	2009	2010	2011	2012
Consumption	11,002	12,840.93	5,367.62	2,402.16	9,547.65	12, 134.02	15,333.21	97,545.70

Table 3.B.2: Summary statistics for two groups of career starters that have worked for 5 years within the dataset's time frame. **Top:** Summary statistics for career starters who received over €5,000 in transferred financial wealth before the start of their careers ((+5k) recipients). The correlation between financial boost (+€5,000) and the combined cash boost is -0.72 (-0.22 for +€10,000 and -0.41 for €5,000.€10,000). **Bottom:** Summary statistics for career starters who received less than €5,000 in transferred wealth before the start of their careers ((+5k) non-recipients)

	count	mean	std	min	25p	median	75p	max
variable	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
Full sample								
2y thrift	12,103	0.27	0.30	0.00	0.04	0.17	0.46	1
3y thrift	8,383	0.24	0.28	0.00	0.03	0.14	0.39	1
(+5k) recipio	ents							
2y thrift	1,524	0.48	0.44	0.00	0.14	0.50	0.73	1
3y thrift	1,116	0.45	0.44	0.00	0.12	0.44	0.67	1
(+5k) non-re	ecipients							
2y thrift	10,579	0.24	0.26	0.00	0.03	0.15	0.40	1
3y thrift	7,267	0.21	0.23	0.00	0.02	0.11	0.34	1

Table 3.B.3: Summary statistics for the thrift of career starters in the dataset that worked for five years. The top part of the table shows thrift values for the full sample while the bottom two parts show thrift values for those that got transferred at least \in 5,000 wealth at least once, and those that did not, respectively.

3.C Effects of income thresholds

As mentioned in the main text, the chosen thresholds in income (condition 1 and 2) cause some false negatives among the detected career starters. More specifically, if the timing of the start of an individual's career causes them to fall between $\in 6,000$ and $\in 10,000$ income in their first working year, they are dropped from the sample. Here we use publicly available data on recently graduated job seekers, collected by the public employment service of Flanders (VDAB) and made available via their online tool Arvastat [44]. We utilize this data to estimate the impact of the income thresholds on capturing career starters in the data.

Among the unemployed, we select only the BIT category. Individuals that have completed their education, before having the right to unemployment benefits, have to register for this BIT status. During periods of unemployment within the first 12 months after registration, the individual will remain in this category. After this 12 month period, the individual will have the right to unemployment benefits and will no longer appear in this category when unemployed. This 12 month period is the waiting period before being eligible for unemployment benefits which is referred to in the main text. When a person has worked the majority of a month, they automatically get unsubscribed from the BIT category in that month. A decline in BIT individuals thus means a net outflow of newly graduated unemployed. Monthly data on the amount of individuals with BIT status for the < 25 age category and per education level was extracted. Patterns did not differ significantly when including the 25 - 39 age category.

We calculate, for several levels of income, how many of the yearly starters are captured. Figures 3.C.1, 3.C.2, and 3.C.3 show such plots for a starting net income of $\in 1, 300, \in 1, 600$, and $\in 2, 100$ respectively. The three line per plot show the monthly amount of people per education level present in the BIT category. The shaded regions show the months in which starters are detected by our cut-offs and included in our sample. It can be seen that the majority of periods in which large declines of BIT membership occurs are captured. The plots show the following features:

- The periodicity is largely the same for all three levels of education.
- For the wages between $\in 1, 250-1, 500$ we capture the full wave of hiring.
- For wages between €1, 500-2, 000 we drop the people that started their career in September but you can see that there is a larger net outflow in the months from October to the end of May, which we do include.
- For the extremes of the distribution, namely those making less that €1,250 or more than €2,000, we do somewhat worse.

Since the VDAB reports that the median wages are: $\[mathbb{\in}1, 550\]$ for low-skilled (did not complete upper secondary education), $\[mathbb{\in}1, 635\]$ for medium-skilled (complete upper secondary education or did a trade year), and $\[mathbb{\in}1, 700\]$ for high-skilled (college or university) our selection criteria works well for a large majority of the people. Since these statistics only capture the net in-/out-flow of the BIT-category, it is hard to quantify the exact number of career starters we capture, however for a wage between $\[mathbb{\in}1, 500 - \[mathbb{e}2, 000\]$ we should capture 67% of the net outflow of job seekers when only taking into account the timing of outflow. Looking at national statistics, a rough estimation of yearly starters lies around $80, 000\]$ individuals per year (based on statistics of -30 year old individuals that leave school and find a job within a year). This means that, given our sample size, we capture at least three to five percent of the total yearly population of job starters in Belgium, depending on the horizon looked at.



medium-skilled (orange), and high-skilled (red) individuals present in the BIT category. The shaded area marks the months in which career starters, Figure 3.C.1: Impact of false negatives from income thresholds in selection procedure of career starters. The amount of low-skilled (blue),

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medium-skilled (orange), and high-skilled (red) individuals present in the BIT category. The shaded area marks the months in which career starters, Figure 3.C.3: Impact of false negatives from income thresholds in selection procedure of career starters. The amount of low-skilled (blue),

3.D Extended regression tables

Here we present the extended versions of the regression tables in the main text, which include explicit estimations of the most important control variables. To contain the length of the tables within page-limits, we present estimations for the *start year* and *start age* control variables in the next section (3.E).

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	lo	g(income after 3y + 1)		lo	g(income after 5y + 1)		lo	g(income after 7y + 1)	
	(1)	(2)	(3)	(4)	(5)	(9)	(L)	(8)	(6)
og(start income + 1)	0.225^{***}	0.230^{***}	0.061	0.097*	0.067	-0.107	0.124^{*}	0.316^{**}	0.069
	(0.041)	(0.088)	(0.208)	(0.054)	(0.098)	(0.246)	(0.068)	(0.151)	(0.275)
og(start wealth + 1)	0.012^{***}	0.013^{***}	0.016^{***}	0.013^{***}	0.014^{***}	0.018^{***}	0.011^{***}	0.015^{***}	-0.004
	(0.001)	(0.002)	(0.004)	(0.001)	(0.003)	(0.005)	(0.002)	(0.003)	(0.009)
Aarried	0.193^{***}	0.185^{***}	0.413^{***}	0.220^{***}	0.239^{***}	0.200^{***}	0.247^{***}	0.245^{***}	0.244^{***}
	(0.021)	(0.037)	(0.074)	(0.017)	(0.031)	(0.051)	(0.019)	(0.032)	(0.065)
emale	-0.077^{***}	-0.064^{***}	-0.043^{***}	-0.108^{***}	-0.086^{***}	-0.065^{***}	-0.136^{***}	-0.109^{***}	-0.075^{**}
	(0.004)	(0.008)	(0.016)	(0.005)	(0.010)	(0.021)	(0.008)	(0.014)	(0.035)
3elgian	0.044^{***}	0.026	-0.024	0.043 * * *	0.038	-0.008	0.023	0.026	0.018
	(0.013)	(0.020)	(0.051)	(0.016)	(0.025)	(0.049)	(0.023)	(0.037)	(0.087)
Aarried:Female	-0.140^{***}	-0.156^{***}	-0.382^{***}	-0.139^{***}	-0.181^{***}	-0.148^{**}	-0.202^{***}	-0.187^{***}	-0.308^{**}
	(0.026)	(0.043)	(0.088)	(0.021)	(0.039)	(0.075)	(0.025)	(0.044)	(0.094)
Constant	7.575^{***}	7.526^{***}	9.269^{***}	8.896***	9.085***	10.884^{***}	8.794^{***}	6.955^{***}	9.242^{***}
	(0.395)	(0.836)	(1.984)	(0.515)	(0.932)	(2.351)	(0.651)	(1.436)	(2.618)
tart age	>	>	>	>	>	>	>	>	>
tart year	>	>	>	>	>	>	>	>	>
tart income:Start age	>	>	>	>	>	>	>	>	>
tegion	>			>			>		
ostal code		>			>			>	
Veighborhood code			>			>			>
² Statistic	76.73***	6** 6	5.37^{***}	57.34^{***}	5.13^{***}	4.26^{***}	36.55***	4.32^{***}	7.91^{***}
Breusch-Pagan	0	0.003	0	0	0.033	0	0	0.079	0
Observations	17, 576	4,856	1, 416	12, 573	3, 761	1,090	6, 682	2, 121	609
²	0.161	0.187	0.435	0.153	0.183	0.377	0.166	0.199	0.400
Adjusted R ²	0.159	0.158	0.195	0.150	0.148	0.102	0.161	0.146	0.086
tesidual Std. Error	0.245	0.251	0.239	0.270	0.276	0.269	0.295	0.295	0.304
	(df = 17538)	(df = 4688)	(df = 994)	(df = 12537)	(df = 3605)	(df = 755)	(df = 6648)	(df = 1988)	(df = 399)

* p < 0.1; ** p < 0.05; *** p < 0.01 and robust standard errors in parentheses. \checkmark indicates that controls are included.



levels of location controls.	received (+ \in 5k) financial wealth transfer and replacing the start wealth parameter by it. The columns within each estimation model have different	boost); secondly, in the Dummy columns by combining the aforementioned dummies into one Recipient dummy indicating at least one kind of	three dummies indicating the presence of different kinds of financial wealth transfers (+ \in 5k financial boost, \in 5-10k cash boost, and + \in 10k cash	columns 9–12) into a career using OLS regressions. The effect is estimated in two ways: first, in the IV columns by instrumenting start wealth with	able 3.D.2: The effect of transferred financial wealth on income performance three years (columns 1–4), five years (columns 5–8), and seven year
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FStatistic	Residual Std. Error	Sargan	Wu-Hausman	Weak instruments	Adjusted R ²	R ²	Breusch-Pagan	Observations	Postal code	Region	Start income:Start age	Start year	Start age		Constant		Married:Female		Belgian		Female		Married	(marine a marine a marine (marine)	(±5k) Recinient Dummy		$\log(\text{start wealth} + 1)_{IV}$		log(start income + 1)			
(a) = 17330)	0.246	0.37	0	0	0.156	0.158	0	17,576		<	<	<	٢	(0.394)	7.567***	(0.026)	-0.137***	(0.013)	0.042 * * *	(0.004)	-0.079***	(0.021)	0.192***			(0.003)	0.020***	(0.041)	0.220***	(1)	IV	
(a) = 4000) (0.252	0.97	0.06	0	0.153	0.182	0.003	4,856	<		٩	٩	<	(0.843)	7.477***	(0.043)	-0.149^{***}	(0.021)	0.024	(0.008)	-0.066 ***	(0.037)	0.180***			(0.006)	0.024***	(0.088)	0.228 **	(2)	IV	log(income af
$a_J = 17330$ (73.56***	0.246				0.155	0.156	0	17,576		۲	۲	۲	<	(0.396)	7.617***	(0.026)	-0.145^{***}	(0.013)	0.045 * * *	(0.004)	-0.075***	(0.021)	0.195***	(0.006)	0 037***			(0.041)	0.228***	(3)	Dummy	ter 3y + 1)
aJ = 4000J (5.66***	0.252				0.152	0.181	0.001	4,856	<		۲	۲	<	(0.827)	7.607***	(0.043)	-0.164^{***}	(0.020)	0.026	(0.008)	-0.061***	(0.037)	0.188***	(0.012)	0 037***			(0.087)	0.230***	(4)	Dummy	
ay = 12007)	0.270	0.36	0.3	0	0.150	0.152	0	12,573		۲	۲	۲	<	(0.514)	8.902***	(0.021)	-0.138 ***	(0.016)	0.042 **	(0.005)	-0.109 ***	(0.017)	0.219 ***			(0.004)	0.017***	(0.054)	0.094*	(5)	IV	
(<i>aj</i> = 3003) (0.276	0.49	0.65	0	0.147	0.182	0.033	3,761	<		۲	۲	<	(0.931)	9.105***	(0.039)	-0.180^{***}	(0.025)	0.038	(0.010)	-0.087***	(0.031)	0.238***			(0.008)	0.017**	(0.098)	0.063	(6)	IV	log(income af
$a_j = 1200 i$) 54.43***	0.271				0.144	0.147	0	12, 573		۲	٩	٩	<	(0.520)	8.909***	(0.021)	-0.143^{***}	(0.016)	0.045^{***}	(0.005)	-0.105^{***}	(0.017)	0.221***	(0.008)	***650 0			(0.054)	0.105*	(7)	Dummy	ter 5y + 1)
$(a_J = 3003)$ 4.81***	0.278				0.141	0.176	0.021	3,761	<		۲	۲	۲	(0.938)	9.045^{***}	(0.039)	-0.186^{***}	(0.026)	0.039	(0.010)	-0.083***	(0.030)	0.243***	(0.016)	660.0			(0.099)	0.080	(8)	Dummy	
$a_{I} = 0048)$	0.295	0.13	0.94	0	0.161	0.166	0	6,682		۲	۲	۲	<	(0.651)	8.793***	(0.025)	-0.202^{***}	(0.023)	0.023	(0.008)	-0.136^{***}	(0.019)	0.247***			(0.006)	0.011*	(0.068)	0.124*	(9)	IV	
al = 1900) (0.296	0.1	0.31	0	0.142	0.195	0.079	2, 121	<		۲	۲	۲	(1.407)	7.026***	(0.044)	-0.180^{***}	(0.037)	0.027	(0.014)	-0.111***	(0.033)	0.239^{***}			(0.011)	0.026**	(0.149)	0.301**	(10)	IV	log(income aft
$a_J = 0040$ (36***	0.295				0.158	0.162	0	6,682		۲	٩	٩	٢	(0.663)	8.772***	(0.025)	-0.207***	(0.023)	0.024	(0.008)	-0.134^{***}	(0.019)	0.251***	(0.011)	0 095**			(0.069)	0.133*	(11)	Dummy	ter 7y + 1)
<i>aj</i> = 1900) 4.27***	0.296				0.142	0.195	0.06	2, 121	<		۲	٩	<	(1.485)	6.875***	(0.044)	-0.195 ***	(0.037)	0.023	(0.014)	-0.105***	(0.032)	0.252***	(0.022)	0 050***			(0.156)	0.336**	(12)	Dummy	

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years (columns 9–10) into a career using OLS regressions. Thrift is measured over the last two (2y thrift) or over the last three non-working years Table 3.D.3: The effect of transferred financial wealth and thrift on income performance three (columns 1-4), five years (columns 5-8), and seven (3y thrift). The columns within each estimation model have different levels of location controls.

Methoms and 2^{+1} () Methom and 2^{+1} () 2^{+1} () 2^{+1}											
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		$2y \ thrift$	$\log(\text{income a} 2y \ t h \ rift$	(free $3y + 1$) $3y \ thrift$	3y thrift	$2y\ thrift$	$\log(\operatorname{income} z y thrift$	fter $5y + 1$) 3y thrift	$3y\ thrift$	log(income a 2y thrift	fter $7y + 1$) 2y thrift
		(1)	(2)	(3)	(4)	(5)	(9)	(2)	(8)	(6)	(10)
	log(start income+1)	0.219^{***}	0.286***	0.217^{***}	0.361^{***}	0.160^{**}	0.165	0.189^{**}	0.211^{*}	0.101	0.381
(c) blacking human (0.043 ⁺⁺) (0.041 ⁺⁺⁻) (0.041 ⁺⁺⁻) (0.041 ⁺⁺) (0.041 ⁺⁺) (0.041 ⁺⁺		(0.049)	(0.105)	(0.058)	(0.125)	(0.063)	(0.121)	(0.078)	(0.123)	(0.114)	(0.233)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	(+5k) Recipient Dummy	0.045^{***}	0.044^{**}	0.041^{***}	0.041^{**}	0.051^{***}	0.045^{**}	0.051^{***}	0.028	0.048^{**}	0.097^{***}
Split 0.003 ⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺		(0.010)	(0.019)	(0.010)	(0.018)	(0.012)	(0.020)	(0.014)	(0.024)	(0.019)	(0.037)
Mark (0.005) (0.016) (0.016) (0.013) (0.016)	2y thrift	0.051^{***}	0.073^{***}			0.066^{***}	0.082^{***}			0.063^{***}	0.100^{***}
Split 0.007 0.008 0.004 0.003 0.004 0.004 0.004 0.004 0.004 0.004 0.004 0.004 0.004 0.004 0.004 0.004 0.004 0.004 0.004 0.014 0.004 0.014 <t< td=""><td></td><td>(0.008)</td><td>(0.016)</td><td></td><td></td><td>(0.011)</td><td>(0.019)</td><td></td><td></td><td>(0.016)</td><td>(0.032)</td></t<>		(0.008)	(0.016)			(0.011)	(0.019)			(0.016)	(0.032)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	3y thrift			0.051^{***}	0.079***			0.067***	0.084^{***}		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$				(0.010)	(0.020)			(0.014)	(0.028)		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Married	0.199^{***}	0.186^{***}	0.181^{***}	0.116^{**}	0.221^{***}	0.241^{***}	0.198^{***}	0.212^{***}	0.246^{***}	0.245^{***}
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		(0.021)	(0.037)	(0.025)	(0.047)	(0.017)	(0.031)	(0.020)	(0.036)	(0.019)	(0.033)
Begin (0.044) (0.064) (0.064) (0.064) (0.064) (0.063) (0.012) (0.032) (0.012) (0.032) (0.012) (0.033) (0.012) (0.033) (0.012) (0.033) (0.012) (0.033) (0.012) <th< td=""><td>Female</td><td>-0.074^{***}</td><td>-0.061^{***}</td><td>-0.075 * * *</td><td>-0.063 * * *</td><td>-0.105^{***}</td><td>-0.083^{***}</td><td>-0.112^{***}</td><td>-0.090^{***}</td><td>-0.134^{***}</td><td>-0.107^{***}</td></th<>	Female	-0.074^{***}	-0.061^{***}	-0.075 * * *	-0.063 * * *	-0.105^{***}	-0.083^{***}	-0.112^{***}	-0.090^{***}	-0.134^{***}	-0.107^{***}
Begin 0.043^{***} 0.022 0.007^{**} 0.047^{***} 0.042 0.023 0.023 0.023 0.023 0.023 0.023 0.023 0.023 0.023 0.023 0.023 0.023 0.023 0.023 0.023 0.023 0.033 0.033 0.033 0.033 0.033 0.014^{**} 0.023 0.023 0.023 0.023 0.023 0.023 0.023 0.023 0.023 0.033 0.023 0.013 0.023 0		(0.004)	(0.008)	(0.004)	(0.00)	(0.005)	(0.010)	(0.006)	(0.012)	(0.008)	(0.015)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Belgian	0.043^{***}	0.022	0.030^{*}	0.017	0.042^{**}	0.037	0.047^{**}	0.042	0.022	0.022
(45) Recipicat Dumuy $:$ 2^{4} thif -0.042^{**} -0.054 -0.074^{**} -0.034 (0.034) (0.034) (0.034) (0.034) (0.034) (0.034) (0.034) (0.034) (0.035) (0.025)		(0.014)	(0.021)	(0.016)	(0.024)	(0.017)	(0.026)	(0.019)	(0.030)	(0.023)	(0.038)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	(4.5b) Daviniant Dumme (20 thild)	-0.042^{**}	-0.054			-0.074^{***}	-0.096^{***}			-0.074^{**}	-0.153^{**}
(45) Recipiat Dumny. 3) thift -0.047^* -0.047^* -0.047^* -0.047^* -0.047^* -0.043^* -0.038^* -0.043 (0.023) (0.033) (0.033) (0.033) (0.033) (0.033) (0.033) (0.033) (0.033) $(0.023)^*$ -0.128^{***} -0.124^{***} -0.124^{***} -0.124^{***} -0.123^{***} -0.123^{***} -0.123^{***} -0.123^{***} -0.123^{***} -0.203^* $(0.023)^*$	mun vz. tunnu unnut more (w.t.)	(0.018)	(0.033)			(0.019)	(0.028)			(0.034)	(0.069)
(0.018) (0.028) (0.023) (0.033) (0.033) (0.035) (0.035) (0.035) (0.035) (0.035) (0.035) (0.035) (0.035) (0.035) (0.035) (0.035) (0.025) (0.035) (0.025) <	(±5b) Daviniant Dummu -3v thrift			-0.038^{**}	-0.047*			-0.064^{***}	-0.043		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	mun (c. funnud maidraat (set)			(0.018)	(0.028)			(0.023)	(0.035)		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Married:Female	-0.147^{***}	-0.162^{***}	-0.124^{***}	-0.096*	-0.144^{***}	-0.189^{***}	-0.125^{***}	-0.174^{***}	-0.205 * * *	-0.200^{***}
Constant 7.703*** 7.081*** 7.73*** 6.323*** 8.389*** 8.139*** 7.778*** 9.107*** 6.323*** Constant (0.46s) (0.997) (0.566) (1.154) (0.750) (1.182) (1.079) (2.3) Start age \checkmark <		(0.026)	(0.043)	(0.030)	(0.053)	(0.021)	(0.039)	(0.026)	(0.048)	(0.025)	(0.045)
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	Constant	7.703^{***}	7.081^{***}	7.737^{***}	6.323^{***}	8.389***	8.253^{***}	8.139^{***}	7.778***	9.107^{***}	6.485^{***}
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		(0.468)	(0.997)	(0.556)	(1.189)	(0.600)	(1.154)	(0.750)	(1.182)	(1.079)	(2.205)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Start age	>	>	>	>	>	>	>	>	>	>
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Start year	>	>	>	>	>	>	>	>	>	>
Region \checkmark \sim \sim \sim <	Start income:Start age	>	>	>	>	>	>	>	>	>	>
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Region	>		>		>		>		>	
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	Postal code		`		>		>		`		`
$ \begin{array}{ccccc} \mbox{Breach-Pagm} & 0 & 0.001 & 0 & 0.038 & 0 & 0.026 & 0 & 0.015 & 0 & 0.016 \\ \mbox{Okervalues} & 17,109 & 4,735 & 13,382 & 3,547 & 12,103 & 3,640 & 8,383 & 2,458 & 6,216 & 2,016 & 0.157 & 0.155 & 0.181 & 0.148 & 0.178 & 0.144 & 0.181 & 0.167 & 0.157 \\ \mbox{Adjusted} R^2 & 0.155 & 0.153 & 0.143 & 0.141 & 0.141 & 0.162 & 0.158 \\ \mbox{Adjusted} R^2 & 0.247 & 0.255 & 0.275 & 0.275 & 0.281 & 0.296 & 0.162 \\ \mbox{Adjusted} R^2 & 0.246 & 0.322 & 0.247 & 0.255 & 0.279 & 0.279 & 0.2713 & 0.140 & 0.142 & 0.162 & 0.162 & 0.162 \\ \mbox{Adjusted} R^2 & 0.246 & 0.255 & 0.275 & 0.271 & 0.275 & 0.281 & 0.296 & 0.162 & 0$	F Statistic	68.14***	01.8**	53.38***	4.73^{***}	50.28^{***}	4.74^{***}	35.45***	3.83***	32.55***	8.3**
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Breusch-Pagan	0	0.001	0	0.038	0	0.026	0	0.015	0	0.077
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Observations	17, 109	4,735	13, 382	3, 547	12, 103	3,640	8, 383	2,458	6, 216	2,001
Adjusted \mathbb{R}^2 0.155 0.155 0.153 0.144 0.145 0.140 0.132 0.162 0.1 Residual Std Error 0.246 0.252 0.247 0.255 0.272 0.279 0.275 0.296 0.1 Residual Std Error (df = 17069) (df = 13343) (df = 13393) (df = 12065) (df = 8346) (df = 2318) (df = 6180) (df = 6180) (df = 6180) (df = 2000) (df = 6180) (df = 6180) </td <td>\mathbb{R}^2</td> <td>0.157</td> <td>0.185</td> <td>0.155</td> <td>0.181</td> <td>0.148</td> <td>0.178</td> <td>0.144</td> <td>0.181</td> <td>0.167</td> <td>0.204</td>	\mathbb{R}^2	0.157	0.185	0.155	0.181	0.148	0.178	0.144	0.181	0.167	0.204
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Adjusted R ²	0.155	0.155	0.153	0.144	0.145	0.141	0.140	0.132	0.162	0.147
(df = 17069) (df = 4565) (df = 13343) (df = 3393) (df = 12065) (df = 3482) (df = 2318) (df = 6180)	Residual Std. Error	0.246	0.252	0.247	0.255	0.272	0.279	0.275	0.281	0.296	0.295
		(df = 17069)	(df = 4565)	(df = 13343)	(df = 3393)	(df = 12065)	(df = 3482)	(df = 8346)	(df = 2318)	(df = 6180)	(df = 1866)

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3.E Sanity checks

For several of the personal characteristic controls, the results align well with known effects from literature, passing sanity checks. The negative coefficient for females and married females shows the documented gender gap in income growth [45, 46]. The positive coefficient for having a native nationality coincides with migration literature [47]. The start age proxies for attained education and shows rising income up till the age of 23-24. This is the age that someone who followed a model trajectory for a master's degree typically has in their first working year, as per the known college wage premium [48]. The region coefficients reflect the known higher youth unemployment in the Walloon region and lower youth unemployment in the Flemish region relative to the Brussels-Capital Region [49]. And lastly, the start year dummies confirm the negative effect of the financial crisis on the labour market [50, 51], which made it more difficult for starters to find a job [52–54], which in turn has a negative influence on labour market outcomes [55-57]. Examples of the coefficient estimates for the basic model (Eq.1 in main text) can be found in Table 3.E.1 and Table 3.E.2. The coefficients retain their sign and magnitude throughout the regressions, which can be provided on request.

		Dependent variable:	
	log(income after 3y + 1)	log(income after 5y + 1)	log(income after 7y + 1)
	(1)	(2)	(3)
log(start income + 1)	0.279***	0.241***	0.212***
	(0.009)	(0.011)	(0.016)
log(start wealth + 1)	0.012***	0.013^{***}	0.011^{***}
	(0.001)	(0.001)	(0.002)
Start age 18	0.010	0.035	0.038
	(0.030)	(0.033)	(0.051)
Start age 20	0.004	0.008	-0.014
	(0.011)	(0.013)	(0.020)
Start age 21	0.022**	0.007	-0.006
	(0.011)	(0.013)	(0.019)
Start age 22	0.050***	0.050***	0.034^{*}
	(0.010)	(0.013)	(0.018)
Start age 23	0.098***	0.095****	0.076***
	(0.010)	(0.013)	(0.018)
Start age 24	0.113***	0.110****	0.112***
	(0.010)	(0.013)	(0.018)
Start age 25	0.126***	0.102***	0.078***
	(0.011)	(0.013)	(0.020)
Start age 26	0.088***	0.081***	0.025
	(0.012)	(0.015)	(0.023)
Start age 27	0.073***	0.056^{***}	0.068**
	(0.014)	(0.019)	(0.028)
Start age 28	0.089***	0.077***	-0.024
	(0.017)	(0.022)	(0.030)
Start age 29	0.078***	0.047	-0.010
	(0.023)	(0.029)	(0.038)
Start age 30	0.087***	0.064^{**}	-0.057^{*}
	(0.025)	(0.026)	(0.034)
Start year 2010	0.006	0.021***	-0.005
	(0.006)	(0.007)	(0.007)
Start year 2011	0.016^{***}	0.018^{***}	
	(0.006)	(0.007)	
Start year 2012	0.013^{**}	0.011	
	(0.006)	(0.007)	
Start year 2013	0.024^{***}		
	(0.007)		
Start year 2014	0.019***		
	(0.007)		
Married	0.200***	0.225***	0.249***
	(0.021)	(0.017)	(0.019)
Female	-0.076^{***}	-0.106^{***}	-0.135^{***}
	(0.004)	(0.005)	(0.008)
Belgian	0.049***	0.048***	0.027
	(0.013)	(0.016)	(0.023)
Region Flanders	0.036^{***}	0.024^{**}	0.027^{*}
	(0.008)	(0.010)	(0.015)
Region Wallonia	0.002	-0.014	-0.019
	(0.008)	(0.010)	(0.014)
Married:Female	-0.151^{***}	-0.146^{***}	-0.203^{***}
	(0.026)	(0.021)	(0.025)
Constant	7.053***	7.516****	7.948***
	(0.083)	(0.105)	(0.151)
F Statistic	107 7***	80 56***	55 65***
Proueab Degen test (=1)	107.7	02.00	0.66
Observations	17 576	10 579	U 6 600
Deservations p ²	11,010	12, 073	0,082
A directed P ²	0.150	0.147	0.101
Aujusteu K Daaidual Std. Eman	0.104	0.071/36 10540	0.005(35 6660)
Residual Std. Error	0.240(af = 17550)	0.271(af = 12549)	0.295(af = 6660)

 $^{*}p{<}0.1;$ $^{**}p{<}0.05;$ $^{***}p{<}0.01\;$ and robust standard errors in parentheses.

Table 3.E.1: The effect of starting wealth on income performance three years (column 1),five years (column 2), and seven years (column 3) into a career using Ordinary LeastSquares (OLS) regressions. The columns within each horizon have different levels oflocation controls. For start year, 2009 is the reference year. For start age, 19 is thereference age. For region, Brussels is the reference region.

Note:

Note:		Residual Std. Error	Adjusted R ²	\mathbb{R}^2	Observations	Breusch-Pagan	F Statistic	Neighborhood code	Postal code	Start income:Start age	Start age		Constant		Married: Female		Region Wallonia		Region Flanders		Belgian		Female		Married		Start year 2014		Start year 2013		Start year 2012		Start year 2011		Start year 2010		log(start wealth + 1)		log(start income + 1)				
	(df = 17538)	0.245	0.159	0.161	17,576	0	76.73***			م	۲	(0.395)	7.575***	(0.026)	-0.140^{***}	(0.008)	0.001	(0.008)	0.035***	(0.013)	0.044^{***}	(0.004)	-0.077***	(0.021)	0.193^{***}	(0.007)	0.018^{***}	(0.007)	0.024^{***}	(0.006)	0.011^{*}	(0.006)	0.016^{***}	(0.006)	0.005	(0.001)	0.012^{***}	(0.041)	0.225^{***}	(1)	log(in		
)>d*	(df = 4688)	0.251	0.158	0.187	4,856	0.003	6***		۲	٩	۲	(0.836)	7.526***	(0.043)	-0.156^{***}					(0.020)	0.026	(0.008)	-0.064^{***}	(0.037)	0.185^{***}	(0.015)	0.018	(0.016)	0.032^{**}	(0.014)	0.011	(0.012)	0.031**	(0.012)	0.010	(0.002)	0.013^{***}	(0.088)	0.230^{***}	(2)	come after 3y +		
).1; **p<0.05; '	(df = 994)	0.239	0.195	0.435	1,416	0	5.37***	×		<	<	(1.984)	9.269***	(0.088)	-0.382^{***}					(0.051)	-0.024	(0.016)	-0.043^{***}	(0.074)	0.413^{***}	(0.061)	-0.023	(0.085)	0.125	(0.054)	0.004	(0.055)	0.095^{*}	(0.048)	-0.042	(0.004)	0.016^{***}	(0.208)	0.061	(3)	-1)		
p<0.01 and	(df = 12537)	0.270	0.150	0.153	12,573	0	57.34			۲	<	(0.515)	8.896***	(0.021)	-0.139^{***}	(0.010)	-0.015	(0.010)	0.023^{**}	(0.016)	0.043^{***}	(0.005)	-0.108^{***}	(0.017)	0.220 ***					(0.007)	0.010	(0.007)	0.018^{***}	(0.006)	0.019^{***}	(0.001)	0.013^{***}	(0.054)	0.097^{*}	(4)	log(ir	Dep	
robust standard	(df = 3605)	0.276	0.148	0.183	3,761	0.033	5.13***		٢	۲	<	(0.932)	9.085***	(0.039)	-0.181^{***}					(0.025)	0.038	(0.010)	-0.086^{***}	(0.031)	0.239 * * *					(0.015)	0.001	(0.015)	0.022	(0.014)	0.011	(0.003)	0.014^{***}	(0.098)	0.067	(5)	come after 5y +	endent variable.	
errors in paren	(df = 755)	0.269	0.102	0.377	1,090	0	4.26^{***}	<		۲	م	(2.351)	10.884^{***}	(0.075)	-0.148^{**}					(0.049)	-0.008	(0.021)	-0.065^{***}	(0.051)	0.200^{***}					(0.071)	-0.011	(0.071)	0.142^{**}	(0.057)	0.040	(0.005)	0.018^{***}	(0.246)	-0.107	(6)	- 1)		
theses. √indica	(df = 6648)	0.295	0.161	0.166	6,682	0	36.55***			۲	<	(0.651)	8.794***	(0.025)	-0.202^{***}	(0.014)	-0.019	(0.014)	0.027^{*}	(0.023)	0.023	(0.008)	-0.136^{***}	(0.019)	0.247 ***									(0.007)	-0.005	(0.002)	0.011^{***}	(0.068)	0.124^{*}	(7)	log(iı		
ates that control	(df = 1988)	0.295	0.146	0.199	2, 121	0.079	4.32***		٩	۲	<	(1.436)	6.955***	(0.044)	-0.187^{***}					(0.037)	0.026	(0.014)	-0.109^{***}	(0.032)	0.245^{***}									(0.016)	-0.005	(0.003)	0.015^{***}	(0.151)	0.316^{**}	(8)	ncome after 7y		
ls are included.	(df = 399)	0.304	0.086	0.400	609	0	7.91***	<		۲	۲	(2.618)	9.242***	(0.094)	-0.308***					(0.087)	0.018	(0.035)	-0.075^{**}	(0.065)	0.244^{***}									(0.086)	0.160^{*}	(0.009)	-0.004	(0.275)	0.069	(9)	+ 1)		

Table 3.E.2: The effect of starting wealth on income performance five years into a career with the income growth trim (columns 1–3), the separate income trim (columns 4–6), and no trim (columns 7–9) using Ordinary Least Squares (OLS) regressions. The columns within each trim have different levels of location controls.

3.F Robustness checks

Here we check the robustness of our results against some of the choices that were made in the main text. We check different income trimmings and income definitions. We always show the furthest horizon available. We find that our results hold throughout.

3.F.1 Trimming

Here we show that outliers in the data are not driving the observed effect. We compare the results of three different trimming schemes:

- Income growth trim (used in main text): here we jointly exclude the individuals in the top 1% of wealth and those in the top 1% of income growth after the specified horizon.
- Separate income trim: here we jointly exclude the individuals in the top 1% of wealth, the top 1% of start income, and the top 1% of income after the specified horizon.
- No trim.

The results can be found in Table 3.F.1-3.F.4. We always show the furthest horizon available (seven years). Where neighbourhood controls are used however, we show the five year horizon. We do this for the same reason as given in the main text, namely sample size.

		L	Dependent varic	uble: log(incom	e after 7y + 1)	
	Income gr	owth trim	Separate i	ncome trim		No trim
	(1)	(2)	(3)	(4)	(5)	(6)
log(start income + 1)	0.124^{*}	0.316^{**}	0.114^{*}	0.289^{*}	0.086	0.289^{*}
	(0.068)	(0.151)	(0.069)	(0.154)	(0.071)	(0.152)
log(start wealth + 1)	0.011^{***}	0.015^{***}	0.012^{***}	0.017***	0.013^{***}	0.016^{***}
	(0.002)	(0.003)	(0.002)	(0.004)	(0.002)	(0.004)
Married	0.247^{***}	0.245^{***}	0.232^{***}	0.238^{***}	0.260^{***}	0.281^{***}
	(0.019)	(0.032)	(0.019)	(0.032)	(0.020)	(0.034)
Female	-0.136^{***}	-0.109^{***}	-0.135^{***}	-0.108^{***}	-0.146^{***}	-0.112^{***}
	(0.008)	(0.014)	(0.008)	(0.014)	(0.008)	(0.014)
Belgian	0.023	0.026	0.026	0.016	0.003	0.012
	(0.023)	(0.037)	(0.023)	(0.038)	(0.027)	(0.042)
Married:Female	-0.202^{***}	-0.187^{***}	-0.185^{***}	-0.169^{***}	-0.218^{***}	-0.223^{***}
	(0.025)	(0.044)	(0.025)	(0.045)	(0.025)	(0.046)
Constant	8.794^{***}	6.955^{***}	8.887***	7.224^{***}	9.168^{***}	7.228***
	(0.651)	(1.436)	(0.655)	(1.464)	(0.683)	(1.447)
Start age	<	م	<	<	٩	٩
Start year	٩	م	٢	٩	<	م
Start income:Start age	٩	م	٢	<	م	م
Region	٢		<		٢	
Postal code		٩		<		<
F Statistic	36.55^{***}	4.32^{***}	30.67***	4.12^{***}	35.91^{***}	4.39^{***}
Breusch-Pagan	0	0.079	0	0.073	0	0.067
Observations	6,682	2, 121	6,622	2,105	6,816	2,197
R ²	0.166	0.199	0.139	0.185	0.161	0.200
Adjusted R ²	0.161	0.146	0.135	0.131	0.157	0.147
Residual Std. Error	0.295	0.295	0.295	0.297	0.307	0.308
	(0100 - JL)		111 1100	1 10101	1100	1 10 0011

Table 3.F.1: The effect of starting wealth on income performance seven years into a career with the income growth trim (columns 1–2), the separate income trim (columns 3–4), and no trim (columns 5–6) using Ordinary Least Squares (OLS) regressions. The columns within each trim have different levels of location controls.

Table 3.F.2: The effect of starting wealth on income performance five years into a career with the income growth trim (columns 1–3), the separate	income trim (columns 4–6), and no trim (columns 7–9) using Ordinary Least Squares (OLS) regressions. The columns within each trim have different	levels of location controls.
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	Inc	ome growth trin	u	sep	arate income trii	в		No trim	
	(1)	(2)	(3)	(4)	(5)	(9)	(1)	(8)	(6)
og(start income + 1)	0.097^{*}	0.067	-0.107	0.085	0.065	-0.067	0.080	0.056	-0.110
	(0.054)	(0.098)	(0.246)	(0.054)	(0.098)	(0.244)	(0.055)	(0.098)	(0.245)
og(start wealth + 1)	0.013^{***}	0.014^{***}	0.018^{***}	0.014^{***}	0.015^{***}	0.019^{***}	0.014^{***}	0.014^{***}	0.016^{***}
	(0.001)	(0.003)	(0.005)	(0.001)	(0.003)	(0.005)	(0.001)	(0.002)	(0.005)
Married	0.220^{***}	0.239^{***}	0.200^{***}	0.210^{***}	0.225^{***}	0.178^{***}	0.248^{***}	0.250^{***}	0.197^{***}
	(0.017)	(0.031)	(0.051)	(0.017)	(0.030)	(0.052)	(0.018)	(0.030)	(0.049)
Temale	-0.108^{***}	-0.086^{***}	-0.065^{***}	-0.107^{***}	-0.083^{***}	-0.066^{***}	-0.114^{***}	-0.089^{***}	-0.073^{***}
	(0.005)	(0.010)	(0.021)	(0.005)	(0.010)	(0.021)	(0.005)	(0.010)	(0.021)
3elgian	0.043^{***}	0.038	-0.008	0.044^{***}	0.046^{*}	-0.010	0.037^{**}	0.036	-0.009
	(0.016)	(0.025)	(0.049)	(0.016)	(0.025)	(0.052)	(0.018)	(0.026)	(0.050)
Married:Female	-0.139^{***}	-0.181^{***}	-0.148^{**}	-0.132^{***}	-0.165^{***}	-0.113	-0.162^{***}	-0.170^{***}	-0.141^{*}
	(0.021)	(0.039)	(0.075)	(0.021)	(0.039)	(0.077)	(0.022)	(0.041)	(0.073)
Constant	8.896^{***}	9.085^{***}	10.884^{***}	9.013^{***}	9.088^{***}	10.439^{***}	9.056^{***}	9.194^{***}	10.922^{***}
	(0.515)	(0.932)	(2.351)	(0.515)	(0.929)	(2.334)	(0.522)	(0.932)	(2.344)
start age	>	>	>	>	>	>	>	>	>
tart year	>	>	>	>	>	>	>	>	>
tart income: Start age	>	>	>	>	>	>	>	>	>
tegion	>			>			>		
ostal code		>			>			>	
Veighbourhood code			>			>			`
² Statistic	57.34^{***}	5.13^{***}	4.26^{***}	46.81^{***}	4.51^{***}	3.29^{***}	56.43^{***}	5.1^{***}	4.21^{***}
3reusch-Pagan	0	0.033	0	0	0.03	0	0	0.019	0
Observations	12, 573	3,761	1,090	12,467	3,635	1,060	12,828	3,871	1, 123
ζ ²	0.153	0.183	0.377	0.121	0.161	0.376	0.147	0.176	0.374
Adjusted R ²	0.150	0.148	0.102	0.119	0.123	0.097	0.145	0.141	0.098
Residual Std. Error	0.270	0.276	0.269	0.269	0.273	0.263	0.281	0.286	0.273
	(df = 12537)	(df = 3605)	(df = 755)	(df = 12431)	(df = 3480)	(df = 731)	(df = 12792)	(df = 3712)	(df = 778)

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columns within each estimation model have different levels of location controls.	Recipient dummy indicating at least one kind of received (\pm 5k) financial wealth transfer and replacing the start wealth parameter by it. T	inancial boost, \in 5-10k cash boost, and + \in 10k cash boost); secondly, in the Dummy columns by combining the aforementioned dummies into	in the IV columns by instrumenting start wealth with three dummies indicating the presence of different kinds of financial wealth transfers (+ ϵ	olumns 1–4), the separate income trim (columns 5–8), and no trim (columns 9–12) using OLS regressions. The effect is estimated in two ways:	Table 3.F.3: The effect of ($+ \in 5, 000$) transferred financial wealth on income performance seven years into a career with the income growth to
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1					Dependen	t variable: lo	g(income afte	r 7y + 1)				
		Income gr	owth trim			separate in	come trim			No t	rim	
	$_{IV}$	IV	Dummy	Dummy	IV	IV	Dummy	Dummy	IV	IV	$Dumm_{i}$	-
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	
log(start income + 1)	0.124^{*}	0.301^{**}	0.133^{*}	0.336^{**}	0.112	0.268*	0.124^{*}	0.310^{*}	0.086	0.273^{*}	0.096	
	(0.068)	(0.149)	(0.069)	(0.156)	(0.069)	(0.150)	(0.070)	(0.159)	(0.072)	(0.149)	(0.073)	
log(start wealth + 1)	0.011*	0.026^{**}			0.014^{**}	0.033^{***}			0.013^{**}	0.027***		
	(0.006)	(0.011)			(0.006)	(0.011)			(0.005)	(0.010)		
(+5k) Recipient			0.025^{**}	0.059^{***}			0.030^{***}	0.067^{***}			0.030^{**}	*
			(0.011)	(0.022)			(0.011)	(0.022)			(0.011)	
Married	0.247^{***}	0.239^{***}	0.251^{***}	0.252^{***}	0.231^{***}	0.228^{***}	0.236^{***}	0.246^{***}	0.260^{***}	0.276^{***}	0.264^{**}	*
	(0.019)	(0.033)	(0.019)	(0.032)	(0.019)	(0.033)	(0.019)	(0.032)	(0.020)	(0.035)	(0.020)	
Female	-0.136^{***}	-0.111^{***}	-0.134^{***}	-0.105^{***}	-0.135^{***}	-0.111^{***}	-0.133^{***}	-0.104^{***}	-0.146^{***}	-0.114^{***}	-0.144^{**}	*
	(0.008)	(0.014)	(0.008)	(0.014)	(0.008)	(0.015)	(0.008)	(0.014)	(0.008)	(0.015)	(0.008)	
Belgian	0.023	0.027	0.024	0.023	0.025	0.018	0.026	0.012	0.003	0.012	0.005	
	(0.023)	(0.037)	(0.023)	(0.037)	(0.023)	(0.038)	(0.023)	(0.038)	(0.027)	(0.042)	(0.027)	
Married:Female	-0.202^{***}	-0.180^{***}	-0.207^{***}	-0.195^{***}	-0.185^{***}	-0.159^{***}	-0.191^{***}	-0.179^{***}	-0.218^{***}	-0.219^{***}	-0.223^{***}	
	(0.025)	(0.044)	(0.025)	(0.044)	(0.025)	(0.045)	(0.025)	(0.044)	(0.025)	(0.047)	(0.025)	
Constant	8.793^{***}	7.026***	8.772***	6.875^{***}	8.894^{***}	7.323***	8.867***	7.143***	9.169^{***}	7.303***	9.156^{***}	
	(0.651)	(1.407)	(0.663)	(1.485)	(0.654)	(1.423)	(0.668)	(1.515)	(0.683)	(1.418)	(0.694)	
Start age	٢	٩	٢	<	<	<	<	۲	<	۲	۲	
Start year	۲	م	م	٢	<	<	٢	٢	٢	<	<	
Start income:Start age	٢	<	<	٢	<	<	<	<	<	<	<	
Region	٢		<		<		<		<		٢	
Postal code		۲		~		<		۲		<		
Observations	6,682	2,121	6,682	2, 121	6,622	2,105	6,622	2,105	6,816	2,197	6,816	
Breusch-Pagan	0	0.079	0	0.06	0	0.073	0	0.084	0	0.067	0	
\mathbb{R}^2	0.166	0.195	0.162	0.195	0.139	0.177	0.135	0.180	0.161	0.196	0.157	
Adjusted R ²	0.161	0.142	0.158	0.142	0.134	0.122	0.131	0.125	0.157	0.144	0.152	
Weak instruments	0	0			0	0			0	0		
Wu-Hausman	0.94	0.31			0.68	0.13			0.96	0.25		
Sargan	0.13	0.1			0.21	0.1			0.4	0.22		
	0.295	0.296	0.295	0.296	0.295	0.298	0.296	0.298	0.307	0.309	0.308	
Residual Std. Error	df = 6648	(df - 1088)	(df = 6648)	(df = 1988)	(H = 6588)	111 1070		(df = 1972)		(FOUG AL	(df = 6782)	\sim
Residual Std. Error ((0100 - (m)	(00 m - fn)	(e		(u) - 00007	(af = 1972)	(df = 6588)		df = 6782) (af = 2001		`

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Table 3.F.4: The effect of ($+ \in 5$, 000) transferred financial wealth and thrift on income performance seven years into a career with the income growth trim (columns 1-2), the separate income trim (columns 3-4), and no trim (columns 5-6) using OLS regressions. Thrift is measured over the last two (2y thrift) non-working years. The columns within each estimation model have different levels of location controls.	
--	--

Ι			перепает	variable: 10g(1	ncome after /y +	1)
	Income gr 2n thrift	owth trim 2 <i>n thri ft</i>	Separate ir 2 <i>n thri ft</i>	ncome trim 2n thrift	$2u\ thrift$	No trim 2 <i>u thri ft</i>
	(1)	(2)	(3)	(4)	- f - m - f - (2)	(9)
loo(start income + 1)	0.101	0.381	0.081	0.318	0.073	0.323
(1) amoant ame)Sat	(0.114)	(0.233)	(0.115)	(0.238)	(0.113)	(0.235)
(+5k) Recipient	0.048^{**}	0.097***	0.054^{***}	0.100^{***}	0.058***	0.100^{***}
•	(0.019)	(0.037)	(0.019)	(0.038)	(0.020)	(0.038)
2y thrift	0.063^{***}	0.100^{***}	0.065^{***}	0.104^{***}	0.074^{***}	0.109^{***}
	(0.016)	(0.032)	(0.017)	(0.033)	(0.017)	(0.033)
Married	0.246^{***}	0.245^{***}	0.231^{***}	0.240^{***}	0.260^{***}	0.282^{***}
	(0.019)	(0.033)	(0.020)	(0.033)	(0.020)	(0.035)
Female	-0.134^{***}	-0.107^{***}	-0.134^{***}	-0.106^{***}	-0.145^{***}	-0.111^{***}
	(0.008)	(0.015)	(0.008)	(0.015)	(0.008)	(0.015)
Belgian	0.022	0.022	0.024	0.012	0.001	0.006
	(0.023)	(0.038)	(0.023)	(0.038)	(0.028)	(0.043)
(+5k) Recipient :2y	-0.074^{**}	-0.153^{**}	-0.076^{**}	-0.139^{**}	-0.089^{***}	-0.155^{**}
thrift	(0.034)	(0.069)	(0.034)	(0.070)	(0.035)	(0.071)
Married:Female	-0.205^{***}	-0.200^{***}	-0.189^{***}	-0.180^{***}	-0.222^{***}	-0.236^{***}
	(0.025)	(0.045)	(0.025)	(0.045)	(0.026)	(0.047)
Constant	9.107^{***}	6.485^{***}	9.298^{***}	7.098^{***}	9.391^{***}	7.049^{***}
	(1.079)	(2.205)	(1.091)	(2.248)	(1.075)	(2.222)
Start age	>	>	>	>	>	>
Start year	>	>	>	>	>	>
Start income:Start age	>	>	>	>	>	>
Region	>		>		>	
Postal code		^		>		~
F Statistic	32.55^{***}	8.3^{***}	27.16^{***}	8.1^{***}	31.94^{***}	4.81^{***}
Breusch-Pagan	0	0.077	0	0.075	0	0.047
Observations	6, 216	2,001	6, 154	1,989	6, 343	2,072
\mathbb{R}^2	0.167	0.204	0.139	0.189	0.162	0.203
Adjusted R ²	0.162	0.147	0.134	0.130	0.157	0.147
Residual Std. Error	0.296	0.295	0.296	0.298	0.309	0.310
	(df - 6180)	l J t = 1866	(3L - 2L)	110 1014)	(2000 Jr)	$(T_{H} = 109.4)$

3.F.2 Income definition

Here we show robustness of the results against the income definition. We compare the results for three different income definitions:

- supernarrow income (used in main text) = electronic transfers from €2,000-5,000 + electronic transfers from €1,000-2,000 + electronic transfers from €0-1,000
- narrow income = electronic transfers from €5,000-10,000 + electronic transfers from €2,000-5,000 + electronic transfers from €1,000-2,000 + electronic transfers from €0-1,000
- narrowplus income = cash deposits + deposits via cheques + electronic transfers from €5,000-10,000 + electronic transfers from €2,000-5,000 + electronic transfers from €1,000-2,000 + electronic transfers from €0-1,000

Because of the influence between the income definition, the starters detection, and the *Recipient* dummy variable, we have to vary both the income definition and the *Recipient* threshold simultaneously.

For instance, in the main text, the Recipient dummy variable was based on dummy variables signifying exogenous wealth transfers of $\in 5,000$ or more ((+5k) *Recipient*). With the *supernarrow* definition, income contains electronic transfers up to $\in 5,000$. This way there is no overlap between what is labeled income, and what categorizes a person as being a Recipient. However, if then only the income definition is changed to narrow or narrowplus, which include up to $\in 10,000$ electronic transfers, a transfer of $\in 5,000$ before the start of a career is also counted towards income. This only leaves $\in 1,000$ till the individual gets excluded from the career starters due to reaching the $\in 6,000$ euro income limit under which they need to fall pre-career. It thus makes sense to only use exogenous wealth transfers of $\in 10,000$ or more to construct the *Recipient* dummy ((+10k) Recipient) when using the narrow or narrowplus income definition. This high requirement of receiving over €10,000 in financial support decreases the overall sample of recipients by more than half for the five year horizon. Even with this decrease in sample size, the basic results, shown in Table 3.F.5-3.F.7 are in line with those of the main text.

Table 3.E5: The effect of starting wealth on income performance seven years into a career for the Supernarrow (columns 1-2), Narrow (columns 3-4), and Narrowplus (columns 5-6) income definition using Ordinary Least Squares (OLS) regressions. The columns within each horizon have different levels of location controls.

log(start income + 1)	Supernarro	w income	Narrow	income	Narrow	volus income
log(start income + 1)					INGLIDA	
log(start income + 1)	(1)	(2)	(3)	(4)	(5)	(9)
;	0.124^{*}	0.316^{**}	0.109	0.282^{**}	0.076	0.296^{**}
	(0.068)	(0.151)	(0.067)	(0.137)	(0.072)	(0.145)
log(start wealth + 1)	0.011^{***}	0.015^{***}	0.012^{***}	0.020^{***}	0.014^{***}	0.025^{***}
	(0.002)	(0.003)	(0.002)	(0.004)	(0.002)	(0.004)
Married	0.247^{***}	0.245^{***}	0.256^{***}	0.277^{***}	0.277^{***}	0.292^{***}
	(0.019)	(0.032)	(0.020)	(0.032)	(0.022)	(0.041)
Female	-0.136^{***}	-0.109^{***}	-0.136^{***}	-0.116^{***}	-0.135^{***}	-0.102^{***}
	(0.008)	(0.014)	(0.008)	(0.015)	(0.009)	(0.018)
Belgian	0.023	0.026	0.007	-0.001	-0.015	-0.022
	(0.023)	(0.037)	(0.024)	(0.039)	(0.027)	(0.052)
Married:Female	-0.202^{***}	-0.187^{***}	-0.201^{***}	-0.221^{***}	-0.22^{***}	-0.232^{***}
	(0.025)	(0.044)	(0.026)	(0.046)	(0.029)	(0.055)
Constant	8.794^{***}	6.955^{***}	8.981***	7.335^{***}	9.363^{***}	7.200^{***}
	(0.651)	(1.436)	(0.639)	(1.313)	(0.688)	(1.387)
Start age	>	>	>	>	>	>
Start year	>	>	>	>	>	>
Start income: Start age	>	>	>	>	>	>
Region	>		>		>	
Postal code		>		>		>
F Statistic	36.55^{***}	4.32^{***}	34.19^{***}	4.67^{***}	27.79^{***}	4.06^{***}
Breusch-Pagan	0	0.079	0	0.06	0	0.479
Observations	6,682	2, 121	6,624	2,068	5,985	1,618
\mathbb{R}^2	0.166	0.199	0.153	0.207	0.143	0.202
Adjusted R ²	0.161	0.146	0.149	0.154	0.138	0.143
Residual Std. Error	0.295	0.295	0.316	0.317	0.322	0.325
(r	df = 6648)	(df = 1988)	(df = 6590)	(df = 1936)	(df = 5951)	(df = 1507)

log(start income + 1)	(1) (1)	(2) 0.067	e (3) -0.107	Dependent vari. (4) 0.061	Able: log(income Varrow income (5) 0.160	(6) -0.321	0.15	Nau 22**	Narrowplus incom) (8) 22** 0.107
log(start wealth + 1)	(0.054) 0.013^{***}	(0.098) 0.014^{***}	(0.246) 0.018^{***}	(0.053) 0.015^{***}	(0.098) 0.018^{***}	(0.28) 0.01	3**	7) (0.050) 3^{**} 0.014^{***}	$\begin{array}{llllllllllllllllllllllllllllllllllll$
((0.001)	(0.003)	(0.005)	(0.001)	(0.003)	(0.006)	0) (0.002)	(0.002) (0.003)
Married	0.220***	0.239***	0.200^{***}	0.225^{***}	0.252^{***}	0.19	2***	2*** 0.251***	2*** 0.251*** 0.250***
	(0.017)	(0.031)	(0.051)	(0.018)	(0.034)	(0.05)	52)	52) (0.020)	(0.020) (0.039)
Female	-0.108^{***}	-0.086^{***}	-0.065^{***}	-0.110^{***}	-0.088^{***}	-0.0	91***	$0.106^{***} -0.106^{***}$	991^{***} -0.106^{***} -0.088^{***}
	(0.005)	(0.010)	(0.021)	(0.005)	(0.010)	(0.	025)	(0.006) (0.006)	(0.006) (0.013)
Belgian	0.043^{***}	0.038	-0.008	0.035^{*}	0.026	ļ	0.050	0.050 0.055***	0.050 0.055*** 0.030
	(0.016)	(0.025)	(0.049)	(0.018)	(0.029)	_	0.060)	(0.060) (0.021)	$(0.060) \qquad (0.021) \qquad (0.035)$
Married:Female	-0.139^{***}	-0.181^{***}	-0.148^{**}	-0.155^{***}	-0.207^{***}	T	0.057	$0.057 - 0.186^{***}$	$0.057 -0.186^{***} -0.209^{***}$
	(0.021)	(0.039)	(0.075)	(0.023)	(0.044)	_	0.083)	(0.083) (0.026)	$(0.083) \qquad (0.026) \qquad (0.052)$
Constant	8.896***	9.085***	10.884^{***}	9.274^{***}	8.245***		13.396^{***}	13.396^{***} 8.705^{***}	13.396*** 8.705*** 8.753***
	(0.515)	(0.932)	(2.351)	(0.512)	(0.937)		(2.734)	(2.734) (0.477)	$(2.734) \qquad (0.477) \qquad (0.997)$
Start age	<	<	<	<	<		٩	د د	< < <
Start year	<	٢	٢	٩	م		م	د د	< < <
Start income:Start age	<	٢	<	٢	٢		۲	ح ح	۲ ۲ ۲
Region	<			٢				<	٢
Postal code		<			٢				۲
Neighbourhood code			<				<	<i>ح</i>	<
F Statistic	57.34^{***}	5.13***	4.26^{***}	50.32***	5.22***		4.19^{***}	4.19*** 39.25***	4.19*** 39.25*** 4.35***
Breusch-Pagan	0	0.033	0	0	0.002		0	0 0	0 0 0.003
Observations	12,573	3,761	1,090	12,320	3,579		970	970 11,146	970 11,146 2,738
\mathbb{R}^2	0.153	0.183	0.377	0.140	0.177		0.392	0.392 0.124	0.392 0.124 0.171
Adjusted R ²	0.150	0.148	0.102	0.138	0.141		0.109	0.109 0.121	0.109 0.121 0.130
Residual Std. Error	0.270	0.276	0.269	0.289	(2f - 3497)		0.289	0.289 0.299 0.299	0.289 0.299 0.305
		•	*p<0.1; **	p<0.05; ***p<0	.01 and standa	i i i i i i i i i i i i i i i i i i i	rd errors in pare	rd errors in parentheses. √indic	rd errors in parentheses.
Note:			*p<0.1; **	p<0.05; *** p<0	.01 and standar	d errors	in pare	in parentheses. ✓ indica	in parentheses. \checkmark indicates that control

Table 3.F.6: The effect of starting wealth on income performance five years into a career for the Supernarrow (columns 1–3), Narrow (columns 4–6), and Narrowplus (columns 7–9) income definition using Ordinary Least Squares (OLS) regressions. The columns within each horizon have different levels of location controls.

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1-4), Narrow (columns 5-8), and Narrowplus (columns 9-12) income definition using OLS regressions. The effect is estimated in two ways: first, in Table 3.F.7: The effect of $(+ \in 10, 000)$ transferred financial wealth on income performance seven years into a career for the Supernarrow (columns the IV columns by instrumenting start wealth with two dummies indicating the presence of different kinds of financial wealth transfers (+ \in 10k

indicating at least one kind of received (+ \in 10k) financial wealth transfer and replacing the start wealth parameter by it. The columns within each financial boost, and $+ \in 10k$ cash boost); secondly, in the **Dummy columns** by combining the aforementioned dummies into one Recipient dummy

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contr	11100
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of o	5
spore	322
-	5
oroni	2010
÷	3
h our	2
4	3
-	2
mode	2007
ation	110110
estim	111100

		Supernarrov	v income			Narrow	ncome			Narrowplu	is income	
	M	M	D^{ummy}	Dummy	M	M	Dummy	Dummy	M	II	Dummy	Dummy
	(1)	(2)	(3)	(4)	(5)	(9)	(1)	(8)	(6)	(10)	(11)	(12)
log(start income + 1) (0.219^{***}	0.226^{**}	0.228^{***}	0.232^{***}	0.136^{***}	0.178^{**}	0.143^{***}	0.168^{**}	0.176^{***}	0.235^{**}	0.176^{***}	0.223^{**}
))	0.041)	(0.089)	(0.042)	(0.087)	(0.041)	(0.079)	(0.040)	(0.077)	(0.042)	(0.096)	(0.042)	(0.094)
log(start wealth + 1) (0.022***	0.031^{***}			0.021^{***}	0.024^{**}			0.013^{***}	0.026^{**}		
))	0.004)	(0.008)			(0.005)	(0.010)			(0.005)	(0.011)		
(+10k) Recipient			0.048^{***}	0.058^{***}			0.048^{***}	0.047^{**}			0.032^{***}	0.059^{**}
			(0.008)	(0.017)			(0.00)	(0.021)			(0.011)	(0.027)
Married (0.192***	0.177^{***}	0.195^{***}	0.188^{***}	0.191^{***}	0.220^{***}	0.192^{***}	0.226^{***}	0.252^{***}	0.258^{***}	0.253^{***}	0.266^{***}
U)	0.021)	(0.037)	(0.021)	(0.037)	(0.023)	(0.045)	(0.023)	(0.045)	(0.028)	(0.055)	(0.028)	(0.055)
Female –(0.079***	-0.068^{***}	-0.075^{***}	-0.061^{***}	-0.086^{***}	-0.072^{***}	-0.082^{***}	-0.067^{***}	-0.081^{***}	-0.064^{***}	-0.079^{***}	-0.059^{***}
))	0.004)	(0.008)	(0.004)	(0.008)	(0.004)	(0.00)	(0.004)	(0.008)	(0.005)	(0.010)	(0.005)	(0.010)
Belgian (0.041^{***}	0.022	0.045^{***}	0.026	0.043^{***}	0.027	0.047^{***}	0.028	0.027	0.011	0.031^{*}	0.011
))	0.014	(0.021)	(0.013)	(0.020)	(0.015)	(0.025)	(0.015)	(0.025)	(0.018)	(0.031)	(0.018)	(0.031)
Married:Female –(0.136^{***}	-0.144^{***}	-0.145^{***}	-0.163^{***}	-0.118^{***}	-0.205^{***}	-0.124^{***}	-0.214^{***}	-0.146^{***}	-0.242^{***}	-0.151^{***}	-0.257^{***}
J)	0.026)	(0.043)	(0.026)	(0.043)	(0.028)	(0.051)	(0.028)	(0.051)	(0.034)	(0.064)	(0.034)	(0.064)
Constant	7.565***	7.442^{***}	7.621^{***}	7.586^{***}	8.387***	7.940^{***}	8.451^{***}	8.186^{***}	8.101^{***}	7.417^{***}	8.180^{***}	7.689***
))	0.394)	(0.851)	(0.397)	(0.833)	(0.389)	(0.761)	(0.387)	(0.735)	(0.404)	(0.926)	(0.401)	(0.893)
Start age	>	>	>	>	>	>	>	>	>	>	>	>
Start year	>	>	>	>	>	>	>	>	>	>	>	>
Start income: Start age	>	>	>	>	>	>	>	>	>	>	>	>
Region	>		>		>		>		>		>	
Postal code		`		`		>		`		`		`
Observations 1	7,576	4,856	17, 576	4,856	17, 138	4,582	17, 138	4,582	15,447	3,358	15,447	3,358
Breusch-Pagan	0	0.003	0	0.003	0	0	0	0	0	0.041	0	0.037
R ² (0.156	0.173	0.156	0.182	0.146	0.172	0.145	0.172	0.138	0.180	0.132	0.180
Adjusted R ² (0.154	0.143	0.154	0.153	0.144	0.141	0.143	0.142	0.136	0.145	0.130	0.145
Weak instruments	0	0			0	0			0	0		
Wu-Hausman	0	0.01			0.03	0.19			0.96	0.26		
Sargan	0.31	0.41			0.03	0.91			0.01	0.74		
Residual Std. Error (0.246	0.253	0.246	0.252	0.263	0.271	0.264	0.271	0.273	0.277	0.274	0.277
= dt	$= 17538)$ (ϵ	df = 4688) (df = 17538)	(df = 4688) (df = 17100) ((df = 4419)	df = 17100)	(df = 4419) (df = 15409)	(df = 3221) ((df = 15409)	(df = 3221)
F Statistic			73.29***	5.67***			66.02^{***}	5.37***			51.36^{***}	5.4^{***}

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	Residual Std. Error	Adjusted R ²	\mathbb{R}^2	Observations	Breusch-Pagan	F Statistic	Postal code	Region	Start income:Start age	Start year	Start age		Constant		Married: Female	:3y thrift	(+10k) Recipient	:2y thrift	(+10k) Recipient		Belgian		Female		Married	,	3v thrift	2y thrift		(+10k) Recipient		log(start income + 1)			1
df = 17069)	0.246	0.155	0.157	17, 109	0	68.07***		۲	۲	۲	٢	(0.470)	7.702***	(0.026)	-0.147^{***}			(0.024)	-0.037	(0.014)	0.043^{***}	(0.004)	-0.074^{***}	(0.021)	0.198^{***}		(0.007)	0.047***	(0.015)	0.055^{***}	(0.049)	0.219^{***}	(1)	2y thrift	
(df = 4565)	0.252	0.155	0.186	4,735	0.002	5.8***	<		۲	۲	<	(1.003)	7.082***	(0.043)	-0.161^{***}			(0.034)	-0.055	(0.021)	0.022	(0.008)	-0.061^{***}	(0.037)	0.186***		(0.01)	0.069***	(0.025)	0.067***	(0.105)	0.286***	(2)	Supernarro 2y thrift	
(df = 13343)	0.247	0.153	0.155	13, 382	0	53.37***		۲	۲	۲	م	(0.558)	7.746***	(0.030)	-0.124^{***}	(0.022)	-0.025			(0.016)	0.030^{*}	(0.004)	-0.075^{***}	(0.025)	0.181***	(0.009)	0.045***		(0.014)	0.051^{***}	(0.059)	0.216^{***}	(3)	w income 3y thrift	
(df = 3393)	0.255	0.145	0.182	3,547	0.053	4.77***	~		م	٩	م	(1.199)	6.351^{***}	(0.053)	-0.095^{*}	(0.030)	-0.058^{**}			(0.024)	0.018	(0.009)	-0.063^{***}	(0.046)	0.116**	(0.019)	0.074***		(0.024)	0.078***	(0.126)	0.358***	(4)	3y thrift	
(df = 16625)	0.264	0.144	0.146	16,665	0	61.79***		٩	٢	٩	٩	(0.463)	8.601***	(0.028)	-0.127***			(0.023)	-0.085^{***}	(0.015)	0.044^{***}	(0.004)	-0.081^{***}	(0.023)	0.197 ***		(0.008)	0.050***	(0.015)	0.079^{***}	(0.048)	0.127***	(5)	$2y \ thrift$	Depena
(df = 4308)	0.272	0.142	0.173	4,473	0	5.35***	~		۲	۲	م	(0.899)	8.231***	(0.051)	-0.213^{***}			(0.030)	-0.063^{**}	(0.025)	0.024	(0.009)	-0.067***	(0.045)	0.224^{***}		(0.010)	0.063***	(0.026)	0.062^{**}	(0.094)	0.164^{*}	(6)	Narrow 2y thrift	lent variable: lo
(df = 12899)	0.265	0.144	0.147	12,938	0	48.93***		٩	٢	٩	٩	(0.567)	8.752***	(0.033)	-0.098***	(0.027)	-0.057^{**}			(0.017)	0.041^{**}	(0.005)	-0.082^{***}	(0.026)	0.170***	(0.010)	0.051***		(0.017)	0.063^{***}	(0.059)	0.113^{*}	(7)	income 3y thrift	g(income after
(df = 3171)	0.274	0.126	0.165	3,319	0.022	4.14^{***}	~		٢	٢	٩	(1.194)	7.944***	(0.063)	-0.131^{**}	(0.033)	-0.047			(0.028)	0.033	(0.010)	-0.062^{***}	(0.055)	0.149***	(0.021)	0.085***		(0.029)	0.063^{**}	(0.125)	0.190	(8)	3y thrift	3y + 1)
(df = 14906)	0.274	0.133	0.136	14,946	0	48.92***		٩	٢	٢	٩	(0.461)	8.091***	(0.034)	-0.158^{***}			(0.020)	-0.107^{***}	(0.018)	0.027	(0.005)	-0.078^{***}	(0.028)	0.260^{***}		(600.0)	0.060***	(0.015)	0.074^{***}	(0.048)	0.185^{***}	(9)	2y thrift	
(df = 3114)	0.278	0.145	0.181	3,253	0.058	5.42^{***}	<		٩	٩	٩	(1.146)	7.991***	(0.065)	-0.261^{***}			(0.025)	-0.085^{***}	(0.032)	0.0005	(0.010)	-0.058^{***}	(0.055)	0.266^{***}		(0.020)	0.066***	(0.029)	0.080^{***}	(0.120)	0.194	(10)	Narrowph 2y thrift	
(df = 11557)	0.275	0.131	0.134	11,596	0	38.69***		٩	م	٩	٩	(0.594)	7.777***	(0.040)	-0.145^{***}	(0.035)	-0.088^{**}			(0.021)	0.030	(0.005)	-0.077^{***}	(0.032)	0.250***	(0.011)	0.062***		(0.022)	0.057^{***}	(0.062)	0.219^{***}	(11)	us income 3y thrift	
(df = 2203)	0.279	0.127	0.175	2,332	0.275	4.01***	<		۲	۲	<	(1.840)	7.602***	(0.075)	-0.176^{**}	(0.038)	-0.070^{*}			(0.037)	0.020	(0.012)	-0.053^{***}	(0.064)	0.180***	(0.026)	0 070***		(0.038)	0.077^{**}	(0.194)	0.228	(12)	3y thrift	

Table 3.F.8: The effect of $(+ \in 10, 000)$ transferred financial wealth and thrift on income performance three years into a career with the Supernarrow (columns 1–4), Narrow (columns 5–8), and Narrowplus (columns 9–12) income definition using OLS regressions. Thrift is measured over the last two (2y thrift) or over the last three non-working years (3y thrift). The columns within each estimation model have different levels of location controls.

	2y thrift	Supernarro 2y thrift	w income 3y thrift	3y thrift	2y thrift	Narrow 2y thrift	income 3y thrift	3y thrift	2y thrift	Narrowph 2y thrift	is income 3y thrift	3y thrij
	(1)	(2)	(3)	(4)	(5)	(6)	Э	(8)	(9)	(10)	(11)	(12)
t income + 1)	0.219***	0.286***	0.216***	0.358***	0.127***	0.164^{*}	0.113^{*}	0.190	0.185***	0.194	0.219***	0.228
	(0.049)	(0.105)	(0.059)	(0.126)	(0.048)	(0.094)	(0.059)	(0.125)	(0.048)	(0.120)	(0.062)	(0.194)
Recipient	(0.055***	0.067***	0.051***	0.078****	0.079***	0.062**	0.063***	0.063**	0.074****	0.080.	0.057***	0.077
	(0.015) 0.047***	0.025) 0.060***	(0.014)	(0.024)	0.015) 0.050***	0.026) 0.083***	(0.017)	(0.029)	0.010) (010)	0.029) 0.066***	(0.022)	(0.038)
	(0.007)	(0.015)			(0.008)	(0.016)			(0.009)	(0.020)		
			0.045^{***}	0.074***			0.051^{***}	0.065^{***}			0.065^{***}	0.079^{*}
			(0.009)	(0.019)			(0.010)	(0.021)			(0.011)	(0.026)
	0.198^{***}	0.186***	0.181^{***}	0.116^{**}	0.197 ** *	0.224^{***}	0.170***	0.149^{***}	0.260^{***}	0.266^{***}	0.250^{***}	0.180^{*}
	(0.021)	(0.037)	(0.025)	(0.046)	(0.023)	(0.045)	(0.026)	(0.055)	(0.028)	(0.055)	(0.032)	(0.064)
	-0.074^{***}	-0.061^{***}	-0.075^{***}	-0.063^{***}	-0.081^{***}	-0.067***	-0.082^{***}	-0.062^{***}	-0.078^{***}	-0.058^{***}	-0.077^{***}	-0.053°
	(0.004)	(0.008)	(0.004)	(0.009)	(0.004)	(0.009)	(0.005)	(0.010)	(0.005)	(0.010)	(0.005)	(0.012)
	(0.014)	(0.022	(0.016)	(0.026	(0.015)	(0.024	(0.017)	(0.028)	(0.018)	(0.039)	(0.021)	(0.020
Recipient	-0.037	-0.055			-0.085***	-0.063^{**}			-0.107^{***}	-0.085^{***}		
4	(0.024)	(0.034)			(0.023)	(0.030)			(0.020)	(0.025)		
Recipient			-0.025	-0.058^{**}			-0.057^{**}	-0.047			-0.088^{**}	-0.070°
ť			(0.022)	(0.030)			(0.027)	(0.033)			(0.035)	(0.038)
:Female	-0.147^{***}	-0.161^{***}	-0.124^{***}	-0.095^{*}	-0.127^{***}	-0.213^{***}	-0.098***	-0.131^{**}	-0.158^{***}	-0.261^{***}	-0.145^{***}	-0.176^{*}
-	(0.026) 7.702***	(0.043) 7.082***	(0.030) 7.746***	(0.053) 6.351***	(0.028) 8.601***	(0.051) 8.231***	(0.033) 8.752***	(0.063) 7.944***	(0.034) 8.091***	(0.065) 7.991***	(0.040) 7.777***	(0.075) 7.602*
	(0.470)	(1.003)	(0.558)	(1.199)	(0.463)	(0.899)	(0.567)	(1.194)	(0.461)	(1.146)	(0.594)	(1.840)
0	۰	<	۲	٩	<	<	<	<	۲	۲	۲	٩
ar	<	٢	<	۲	۲	<	۲	<	٩	م	٩	٩
come:Start age	<	۲	<	۲	۲	م	٩	م	م	<	٩	٩
	<		<		۲		٩		٩		٩	
ode		×		×		~		~		~		K
ic	68.07***	5.8***	53.37***	4.77***	61.79***	5.35***	48.93***	4.14^{***}	48.92^{***}	5.42^{***}	38.69^{***}	4.01***
-Pagan	0	0.002	0	0.053	0	0	0	0.022	0	0.058	0	0.275
tions	17,109	4,735	13, 382	3,547	16,665	4,473	12,938	3,319	14,946	3,253	11,596	2,332
	0.157	0.186	0.155	0.182	0.146	0.173	0.147	0.165	0.136	0.181	0.134	0.175
$d R^2$	0.155	0.155	0.153	0.145	0.144	0.142	0.144	0.126	0.133	0.145	0.131	0.127
l Std. Error	0.246	0.252	0.247	0.255	0.264	0.272	0.265	0.274	0.274	0.278	0.275	0.279
	(df = 17069)	(df = 4565)	(df = 13343)	(df = 3393)	(df = 16625)	(df = 4308)	(df = 12899)	(df = 3171)	(df = 14906)	(df = 3114)	(df = 11557)	(df = 220)

Note:

 $^*p{<}0.1; \\ *^*p{<}0.05; \\ *^{**}p{<}0.01 \ \text{ and robust standard errors in parentheses. } \checkmark indicates that controls are included.$

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CHAPTER 3

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4

Liquid wealth heterogeneity, asymmetric consumption dynamics, and myopic loss aversion

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4.1 Schematic overview



Figure 4.1: Schematic overview of the workflow of the project on liquid wealth heterogeneity and the asymmetry in consumption dynamics.

4.2 abstract

The consumption reactions to income changes of individuals is an important transmission channel of monetary and fiscal policies to the economy at large. For this reason, insights into such reactions are crucial for evaluating and designing efficient monetary and fiscal policies. Here, we add to the literature by using transaction-level bank account data on Belgian career starters to empirically study the effect of liquid wealth on consumption dynamics in the absence of both illiquid wealth and debt. We find an asymmetric consumption response to anticipated income changes, with a stronger response to income increases than to decreases. This asymmetry in consumption responses is shown to originate from the asymmetric consumption smoothing effect of liquid wealth. Traditional rational models of consumption are unable to fully explain the results. These results are consistent, however, with the predictions of the behavioural model of myopic loss aversion. Early in a career, individuals thus exhibit a combination of greater sensitivity to losses than to gains and a tendency to evaluate outcomes frequently. This hints that interventions such as those from Kenynesian fiscal policies are more effective in younger economies with lower levels of liquid wealth than in aging economies with high levels of liquid wealth.

4.3 Introduction

Understanding individuals' consumption responses to anticipated income increases and decreases ¹ plays an important role in designing and evaluating monetary and fiscal policies that influence income. Policies such as tax and labour market reforms or stabilisation, and income support policies, affect the economy at large through their effect on individuals' consumption. How will consumption evolve when a policy is expected to affect income? Will an income increase have the same effect on consumption as a decrease? Does this reaction differ throughout the wealth distribution? If so, what drives this? Answering these question precisely has been difficult due to limited empirical data.

Prior work has mostly relied on data from small, survey-based sources [1, 2] facing known issues such as measurement error and recollection bias [3]. Recently, detailed financial trace data, originating from the usage of financial services and products, has become available for research [4, 5]. One trend has been to use data from financial aggregator platforms (FAP) [6–8]. Although the nature of FAP data solves recollection biases and eliminates any potential motivations to misreport,

¹In this paper we focus on anticipated income changes. This has the advantage of not making any assumption about the income process, with income shocks and the error term being modelled jointly. In the remainder of the paper, when we refer to income increases or decreases, we always imply anticipated income decreases or increases.

concerns remain about selection bias and the salience effect of platform usage on financial behaviour [5]. Recent work by *Ganong and Noel* [9] has addressed these concerns by employing representative de-identified bank account data, which suffer less from selection bias in financial literacy ². To the best of our knowledge, such granular trace data have only been used to investigate consumption responses to one type of anticipated income change (increase or decrease) at a time. This paper seeks to fill the gap by investigating the consumption responses to both anticipated income increases and decreases in the presence or absence of liquid wealth.

Theories developed to explain consumption responses to income changes can be roughly divided into two categories: forward-looking, (near-)rational theories and behavioural theories. Rational theories that received much attention are the well-know Life Cycle/Permanent Income Hypothesis (LCH/PIH) [10, 11], and the models extending LCH/PIH with credit- and/or liquidity-constraints [12]. Widely used behavioural models are the myopic agent model [13, 14], and the loss-averse agent model [15, 16]. These various models entail different expected reaction patterns and can thus be tested in an empirical setting.

The LCH/PIH posit that people use savings to smooth fluctuations in income and that they shouldn't respond to anticipated income changes. It predicts no consumption response to anticipated income changes and has been rejected in all recent empirical research i.a. [6, 17–20]. Enriching the LCH/PIH with credit and liquidity constraints allows for the violation of LCH/PIH in the case of binding budget constraints. It states that credit-constrained individuals cannot (fully) borrow against expected future income increases and will thus only react once the increase materialises. Empirical research on anticipated income increases (e.g. tax rebates, temporary government shutdown) [8, 21, 22] has validated this predicted behaviour. In contrast, for anticipated income decreases, the liquidity- and creditconstrained agent model does not predict a reaction, since there is no reason why a liquidity-constrained individual should fail to save in anticipation of an income decrease.

Among the behavioural models, the myopic agent model does predict a consumption reaction to both expected income increases and decreases. It suggests that an agent has the tendency to evaluate outcomes frequently which leads to present-bias and thus to an individual's decision-making focusing around the now (e.g. reaction are based on the short-term). The model allows individuals to have different levels of present-bias or myopia towards consumption, leading to consumption reactions when the income change occurs. For anticipated income decreases, this provides a differentiating prediction between the credit- and liquidityconstrained agent model (no consumption reaction) and the myopic agent model

²Financially literate individuals will be more likely make use of FAP, whereas this is not the case for regular bank accounts.

(sudden consumption decrease). Using data on the phasing out of unemployment benefits, an expected income decrease, *Ganong and Noel* [9] found evidence of sudden consumption decrease after the last month of receiving benefits, in support of the myopic agent model. Myopia can thus explain the response to both anticipated income increases and decreases, in line with much of the previous mentioned findings.

Throughout the literature, a large range of estimated response values can be found [23]. The different data collection methods and circumstances make it hard to compare consumption reactions across studies. Because of this, several aggregate and survey studies [18, 24] have studied income increases and decreases in the same framework. These studies find an asymmetric consumption response, with higher reactions to income decreases than increases, something that myopia in itself is unable to explain. They have in turn proposed the (forward-looking but) loss-averse agent model as an explanation [16, 24]. Herein an individual cares much more about losses than about gains, relative to their reference point. This idea that individuals might tenaciously "hang on" to their former living standards was already noted in 1938 by *Stone and Stone* [25].

We conclude that the empirical work on the subject has led to a host of often contrasting theories. With most studies having some sort of data on credit constraints or liquidity, one consistent observation however has been that individuals with higher levels of liquidity have lower consumption reactions [2, 12]. This makes sense from a consumption smoothing perspective. Liquidity enables individuals to quickly react to income changes of any sorts. In light hereof, we home in on liquidity –in the form of liquid wealth– to investigate consumption reactions to anticipated income changes.

In modern economies, the start of a professional career stands as a major life event and offers unique opportunities to study how wealth inequality interacts with consumption dynamics. In Belgium, career starters hardly have any debt [26]³, hold most of their wealth as liquid wealth, and are all in the same phase of their life. This makes the population particularly well suited to tease out the consumption response heterogeneity to anticipated income changes in the presence, or absence, of liquid wealth. The homogeneity with regards to debt in this population reduces the limitations we face caused by not having data on the individual debt positions. We combine data from all financial transactions, financial wealth, and demographic characteristics of several million Belgian clients obtained from a large European bank between 2006 and 2016. In the data, we identify career starters as individual account of the financial progress of each career starter from a year before their

³Belgium has no tradition of student loans. Tuition fees are low and there are several options for lower income households to get financial support and/or reduced housing and tuition rates from the government.

start to six years into their careers. This data set has the same benefits as the bank data utilised by [9], namely that it eliminates recollection bias, introduces a high level of granularity, but doesn't suffer from the same selection bias as data from specialized financial service providers.⁴. Furthermore, because 6 years of data is available, we are able to eliminate time-fixed unobserved heterogeneity, such as education, risk aversion, innate ability, social capital, and many more, from the regressions.

We find that individuals without liquid wealth or debt exhibit a marginal propensity to consume, or MPC (= $\Delta Consumption/\Delta Income$), of (approximately) 1 to both anticipated income increases (MPC^+) and decreases (MPC^-) early in their career. This is in line with the predictions of myopia or present-bias. Further, in line with what has been consistently observed in literature, we find that higher levels of liquid wealth lead to lower consumption reactions. This indicates that having liquid wealth enables career starters to smooth their consumption in anticipation to income changes. The consumption smoothing is however not symmetric. Those with liquid wealth are found to smooth more for income decreases than for increases, as one would expect from loss-averse individuals. Combined, these findings lead to an average MPC^+ of 0.7, and MPC^- of 0.4.

Overall our results indicate that consumer dynamics early in a career are driven by a combination of both myopia and loss aversion. Myopia gives individuals the tendency to evaluate outcome frequently and become less forward-looking than the rational models suggest. This causes them to react to income changes when they materialise, even if they were anticipated. At the same time, the career starters seem to be loss-averse and resist reducing their consumption below their reference point. The same combination of behaviors –greater sensitivity to losses than to gains and a tendency to evaluate outcomes frequently– has also been observed when individuals are faced with investment choices $[27-29]^{5}$. Furthermore, our results are in line with the predictions of Kőszegi and Rabin's model of referencedependent preferences [30, 31] which formalizes a model with the same intuition as myopic loss aversion.

While the data used in this paper is limited to individuals early in their careers, the resulting finding of myopic loss aversion seems to be in line with much of the partial findings in the MPC-literature. This may indicate that our results extend beyond our sample of career starters. A better understanding of the mechanisms driving consumption decisions in the face of income changes may help us evaluate how the effectiveness of policy interventions is influenced by population characteristics and adapt accordingly. A young economy with a lower average level of liquid

⁴In Belgium, government benefits are, as a rule, paid on a bank account. Furthermore, Europeans have a right to a basic payment account. Because of this, it is a rare exception for a Belgian not to have a bank account. There is thus no financial literacy selection bias.

⁵Strong experimental evidence has been found for myopic loss aversion to explain the equity premium puzzle [28, 29].

wealth might, for instance, be better suited for Keynesian fiscal policy strategies than aging, high wealth economies.

The remainder of the paper is organised as follows. Section 4.4 discusses the data and empirical strategy, section 4.5 presents the results, and section 4.6 discusses the results.

4.4 Data and empirical strategy

We use de-identified data on more than three million clients of a European bank in Belgium. The data covers the period of 2006-2016 and included information on personal characteristics, individual incoming and outgoing monetary transactions, and financial portfolio compositions. We deflated all monetary values to 2006 values. The variables extracted from the data and their definitions are given in Table 3.1. For income, electronic transfers above $\leq 10,000$ and thus windfalls above this size are excluded. This ensures that the results are not driven by such outliers.

Variable	Definition
Consumption (Yearly)	Debit card payments at P.O.S., cash withdrawals, written cheques, credit card payments, outgoing electronic transfers below $\notin 10,000$ single transaction value.
Income (Yearly)	Cash deposits, consumer cheque deposits, and incoming electronic transfers below a single transaction threshold of $\notin 10,000$.
Liquid wealth (Yearly)	Saving deposits, checking deposits, trading account deposits, pension savings, and financial insurances.
Married	Dummy variable equal to 1 if an individual is married.
Female	Dummy variable equal to 1 if the individual is female.
Belgian	Dummy variable equal to 1 if the individual is Belgian.

Table 4.1: Overview of all variables extracted from the data and their definition.

We are interested and therefore extract the clients who remain active over the full time period and start their careers between 2006 and 2016. Below a brief overview of the identification procedure is given. A detailed description can be found in the Supplementary Information (S.I.) of Chapter 3, Appendix 3.A.

We identify 852, 331 individuals in the data that are work-eligible in the full sample period. We show the representativeness of the work-eligible sample in 4.A. Next, we identify career starters and homogenize their timelines to a consistent working years timeline. Our identification of career starters uses a series of thresholds that are based on cost of living statistics in Belgium [32]. From the need to avoid false positives, we consistently remain conservative in our cleaning decisions at the potential cost of losing false negatives.

We distinguish between a working and non-working year t for an active client i using the following conditions: an 'active and not working' individual i in year t has consumption $C_{i,t} > \in 300$ and income $Inc_{i,t} < \in 6,000$; an 'active and working' individual i in year t has $C_{i,t} > \in 2,400$ and $Inc_{i,t} \ge \in 10,000$. The upper income bound ($\in 6,000$) for not working is aimed to account for student worker earning limits in Belgium. The lower income bound ($\in 10,000$) to classify individuals as working is loosely based on minimum wage.

We identify a career starter as an individual having exactly one persistent switch from 'active and not working' to 'active and working'. The calendar year in which this switch occurs is then categorized as their starting year. To further reduce the chances of false positives, we only focus on individuals starting their careers between 2009 and 2011. Doing so ensures that we observe at least three consecutive not working years. It also ensures that our panel regressions can be run on a time series of six working years for all starters. Since individuals have different starting years, we synchronize them on a working-years timeline. Finally, we restrict the age of career start to be between 18 and 30 years old. Individuals completing the standard trajectory of basic or higher education in Belgium are included in this age interval. Summary statistics of the selected sample are reported in Table 3.B.1.

Our final dataset consists of 8, 940 career starters which we observe three years prior to starting their career up to and including their sixth working years. While the reduction in size from the original dataset is significant, the final population sample contains a unique level of granularity and reliability to study the effects of liquid wealth on consumption dynamics in the first years of a career. By focusing on this group, we try to minimize the effect of the observable debt-position, which through credit constraints could affect the consumption reaction.

To unpack the relationship between the consumption reaction to both positive (β_x^+) and negative (β_x^-) income changes, and liquid wealth, we use the following

variable	mean (1)	std (2)	$\min_{(3)}$	median	$\max_{(5)}$
	(-)	(-)	(0)	(.)	(0)
Start income	15,537.69	5,529.19	10,000.09	17,721.05	150, 393.89
Income after 6y	26,346.38	10,190.07	10,018.81	23,990.78	99,474.29
Start consumption	12,110.72	5,458.95	2,402.29	11,438.32	149,912.48
Consumption after 6y	23,526.05	10, 125.44	2,678.17	21,514.38	174,543.82
Start wealth	4,438.20	10,443.91	0.00	1,394.98	380, 239.32
Wealth after 6y	14,609.42	23,911.55	0.00	5,718.57	385, 841.21
Female	0.48	0.50	0	0	1
Married at start	0.01	0.09	0	0	1
Married after 6y	0.09	0.29	0	0	1
Belgian at start	0.97	0.16	0	1	1
Belgian after 6y	0.98	0.14	0	1	1
Start year	2009.98	0.81	2009	2010	2011
Start age	22.8	2.23	18	23	30

Table 4.2: Summary statistics for all career starters that have worked for 6 years within the data set time frame. The variables are always measured at the beginning of the calendar year.

estimation equation:

$$\Delta \mathbf{C}_{i,t} = \beta_1^+ |\Delta \mathrm{Inc}_{i,t}| + \beta_2^- |\Delta \mathrm{Inc}_{i,t}| + \beta_3^+ |\Delta \mathrm{Inc}_{i,t}| \times \log(1 + \mathbf{W}_{i,t-2}) + \beta_4^- |\Delta \mathrm{Inc}_{i,t}| \times \log(1 + \mathbf{W}_{i,t-2}) + \gamma \log(1 + \mathbf{W}_{i,t-2}) + \lambda \mathbf{X}_{i,t-1} + \eta_i + \epsilon_{i,t}$$
(4.1)

Herein, $\Delta C_{i,t} = C_{i,t} - C_{i,t-1}$, and $C_{i,t}$ is the total consumption during working year $t \in [2,6]$ of individual *i*. The distribution of $\Delta C_{i,t}$ over all starters is shown in Fig. 4.1. $|\Delta \text{Inc}_{i,t}| = |\text{Inc}_{i,t} - \text{Inc}_{i,t-1}|$, and $\text{Inc}_{i,t}$ is the total income during working year $t \in [2, 6]$ of individual *i*. The distribution of $\Delta \text{Inc}_{i,t}$ over all starters is shown in Fig. 4.2. β_1^+ and β_2^- thus give us the proportional consumption reaction to, respectively positive and negative, anticipated income changes ⁶. $W_{i,t-2}$ is the amount of liquid wealth individual i has at the start of calendar year t-2. Each individual's time series thus starts with the wealth one year before the start of their careers, and income and consumption in their first working year. γ indicates the effect level of liquid wealth has on consumption. β_3^+ and β_4^- give us the effect liquid wealth has on the consumption reaction to income changes (resp. positive and negative). We expect the signs to be negative, indicating a consumption smoothing effect. Lastly, $X_{i,t-1}$ includes a set of dummy variables for civil state (Married), gender interacted with civil state (Married:Female), calendar year (one dummy for each year), and nationality (non-Belgian). $X_{i,t-1}$ are always a snapshot of the state of the control variables at the start of calendar year t - 1. η_i

⁶We note that there is an implicit assumption of complete information in this model, where individuals can perfectly anticipate income changes. This assumption can be weakened by instrumenting the income change at time t with the change in time t - 1. Due to data access restrictions, we can currently not perform this instrumentation.

are person-fixed effects and $\epsilon_{i,t}$ are the errors, which are clustered at the individual level.

Next to using year-on-year differences in income, further endogeneity concerns between income and liquid wealth are addressed in three ways. Firstly, by explicitly excluding all types of rents and financial income from our income measure, we avoid wealth from generating income. Secondly, by lagging liquid wealth by a full year, we avoid changes in income to be included in liquid wealth. Lastly, by using person-fixed effects (η_i), we control for any individual time-constant unobserved heterogeneity such as education, innate abilities, risk aversion, and others that might depend on wealth.



Figure 4.1: Distribution of the year on year consumption changes for the full Belgian career starting sample over their first 6 working years. In blue the density plot is shown. In red the cumulative distribution function (cdf) is shown. The black vertical lines show the 5th, 25th, 50th, 75th, and 95th percentiles values of the cdf.



Figure 4.2: Distribution of the year on year income changes for the full Belgian career starting sample over their first 6 working years. In blue the density plot is shown. In red the cumulative distribution function (cdf) is shown. The black vertical lines show the 5th, 25th, 50th, 75th, and 95th percentiles values of the cdf.

4.5 Results

We gradually extend the model towards the specification in Eq. 4.1 and show the results in Table 4.3. The first two columns of Table 4.3 provide insights into the overall average consumption response to anticipated income increases and decreases. We find a higher consumption response to anticipated income increases than to income decreases, respectively 0.7, and 0.4. Adding the level of liquid wealth (and the other controls) does not explain away this asymmetry but does show that liquid wealth decreases the year-on-year consumption changes.

To see how liquid wealth influences this asymmetric consumption response, we add interaction terms between liquid wealth and the income changes in the third column of Table 4.3. We find that career starters without liquid wealth - the poor hand-to-mouth individuals [12] - adjust their consumption entirely to a change in income, both for anticipated income increases and decreases. This is in line with the hypothesised reaction of the myopic or present-bias agent model [13, 14]. An agent who is focused on the short term, will only react once the change has materialized. These observations firmly reject the mentioned rational, forward-looking agent models for career starters. For the LCH/PIH model, we reject the hypothesis of insensitivity to anticipated income changes. For the credit-constrained agent model we reject the hypothesis of exclusive sensitivity to anticipated income increases.

For the career starters with liquid wealth, we see that increasing levels of liquid wealth decreases the consumption response to both signs of income changes. While not significant at the 5% level, the size of the consumption smoothing effect of liquid wealth seems larger for anticipated income decreases than for increases. Following *Jappelli and Pistaferri* [1], who argue that individuals might not react to very small anticipated income changes, we exclude the income changes below 10% in the fourth column of Table 4.3. We find that the asymmetry becomes larger and the smoothing effect of liquid wealth now significantly differs between anticipated income increases and decreases.

Career starters are thus not observed to behave as (near-)rational forwardlooking agents but rather as myopic agents. But, while myopia can explain the consumption response to both signs of income changes, it alone can not explain why liquid wealth asymmetrically smooths consumption.

		Dependent va	riable: ΔC_t	
	basic	all controls	interac	tion
			exclude .	ΔInc_t
			none	$<\!10\%$
	(1)	(2)	(3)	(4)
$\Delta Inc_{t,+}$	0.718^{***}	0.700^{***}	1.021^{***}	0.958^{**}
, .	(0.048)	(0.052)	(0.092)	(0.120)
$\Delta Inc_{t,-}$	0.411***	0.392^{***}	0.949***	1.017^{**}
	(0.043)	(0.044)	(0.188)	(0.178)
$\log(1 + W_{t-2})$		-373.775^{***}	-281.524^{***}	-387.845^{**}
		(43.526)	(58.409)	(92.552)
$\Delta Inc_{t,+} \times \log(1+W_{t-2})$		· · · · ·	-0.039^{***}	-0.027^{*}
			(0.012)	(0.016)
$\Delta Inc_{t,-} \times \log(1+W_{t-2})$			-0.065^{***}	-0.080^{**}
, O(<u>·</u> · ·			(0.023)	(0.021)
Controls		\checkmark	\checkmark	\checkmark
Fixed effects	Person	Person	Person	Person
F Statistic	277.72^{***}	322.61^{***}	312.95^{***}	210.77^{***}
Between Adj R ²	0.508	0.515	0.520	0.503
Within Adj \tilde{R}^2	0.162	0.174	0.182	0.150
Overall Adj R^2	0.332	0.338	0.345	0.398
Observations	50,807	50,807	50,807	32,605
Note:		*p<0	.1: **p<0.05: *	**p<0.01

Table 4.3: Estimates of the consumption response to positive and negative income changes without (columns 1-2) and with (column 3-4) liquid wealth interaction using person-fixed effects regressions over the first 6 working years of the career starters. Reported errors are person-clustered.

Behavioral economics has however shown that individuals often exhibit loss aversion when faced with decisions under risk [15]. Herein an individual exhibits a greater sensitivity to losses than to gains.

In a consumption context, this would imply that individuals should be more sensitive to having to decrease consumption than to having to increase it. Furthermore, one would expect loss aversion to become more visible for larger changes, since these entail a higher loss and more psychological stress. To test this hypothesis, we exclude the absolute income changes below the 5_{th} (P_5), 25_{th} (P_{25}), 50_{th} (P_{50}), and 75_{th} (P_{75}) percentiles in Table 4.4.⁷ The distribution of absolute income changes together with the position of the different percentiles are shown in Fig. 4.3. We find that the asymmetry does become larger for larger income changes, in line with the loss aversion theory. We perform a robustness analysis in the S.I., Appendix 4.B by excluding outliers in MPC values. The results are in line with the main results. Career starters are thus found to behave as myopic loss-averse agents who resist consumption decreases more than increases via liquid wealth.

 $^{^7 \}rm Note that this can also be interpreted as a robustness check for the 10% threshold in column (4) of Table 4.3.$



Figure 4.3: Distribution of the year on year absolute income changes for the full Belgian career starting sample over their first 6 working years. In light blue the density plot is shown for the income decreases, in dark blue the same is shown for the income increases. In red the cumulative distribution function (cdf) is shown. The black vertical lines show the 5th, 25th, 50th, 75th, and 95th percentiles values of the cdf.

	1	Dependent va	riable: ΔC_t	
		exclude	ΔInc_t	
	$< P_5$	$< P_{25}$	$<\!P_{50}$	$< P_{75}$
	(1)	(2)	(3)	(4)
$\Delta Inc_{t,+}$	1.033^{***}	1.022^{***}	0.998^{***}	0.844^{**}
	(0.093)	(0.106)	(0.130)	(0.182)
$\Delta Inc_{t,-}$	0.939***	0.951***	0.975***	1.108**
	(0.189)	(0.188)	(0.197)	(0.264)
$\log(1 + W_{t-2})$	-250.304^{***}	-309.509^{***}	-414.795^{***}	-844.034^{**}
	(61.581)	(80.145)	(126.957)	(274.902)
$\Delta Inc_{t,+} \times \log(1+W_{t-2})$	-0.040^{***}	-0.036^{***}	-0.030^{*}	-0.006
	(0.012)	(0.014)	(0.016)	(0.022)
$\Delta Inc_{t,-} \times \log(1+W_{t-2})$	-0.064^{***}	-0.069^{***}	-0.077^{***}	-0.104^{**}
	(0.023)	(0.023)	(0.024)	(0.030)
Controls	\checkmark	 ✓ 	\checkmark	\checkmark
Fixed effects	Person	Person	Person	Person
F Statistic	302.17^{***}	267.89^{***}	198.21^{***}	114.94^{***}
Between Adj R ²	0.485	0.5	0.518	0.55
Within Adj R ²	0.179	0.163	0.099	-0.077
Overall Adj R ²	0.35	0.372	0.409	0.455
Observations	48,272	38,111	25,405	12,708
Note:		*p<0.1	l; **p<0.05; *	***p<0.01

Table 4.4: Estimates of the consumption response to positive and negative income changes excluding the bottom 5 (column 1), 25 (column 2), 50 (column 3), and 75 (column 4) percentiles of absolute income changes. Person-fixed effects and person-clustered errors are used.

4.6 Discussion

The major contribution of this paper is to show evidence for myopic loss aversion in the consumption dynamics during the first years of an individual's career. Specifically, we find an asymmetric consumption response to anticipated income changes, with greater sensitivity to income increases than to decreases.

We further find that this asymmetry can be explained by an asymmetric smoothing effect of liquid wealth on the consumption responses, with a stronger smoothing for income decreases than increases. Individuals without liquid wealth exhibit approximately a one-to-one reaction to both negative and positive income changes, which is in line with myopic or present-bias behavior. Liquid wealth, by enabling an individual to insulate their consumption from income decreases, allows them to express their loss aversion.

Our findings are in line with the predictions made by the reference-dependent utility model that posits that people evaluate outcomes relative to a reference point, are loss-averse, and feel news about imminent consumption more heavily than news about distance consumption [31]. The presence of myopic loss aversion has also been firmly established in investor behavior [27–29]. Furthermore, it is able to explain many of the partial findings in the empirical literature on consumption dynamics. In our paper, it explains why individuals react to both positive and negative income changes and why individuals with higher liquidity exhibit lower consumption responses to anticipated income changes.

An important avenue for further research is to test whether our findings extend beyond our sample of career starters in a mature and relatively egalitarian economy. Specifically we want to make sure that our results also hold for more mature age cohorts and for emerging market economies. As the results by *Japelli* and Pistaferri [2] indicate, we expect more mature age cohorts to have lower total consumption responses. It remains an open question if this is mainly mediated by a built-up of wealth or lower levels of myopia and/or loss aversion or something else.

Finally our results suggest there may be a link between a country's population structure and the effectiveness of its macroeconomic policies. Indeed, in ageing economies, where most people have liquid wealth and starters constitute only a small part of the total population, our results suggest that consumption may on average be less elastic to income. In young economies, in contrast, starters constitute a more substantial part of the population and the average level of liquid wealth is expected to be lower, suggesting that this country's consumption may on average respond stronger to changes in income. This hints to the possibility that Keynesian fiscal policies, that depend on fiscal multipliers and hence consumption dynamics, may be more effective in less mature and younger economies than in more mature and ageing economies. We defer the further analysis of this to future research.

Appendix

4.A Representativeness of the data

Because few official statistics exist on career starters, we also compare key figures of our work-eligible sample to those of the general Belgian work-eligible population.

- The median net wage in Belgium lies around €2,000 [33]. Our sample's median income, which is broader than wage alone, is €2, 126.86.
- The mean age of a working Belgian was 41.6 in 2013 [34]. The mean age in our sample is 41.63.
- The gender distribution, between the ages 18-64, in 2009 for Belgium was 49.78% female and 50.22% male [33]. In our sample, with ages between 15-60, the gender distribution is 49.4% female and 50.6% male
- The distribution of starters and the work-eligible Belgians among the provinces in our sample is also largely in line with national statistics [33, 35]. Due to confidentiality however, we can not explicitly release these distributions.

We find that the key figures in our work-eligible sample are largely in line with those of the work-eligible Belgian population.

4.B Robustness check

We perform a robustness check against outliers in Table 4.B.1 by excluding extreme MPC-values. Extreme MPC-values might originate from numeric artefacts such as a 10 *cent* increase in income and a ≤ 10 increase in consumption leading to an MPC of 100. For outliers in either consumption or income, these extreme MPC-values might also occur. To avoid this we calculate a yearly MPC per individual and exclude observations in the top and bottom 5% (column 1) and 15% (column 2). The results are in line with our earlier findings.

	Dependent	variable: ΔC_t
	exclud	e extreme
	MPC (1	oothways)
	5%	15%
	(1)	(2)
$\Delta Inc_{t,+}$	0.991^{***}	1.051^{***}
	(0.076)	(0.063)
$\Delta Inc_{t,-}$	1.072^{***}	0.962^{***}
	(0.202)	(0.106)
$\log(1+W_{t-2})$	-371.303^{***}	-315.510^{***}
	(78.056)	(59.283)
$\Delta Inc_{t,+} \times \log(1 + W_{t-2})$	-0.023^{**}	-0.020^{**}
	(0.010)	(0.009)
$\Delta Inc_{t,-} \times \log(1+W_{t-2})$	-0.074^{***}	-0.041^{***}
	(0.025)	(0.014)
Controls	\checkmark	\checkmark
Fixed effects	Person	Person
F Statistic	376.81^{***}	569.93^{***}
Between Adj R ²	0.586	0.708
Within Adj R ²	0.289	0.455
Overall Adj R ²	0.437	0.586
Observations	45,217	35,057
Note:	*p<0.1; **p<	0.05; *** p<0.01

 Table 4.B.1: Robustness checks of the regression reported in column (3) of Table 4.3 for

 different MPC trimming schemes. The table excludes the top and bottom 5% (column 1),

 and 15% (column 2) of MPC-value observations. Person-fixed effects and

 person-clustered errors are used.

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Part III

A multi-faceted view on behavior in a virtual world

5

Revealed behavior in a virtual world: the case of EVE Online

The work presented here on the collection and processing of the EVE Online data was made possible and done in collaboration with the team members of the LAB-M project, led by Koen Schoors and Jan Ryckebusch. Special thanks to Kevin Hoefman for always providing expert knowledge on the internal game dynamics and Andres Maria Belaza Vallejo for his help in processing the raw data. Without their efforts several, if not all, of these projects would not have been possible.

5.1 Schematic overview



Figure 5.1: Schematic overview of the workflow leading to the research subjects presented in Chapter 5.

5.2 A live feed into socioeconomic behavior

As mentioned in the introduction, even when researchers can get access to the data of multinational companies with millions of clients, it is often only data on one small aspect of their clients' lives. This narrow view limits the possible questions that can be posed and insights that can be gathered. Being able to track, in detail, multiple aspects of an individual's behavior would enable researchers to ask a wider variety of questions, and to better capture the complexity of socioeconomic behavior. Currently, Virtual worlds, defined as: *"computer-based online community environments that are designed and shared by individuals so that they can interact in a custom-built, simulated world"*, are one of the best possible sources of such diverse trace data. Since every action inside it is logged, it can be seen as a live feed into the socioeconomic behavior of hundreds of thousands of people.

Virtual worlds come in all shapes and sizes, all with their own setting and goals. For this reason it is important for researchers to have an as complete as possible understanding of the experiences of participants before constructing possible research questions on the data. Finding relevant answers to enduring social science questions requires the motivations of the individuals inside the virtual world to align with the motivations in the real world. For instance, many virtual worlds exist in which there are one or several fixed story lines through which the players can choose to play, getting rewarded by the game along the way. Players can then choose to do this alone or in collaboration with other players but they almost always play against the game (e.g. players have a common, computer-driven enemy or developer-designed goal). While such a game could be useful to investigate collaboration, importance of team composition, leadership, and other social factors, it often lacks the driving forces to investigate economic questions such as market efficiency, price setting, etc.

Partly because of this lacking alignment in economic motivations, not much economic research has been done using virtual worlds. Recent advances in computer power and internet usage have however brought about more opportunities. Indeed, as *Knowles and Castronova* explain in [1], together with growing global access to the internet and increasing available computer power, the complexity and populations of virtual worlds also experienced an explosive growth. This brought with it more complex virtual economies which present a unique opportunity for socioeconomic research.

Recent literature employing these worlds for research ranges from: the general usefulness of virtual worlds as a research tool [2, 3], their economic organisation [1, 4], war and conflict economics within them (e.g. drivers of military success [5], conflict kindling institutions [6], etc.), and even inequality [7]. A lot of questions, originating from a range of social science fields, however remain. Our group already investigated a few of these as will be described below. The rest of this chapter is organised as follows. In section 5.3 I first explain what EVE Online, the virtual world we study, is and why it is fit for economic research. Then, in section 5.4, I describe what data we collected and what we did to get it. Finally, I end this chapter in section 5.5 with a short description of what research this data has already brought about, what is still in progress, and what the future might bring.

5.3 Warping into the EVE Online universe

As mentioned above, there are many types of virtual worlds, differing primarily in the objective set out for players. One of the most interesting types of virtual worlds for research purposes are so-called "sandbox games" [8]. Just like the sandbox in a playground, players are provided with an environment and the tools to explore it but can choose what, when, and how they approach the available content. There are no stories to be followed, no greater evil to defeat. The totality of interactions players have with each other and the environment is able to transform and shape the experience of the virtual world. For instance social institutions emerge, players organise, long-lasting power dynamics are formed, etc. The freedom players get in sandbox games fosters realistic socioeconomic behavior and makes it a suitable candidate from research.

Arguable the most advanced and complex open-ended sandbox game is EVE Online (EVE). Since it is such a complex game, explaining all the game-dynamics would require an entire book's worth of pages, which is out of scope here. We instead give two excerpts from papers produced by our research group which demonstrate the socioeconomic complexity and relevance of EVE.

Hoefman et al. [9] describes the variety of actions that players can perform, the permanence of losses, and the existence of completely player-driven supply- and manufacturing chains leading to realistic economic behavior (e.g. loss aversion, endogeneous prices, market specialization, etc.) :

Eve Online (EVE) is an open-ended Massively Multiplayer Online Game set in a science fiction universe and created by Icelandic company CCP Games in 2003. More than 500,000 players compete for resources and territory while engaging in a variety of professions and activities including mining, manufacturing, trading, piracy, exploration, and combat, both versus the environment and against other players.

EVE contains 12,709 distinct items that can be bought and sold between players including ships, ship modules, minerals, ammunition, blueprints, and many more. The items available and their characteristics (which players can view at any time at zero cost) are decided

...
...

by CCP and only rarely adjusted. Market prices, on the other hand, are endogenously determined by the market behavior of players via a double auction system that matches buy orders with sell orders. Prices fluctuate daily around a mostly stable base. Players can buy and sell anywhere in the virtual universe, but for reasons of efficiency market activity tends to cluster in hubs. Two thirds of all market transactions are conducted in a single central trading hub.

Items and resources in the game are bought and sold with an ingame currency called the Inter-Stellar Kredit (ISK). Players earn ISK as a reward for engaging in activities such as defeating pirates, running missions, selling resources gained through mining, selling goods made through industry, offering services like courier contracts or protection to other players, or by paying real-world money. Most players spend time in the game earning ISK to purchase ships, modules, skills, etc. Advanced players even pay for their game subscription through their in-game earnings. One billion ISK is roughly equivalent to 15 USD in the period of our analysis. Because ISK has both in-game and real-world value, and because losses in EVE are permanent, players tend to be risk averse, and this fosters realistic economic behavior.

On the social organisation aspect of the virtual world, *Belaza et al.* [10] explain:

The players organize themselves in social structures called alliances with sizes between one and about 25,000 players. The alliances can conquer territory, where they can impose their own taxes, exploit mineral resources, and so on. Because the data comes from a virtual world, complete and accurate records of all alliance standings across time are available and advanced statistical analyses become feasible.

The relations between the alliances represent an important aspect of the game as they impact a wide range of game-play experiences. The leadership of an alliance can explicitly and publicly set these relationships to friendly, hostile, neutral or undetermined. This is important because these standings affect how players from one alliance react to players from another alliance by facilitating the process of discriminating between friends, enemies, and others. Most alliances in EVE follow a "Not Blue, Shoot It" policy: friends are to be left in peace, while any other relationship means to shoot on sight. However, military, planned and coordinated actions between players have mainly enemy alliances as objectives.

Beyond the aspects discussed in the excerpts, there are two important features of EVE Online worth mentioning. First, there is a real time-investment for players to learn skills inside the game, taking weeks to even months before being proficient in anything from market trading to mining. Because of this we see that most players, as in life, have to choose what they want to spend their time on learning and end up specializing in certain fields. Second, even when there is no specific game dynamic provided by the developers to organise a certain activity, players find a way to organise it on their own. A fascinating example of this are coalitions. The highest built-in organisational structure for players to organise themselves in are alliances. Each player can see to what alliance a certain player belongs inside the game. As explained in the second excerpt, alliances collect taxes and organise industry and logistic activities for their members. These alliances can seen as the virtual counterpart of countries. While there is no in-game feature available that enables further organisation of these alliances, there exist player organised coalitions of alliances (comparable to the EU) that band together to protect their common interests (e.g. border security, internal trade, external trade, industry activities, etc.).

A definitive overlap in behavioral drivers can thus be seen between the virtual world of EVE Online and the real world, making it suitable to perform social science research on.

5.4 Collecting data wearing ice cleats

As discussed in the introduction of this work, collecting trace data is never easy. This was no different when trying to get access to the EVE Online data. However, thanks to the efforts of Kevin Hoefman, who presented on several player meets, we eventually got a skype meeting with the people who could make this project happen. Luckily, they were as excited as us to gain more insights into the behavior of their players.

This wasn't the first time CCP invested resources into something like this. Because it has such a complex economy, CCP hired Dr. Eyjolfur Gudmundsson in 2008, world's first economic scholar in charge of overseeing a virtual economy, or "the virtual Alan Greenspan" [11] as the BBC dubbed him. He was tasked with overseeing the health of EVE's economy. Among his responsibilities were: keeping track of money drains and sources, keeping inflation in check, countering real money trading, which is the act of selling in-game goods for real-world money, sometimes linked to money laundering, and many other tasks normally performed by central banks.

After negotiating contracts, signing NDA's, and getting clearance to go to the CCP offices, which are located in Reykjavik, Iceland, we were ready to go and collect data. We had to go in person because the size of the data didn't allow an

efficient transfer via any sort of VPN connection. I personally went to Iceland twice to go and gather data. We prepared for these trips as good as we could in advance, prioritizing what data we needed, learning the ins and outs of the databases they used, from Python based Hadoop to SQL servers, so that we could extract as much as we could in the limited time we had on-site. I even bought ice cleats to wear on my shoes because, during winter, the sidewalks and roads in Iceland are covered in a thick layer of ice and I couldn't risk falling on one of our precious hard drives.

The data we eventually collected ranged from years worth of every single timestamped market transactions, the population of courier-, exchange-, and auctioncontracts, the distribution of activities that players spent their time on, the supply and production lines of items, details on all the industry activities, (changes in) political standings between alliances, social interactions between players, personal characteristics of players, and many more aspects of life in EVE and of its players.

With this data in hand, we came back to Ghent, Belgium and went to work.

5.5 Realized, ongoing, and future projects

In this section I will briefly explain the different projects that utilize the EVE data that Kevin Hoefman and myself collected. I start with the projects that have already resulted in publications and end with a short conceptual overview of the ongoing projects and a note on what the future might bring.

5.5.1 Realized projects

Social Balance Theory The first application was on testing and extending Social Balance theory (SBT), which is the theory behind the principle of "the enemy of my enemy is my friend", utilizing a statistical physics approach. **Personal contribution:** collected and prepared data, advised on early text and research.

This project resulted in a paper titled: *Statistical physics of balance theory* [12] (http://hdl.handle.net/1854/LU-8530113) and was published in the journal PLOS One. It built on insights gleaned from balance theory in social network studies and from Boltzmann-Gibbs statistical physics. It proposed a generic Hamiltonian with three terms to model the triadic energies. One term is connected with a three-body interaction that captures balance theory. The other terms take into account the impact of heterogeneity and of negative edges in the triads. The validity of this model was then tested on four datasets including the time series of triadic relationships for the standings between alliances in EVE.

This model was later extended to include non-active relationships among alliances. A paper detailing this was published in *Physica A: Statistical Mechanics and its Applications* under the title *Social stability and extended social bal-* *ance:* Quantifying the role of inactive links in social networks [10]http://hdl.handle.net/1854/LU-8586026.

Hedonic Pricing Theory A second application was in testing Hedonic Pricing Theory (HPT), according to which market forces operate on individual characteristics of a good, and the price of a product is the aggregate of the price across those characteristics. **Personal contribution:** assisted in the collection of the data.

By analyzing data from the large, market-driven virtual world of EVE, it was possible to test HPT, while largely avoiding the pitfalls of data limitations in the real-world (e.g. heterogeneous availability of information among individuals, hard to quantify characteristic qualities, etc.). It was found that a linear model with functional characteristics predicts the prices poorly, but that a log-linear model performed quite well. Adding social characteristics to this log-linear model (e.g. rarity, status signaling), which was possible with the EVE data but is very difficult to measure in the real-world, improved the predictions substantially.

These findings, published in the article "*The impact of functional and social value on the price of goods*" [9] in PLOS One (http://hdl.handle.net/1854/LU-8582900), strongly supports HPT and demonstrates a rational calculus including social value.

5.5.2 Ongoing projects and the future

With the many opportunities this data offers, we also have quite a few ongoing projects. While not going into detail on every single project, I will try to outline a sample of the research questions here.

Connections with the real world An interesting idea is to approach the virtual world as a large questionnaire about the real world, answered by hundreds of thousands of people through their actual *revealed behavior*. The thousands of decisions individuals make in the virtual world could then reflect the evolution of their socioeconomic situation and behavior in the real world. This would make virtual worlds a real-time or even predictive tool for socioeconomic changes in the real world. For instance the decision of subscription payment, where the choice is between investing time to collect ISK (in-game currency) to pay for the monthly subscriptions or to pay by cash, could reflect the economic situation in the country of the player. With the recent Ruble crash in 2014, we for instance clearly saw a rise in Russian players switching from paying cash to investing time gathering ISK inside the game to buy the subscription. We are exploring such dynamics to construct economic metrics that can be updated daily and would mean a step forward in measuring the economic situation in countries beyond the infrequent data publicised by governing bodies.

Beyond the economic metrics, this data also provides an opportunity to keep track of social unrest. Roma Standaert, under my supervision, recently completed her master thesis [13] on the connection between the characteristics of individual's country of origin and their behavior inside EVE. She found that individuals from less developed countries are less cooperative and those from countries with more violence exhibit more aggression in EVE.

Complete information Just as for the papers discussed in section 5.5.1, one of the main advantages of a virtual world is the completeness of the data. This enables us to capture dynamics more completely than real-world data currently allows.

An ongoing project for instance is using the fact that we have every single change in political standings between the alliances to fully track the propagation of these changes throughout the system using temporal webs [14]. Temporal webs are networks that also capture the time dimension and as such can be used to track the evolution of networks. Doing so for the political network in EVE can provide insight into how divides and fragmentation happens in political systems.

Future possibilities Out of experience, I learned that it is impossible to exhaustively say what is possible with a dataset. Maybe (and hopefully) a new Ph.D. researcher will come up with a new and innovative use for all these data to further many different fields. I am for one excited to see what is to come.

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6 Summary and outlook

The work presented in this dissertation is part of an emerging specialism within economics. This specialism focuses on employing new types of data-sets to provide novel perspectives on enduring and previously unanswerable questions. We employ three different sets of *"Trace data"*, which we define here as *"data originating from the natural usage of (digital) products or services of which the collection does not interfere with the natural flow of behaviour and events in the given context"*, to conduct four research projects. For every project, we highlight one important aspect of working with this emerging type of data.

In the second chapter, we analyze data on the full population of contracts from the Russian domestic unsecured interbank lending market between January 2000 to October 2004. We investigate whether common data granularity limitations and aggregation choices concerning loan maturity in the interbank literature obscures important structure and/or economic functions. Our main finding is that disregarding loan maturity consistently obscures mesoscale structure. We also find that this practice obscures important economic functions and that the optimal loan maturity granularity is dependent on the development phase of the network.

This chapter highlights the fact that extra granularity only matters if it is informative for the research question at hand. Too much detail spreads the data thin and weakens the power of statistical inference, while too little detail hides features and patterns.

The third and fourth chapter utilizes client-level financial and demographic data on Belgian clients of a large European bank. Both chapters utilize the magnitude of the data-set to zoom in on career starters. This highlights the fact that by carefully selecting a subset of the population, it is possible to minimize confounding factors, increase comparability, and better focus on the research question at hand.

The third chapter explores three possible mechanisms - social capital, innate ability, and human capital allocation - behind the observed positive relationship between wealth inequality and income immobility. We find higher earning performances for individuals with higher financial wealth at the start of their careers. Evidence is found for a transmission channel via human capital allocation, in the form of job-matching efficiencies.

In the fourth chapter, we investigate the consumption response to positive and negative income changes conditional on the presence of liquid wealth. We find an asymmetric consumption response to income changes, with a higher response to income increases than to income decreases. We further find that this asymmetry can be explained by a higher consumption smoothing effect of liquid wealth for income decreases than for income increases. Our results provide evidence for myopic loss-averse behavior.

The fifth and last chapter explores a thus far little used source of trace data in economics, namely virtual worlds. This chapter highlights that in the age of digitalisation, where data is a byproduct of everyday life, useful data can come from new and unexpected sources. We introduce EVE Online, an advanced and complex open-ended sandbox game. We detail the world of EVE Online and explains what design choices drive the realism of in-game behavior. I then describe the contributions I made for our team to acquire data from EVE Online, enabling the construction of a multi-faceted view on the behavior of (groups of) players. I further describe three published papers that utilized the collected data.

Apart from the types of data used and the new methodological skills necessary to handle and process such data, an epistemological theme stands central in this specialism, complementing that of classic, theory-driven economics. It does so by not solely relying on theoretical insights to steer the research, which then becomes mostly deductive, but rather working in complementary phases of induction and deduction. Herein theories and hypotheses are constructed and refined by interacting with the data, often without a preconceived notion of what patterns to expect. The specialism underlines the transformative power data has and will continue to have on the field of (empirical) economics. However, we find that the expert-knowledge needed throughout every chapter underlines that, in a world filled with extensive, complex data-sets, a solid organizing economic framework will become more important than ever.

Outlook

As a final step we look ahead by discussing the ongoing and planned future research that is connected to the work or data presented in the preceding chapters.

In line with the societal problems investigated with the European bank's client data, we are currently utilizing this data to investigate gentrification. More precisely, we are trying to figure out who benefits from gentrification and if and how these benefits could be optimized. To this end, we have already extracted over 200,000 moving events from the data together with the composition of the individual's neighbourhood before and after the move. We have preformed some exploratory analyses on the characteristics of these moves and calculated first estimates of the effect of growing up in a financially diverse neighbourhood on income. Preliminary findings show a positive effect of growing up in a financially diverse neighbourhood on income. However, we also find indications of the lower wealth households being crowded out of their neighbourhoods which could indicate that they are often not able to reap the benefits of these effects.

Further, beyond the ongoing projects pertaining to the EVE Online data already mentioned in Chapter 5, we are also using the data to construct network measures that characterize the spatial distribution of activity and are still actively searching for potential use-cases and collaborations to leverage these data.

Lastly, it became apparent throughout the analyses of the different projects that the classic economist's analytical toolbox is ill-equipped to handle the sheer magnitude and diversity of these new types of data. Especially when extensive models are needed to capture the full heterogeneity and complexity of the data, one quickly reaches the computational and conceptual limits of the classic tools. If researchers want to move beyond zooming in on subsets of these massive datasets and leveraging them in full, new tools are needed. We, together with among others Susan Athey [1], believe such tools can come from adapting methods from Machine Learning to fit the inference needs of economists. Doing so would make model selection data-driven, would produce confidence intervals for the models, is systematic, and most importantly has a fully transparent methodology. For these reasons, we have started researching the foundations of Machine Learning to investigate if the methods used to give their algorithms the power to handle immense complexity can be transferred to inference problems.

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Samenvatting

Het werk gepresenteerd in dit proefschrift maakt deel uit van een opkomend specialisme binnen de economie. Dit specialisme richt zich op het gebruik van nieuwe soorten datasets om originele perspectieven te bieden op blijvende en voorheen onbeantwoordbare vragen. We gebruiken drie verschillende sets van "*Trace data*", hier gedefinieerd als "gegevens komende van het normale gebruik van (digitale) producten of diensten, waarvan de vergaring de gedragingen of acties niet beinvloeden in de gegeven context", om vier onderzoeksprojecten te realiseren. Voor elk project belichten we een belangrijk aspect van het werken met dit opkomende type dataset.

In het tweede hoofdstuk analyseren we gegevens over alle contracten binnen de Russische binnenlandse onbeveiligde interbancaire kredietmarkt tussen januari 2000 tot oktober 2004. We onderzoeken of veelvoorkomende granulariteitsbeperkingen en aggregatiekeuzes met betrekking tot de looptijd van leningen in de interbancaire literatuur belangrijke structuur en/of economische functies verbergen.

Onze belangrijkste bevinding is dat het negeren van de looptijd van een lening consequent de mesoschaalstructuur verbergt. We zien ook dat deze praktijk belangrijke economische functies verhult en dat de optimale granulariteit voor de informatie over de looptijd van leningen afhankelijk is van de ontwikkelingsfase van het netwerk.

Dit hoofdstuk benadrukt het feit dat extra granulariteit alleen van belang is als het informatief is voor de onderzoeksvraag. Teveel detail verzwakt de kracht die statistische conclusies kunnen hebben, terwijl te weinig details functies en patronen kunnen verbergen.

Het derde en vierde hoofdstuk maken gebruik van financiële en demografische gegevens op cliëntniveau over Belgische klanten van een grote Europese bank. In beide hoofdstukken wordt de grootte van de dataset gebruikt om in te zoomen op carrire starters. Dit benadrukt het feit dat door zorgvuldig een subgroep van de populatie te selecteren, het mogelijk is om verstorende factoren te minimaliseren, de vergelijkbaarheid te vergroten en een betere focus op de onderzoeksvraag in de hand te werken.

Het derde hoofdstuk onderzoekt drie mogelijke mechanismen - sociaal kapitaal, aangeboren bekwaamheid en toewijzing van menselijk kapitaal - achter de waargenomen positieve relatie tussen ongelijkheid in kapitaal en inkomensimmobiliteit. We vinden hogere verdienprestaties voor mensen met meer financiële middelen aan het begin van hun loopbaan. Er worden aanwijzingen gevonden voor een transmissiekanaal via toewijzing van menselijk kapitaal, in de vorm van hoe efficiënt het zoeken van een baan verloopt binnen de job markt.

In het vierde hoofdstuk onderzoeken we de consumptiereactie op positieve en negatieve inkomensveranderingen in de aanwezigheid van liquide kapitaal. We vinden een asymmetrisch consumptiereactie op inkomensveranderingen, met een hogere respons op inkomensstijgingen dan op inkomensdalingen. Verder constateren we dat deze asymmetrie verklaard kan worden door een hoger effect op het afvlakken van de consumptie van liquide kapitaal voor inkomstendalingen dan voor inkomensstijgingen. Onze resultaten zijn consistent met het bestaan van kortzichtigheid en een afkeer van het verlagen van consumptie.

Het vijfde en laatste hoofdstuk onderzoekt een tot nu toe weinig gebruikte bron van "Trace data" in de economie, namelijk virtuele werelden. Dit hoofdstuk benadrukt dat in het tijdperk van digitalisering, waar gegevens een bijproduct zijn van het dagelijks leven, nuttige gegevens afkomstig kunnen zijn van nieuwe en onverwachte bronnen. We introduceren EVE Online, een geavanceerd en complex open-ended sandbox-game. We beschrijven de wereld van EVE Online en leggen uit welke gemaakte ontwerpkeuzes het realisme van het in-game gedrag stimuleren. Vervolgens beschrijf ik de bijdragen die ik heb geleverd om ons team in staat te stellen gegevens van EVE Online te verzamelen. Deze inspanningen hebben ervoor gezorgd dat het construeren van een veelzijdig beeld van het gedrag van (groepen van) spelers mogelijk was. Ik beschrijf verder drie gepubliceerde artikelen die de verzamelde gegevens hebben gebruikt.

Afgezien van het nieuwe type data dat wordt gebruikt en de nieuwe methodologische vaardigheden die nodig zijn om dergelijke gegevens te verwerken, merken we ook op hoe het specialisme dat centraal staat in de hoofdstukken de epistemologische framing van klassieke, theorie-gedreven economie aanvult. Dit door niet enkel op theoretische inzichten te steunen om onderzoeksvragen te ontwerpen, dat dan voornamelijk deductief is, maar eerder door in complementaire fasen van inductie en deductie te werken. Hierin worden theorien en hypotheses geconstrueerd en verfijnd door te interageren met de data, vaak zonder vooropgestelde verwachtingen van de resultaten. Echter, hoewel het specialisme de transformatieve kracht benadrukt die "Trace data" heeft, en zal blijven hebben, op het gebied van (empirische) economie, willen we dit toch nuanceren. De hoeveelheid expertkennis die in elk project nodig was om de data en zijn mogelijkheden te kaderen, benadrukt dat in een wereld vol uitgebreide, complexe data sets, een stevig organiserend economisch kader belangrijker zal worden dan ooit.