

Robust matching of occupancy maps for odometry in autonomous vehicles

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Abstract: In this paper we propose a novel real-time method for SLAM in autonomous vehicles. The environment is mapped using a probabilistic occupancy map model and EGO motion is estimated within the same environment by using a feedback loop. Thus, we simplify the pose estimation from 6 to 3 degrees of freedom which greatly impacts the robustness and accuracy of the system. Input data is provided via a rotating laser scanner as 3D measurements of the current environment which are projected on the ground plane. The local ground plane is estimated in real-time from the actual point cloud data using a robust plane fitting scheme based on the RANSAC principle. Then the computed occupancy map is registered against the previous map using phase correlation in order to estimate the translation and rotation of the vehicle. Experimental results demonstrate that the method produces high quality occupancy maps and the measured translation and rotation errors of the trajectories are lower compared to other 6DOF methods. The entire SLAM system runs on a mid-range GPU and keeps up with the data from the sensor which enables more computational power for the other tasks of the autonomous vehicle.

1 INTRODUCTION

The technology advancement in sensors and computer systems is enabling the proliferation of Advanced Driver Assistance Systems (ADAS) into the car market at an unprecedented pace. As of the year 2015, systems such as adaptive cruise control, automatic parking, automotive night vision, collision avoidance, emergency braking, hill descent, lane departure assistance, traffic sign recognition etc. can be found as standard equipment even in the mid-range vehicles on the market. Recent reports about road safety indicate that driver error is the main contributor to more than 90% of traffic accidents (KPMG,2012), (Fagnant,2013). Even when the main reason for a crash is due to malfunctions of the vehicle or problems with the road or environment, some additional human factors can often have contributed to the crash and the severity of the injuries. Leading companies involved in autonomous

vehicles believe that only completely self-driving cars will fully address safety concerns.

Such intelligent vehicles make use of advanced perception systems that could sense and interpret surrounding environment based on various kinds of sensors, such as: radar, lidar (laser rangefinder), monocular / binocular / omnidirectional vision systems, ultrasound, etc. Many of the following tasks for the intelligent vehicle can be performed within the same framework of sensory interpretation (Leonard,2008), (Nguyen,2012). The initial tasks is ego localization since the vehicle can't drive safely if it doesn't know its location and orientation (i.e. pose). The problem of pose estimation has been exhaustively researched in various applications such as stereo vision, structure from motion, mapping and augmented reality, however one can conclude that most of the proposed methods in the literature are computationally expensive and do the estimation off-line. The mainstream of approaches are based on key feature detection in optical video frames, which

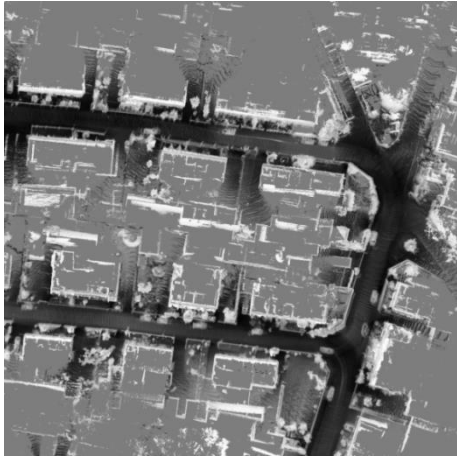


Figure 1: Small section of an occupancy grid map with cell size 12.5x12.5cm

can be assessed by looking at the standard odometry benchmark (Geiger, 2012 and 2013). Tracking and registration of the detected features is often done using the Iterative Closest Point (ICP) approach (Pomerleau, 2013). Pose estimation can also use the data from inertial navigation sensors (INS), global position system (GPS) or wheel rotation sensors, as prior motion information in achieving real-time computation speed (Scherer, 2012). Kalman or particle filters are often used in order to reinforce the measurements with the past data for more natural estimation.

When no additional data is available but the one that comes from the stereo cameras and/or lidar, many approaches have been proposed registering the point clouds using a more suitable representation. Notably, methods such as (Moosmann, 2011) use projection of the point cloud onto a range image and then use features extracted from these images to do the matching between consecutive sweeps. On the other hand, there are methods which try to extract geometric primitives from within the point clouds, such as planes and edges, and then use them for matching and registration (Zhang, 2014). These approaches have their pitfalls in situations where the environment does not contain simple planes and edges (open roads, forests, parks). There are two issues with these types of approaches : first, the high computational cost for extracting the robust image features and second, images in the visual spectrum often fail to capture good information in adverse weather conditions and during the night.

Therefore, we part with the standard 6DOF point cloud registration paradigm and propose a novel algorithm for simultaneously mapping the perceived environment and performing the localization task using the previous state of what has already been

mapped. We adopt the so called occupancy grid map as a medium for all further operations of the autonomous vehicle. In the literature, authors make use of these logical representation, i.e. maps, which explains the occupancy of the environment in a probabilistic way, first proposed by (Moravec, 1985) for use in sonar mapping.

Occupancy grid maps are spatial representations of the external environment. The external world is represented by a high resolution grid of variables that model the occupancy of the space. Besides the mapping the occupancy data can also be used for various other key functions necessary for the mobile vehicle navigation, such as positioning, path planning, collision avoidance object detection and prediction of the future state of the environment.

Older studies suggest that occupancy grid maps are arguably the most successful environment representation in mobile robotics to date (Kortenkamp, 1998). Moreover, in the domain of autonomous vehicles, they are an optimal way of recording a background model of the vast environments, Fig.1. An efficient implementation of these maps has been proposed by (Homm, 2010), which will be explained in more detail in chapter 2.

We also make a simplification to the system assuming that the world the vehicle is moving through is completely flat and that it can be precisely modelled via a two dimensional map. This way the localization becomes a 3DOF registration problem which can be solved robustly and more importantly, with a tight real-time constraint. Our main sensor is the Velodyne HDL-64E lidar which experiences the same general motion as the vehicle: three degrees of translational freedom and three degrees of rotation relative to the environment. The pose estimation can be seen as a closed feedback loop system that also tries to produce a map of the environment using the estimated pose information. A detailed analysis of the classical pose estimation approach and our simplified method follows in chapter 3.

The speed and accuracy of the proposed method is experimentally tested in chapter 4 and we give our concluding remarks in the discussion in chapter 5.

2 OCCUPANCY MAP

The proposed model of the environment estimates the probability of occupancy for each world coordinate using the inverse sensor logic. This means that the sensor measurements are used to reconstruct the most probable map using a Bayesian reasoning. Occupancy maps can be a very elegant

solution to the problem of mapping when there is a multitude of heterogeneous sensors on board the vehicle. They are invariant to the category of the scanned objects in the environment as long as they are correctly transformed into probability of occupancy. For example, one can incorporate measurements from object detectors, ultrasound objects, distance measures from lidar or stereo cameras into one single occupancy map.

Let us define the occupancy map as a 2D grid m in the xy plane with grid elements $m_{i,j}$ and a series of $z_1, \dots, z_T$ measurements obtained from the lidar. Each sensor measurement z_i contains information about the occupancy of several grid locations together with the pose of the vehicle which might come from other sensors. So, the problem of simultaneous building of the map and localization of the vehicle can be explained by finding the ego motion of the vehicle using the previously built map and cumulatively computing the probability of occupancy for each grid element $m_{i,j}$ given the new measurements in Z_T .

We will first explain the update of the occupancy map for a static vehicle, or a moving vehicle for which we already solved the ego location. The probability of occupancy for each grid element (cell) can be estimated separately from the rest of the map

$$p(m_{i,j}|z_1 \dots z_T). \quad (1)$$

Commonly the log-odds or log likelihood ratio representation is used for computational reasons since its update requires a simple addition operation,

$$l_{i,j} = \log \frac{p(m_{i,j}|z_1 \dots z_T)}{1 - p(m_{i,j}|z_1 \dots z_T)}, \quad (2)$$

where the posterior $m_{i,j}$ can be reconstructed from $l_{i,j}$ by

$$p(m_{i,j}|z_1 \dots z_T) = 1 - \frac{1}{e^{l_{i,j}}}. \quad (3)$$

Since the error level of our sensor is lower than the cell size, there is a high probability that most measurements will fall within their respective grid cells. Thus, we make an assumption that the probability of occupancy of $m_{i,j}$ is conditionally independent of the rest of the map, even from its neighbouring cells. We therefore can estimate the posterior as

$$\begin{aligned} & p(m_{i,j}|z_1 \dots z_T) \\ &= \frac{p(z_T|m_{i,j})p(m_{i,j}|z_1 \dots z_{T-1})}{p(z_T|z_1 \dots z_{T-1})}. \end{aligned} \quad (4)$$

If we apply Bayes rule to the term $p(z_T|m_{i,j})$ we have the probability that the cell $m_{i,j}$ is occupied:

$$\begin{aligned} & p(m_{i,j}|z_1 \dots z_T) \\ &= \frac{p(m_{i,j}|z_T)p(z_T)p(m_{i,j}|z_1 \dots z_{T-1})}{p(m_{i,j})p(z_T|z_1 \dots z_{T-1})}. \end{aligned} \quad (5)$$

The probability of the grid cell to be free $\overline{m_{i,j}}$, can be expressed with the same equation, and by noting that $p(\overline{m_{i,j}}) = 1 - p(m_{i,j})$ we can devise recursive expression for the map update at time T given the past map and the current measurements and pose:

$$\begin{aligned} l_{i,j} = \log & \frac{p(m_{i,j}|z_T)}{1 - p(m_{i,j}|z_T)} \\ & + \log \frac{1 - p(m_{i,j})}{p(m_{i,j})} \\ & + l_{i,j}^{past}, \end{aligned} \quad (6)$$

where the initial map can be constructed from the prior probabilities for occupancy for each grid cell:

$$l_{i,j}^0 = \log \frac{p(m_{i,j})}{1 - p(m_{i,j})}. \quad (7)$$

This approach builds an incremental map of the environment containing the log-odds for occupancy. The first term of equation (6) explains the log-odds of occupancy for a single cell given the measurements in z_T , and the second term is the prior log-odd of the cell. This relation is usually called an inverse sensor model because it translates the sensor measurements into their causes, i.e. the map. At any given point one can recover the probability of occupancy for the whole map using equation (3).

A more accurate approach to occupancy map estimation is the forward sensor model which computes the likelihood of the sensor measurements in the space of all possible maps. This approach is an optimization problem where we search an optimal map which maximizes the probability of the given measurements. However, the forward model formulation prohibits a real-time implementation since it requires every sensor measurement in order to find the optimal map. We refer to (Thrun, 2003) for further information about the implementation of the forward sensor model.

In the following chapter we will explain how the pose estimation of the vehicle can be performed using the currently unregistered occupancy map data with relatively low computational complexity and high level of accuracy.

3 POSE ESTIMATION

3.1 Classical 6DOF approach

The pose of the sensor (lidar) corresponds to the orientation and position of the vehicle, where in the first moment of time the pose is arbitrarily set at the coordinate centre. As the vehicle is moving through the world, it experiences rotational and translational changes to its pose. The simplest forward motion on a flat road produces a translation change in the axis perpendicular to the vehicle motion, thus the vehicle is moving with one degree of freedom. In the real world though, the vehicle might be taking a turn in a bend which has some incline (grade) and a slight camber to the road surface. Furthermore, the vehicle suspension will try to dampen the effects of the forward and lateral acceleration and keep the vehicle level to the ground. In these actual scenarios the sensor attached to the vehicle is experiencing changes within 6 degrees of freedom: motion in the three spatial dimensions, and rotation around the three axes, at the same time.

The problem of pose estimation then becomes the standard problem encountered in structure from motion applications where a 6DOF fundamental matrix which explains the change of pose is being estimated from the sensor data. Assuming that the change in sensor data between two time intervals is entirely due to motion through static environment, then the 3D points measured in the present P^t are related to the 3D points measured in the past P^{t-1} via the augmented matrix:

$$P^t = \begin{bmatrix} R_t & T_t \\ 0 & 1 \end{bmatrix} P^{t-1}, \quad (8)$$

where the points are expressed in homogeneous coordinates, R_t represents the 3x3 rotation matrix and T_t represents a 3x1 translation vector. The pose can thus be estimated by finding the optimal transformation matrix which minimizes the distance between the two sets of 3D points after transformation. Although elegant, the solution of the ego motion is a typical non-linear least squares problem which is highly sensitive to noise. Several existing approaches can minimize or remove noisy data from the system at different points. A widely used technique is the Iterative Closest Point algorithm (Chen,1991) which is effectively applied in matching point cloud data by iteratively searching for the nearest neighbours for each point. Another popular method is the Random Sample Consensus which is designed to cope with large percentages of outliers in the data (Fischler,1981) and can be

applied to iteratively estimate the rotation and translation by using a subset of 3D points which produce the maximum number of inliers.

Directly matching the point clouds generated by the lidar sensor cannot produce accurate results because of the non-uniform sampling technique of the rotating head, so most authors are adapting their methods to search for suitable geometric primitives within the point clouds and use them as features for further matching. Other types of approaches try to estimate the geometric primitives by projecting the point clouds onto a 360 degree panoramic image and use it to find robust features for matching. However, the autonomous vehicle does not always encounter regularly shaped manmade objects and most of the time when driving on open roads the surrounding objects are of natural origin. This relative scarcity of geometric primitives in the point-cloud data can render most of the geometrically based matching algorithms ineffective since they discard a lot of otherwise useful information.

3.2 Proposed method

We are guided by the idea that no information from the sensors should be discarded and as such, the whole lidar point cloud should be used as a single feature for pose estimation. Since the objective in our project is SLAM with additional object detection within the built environment model, we adopt the occupancy map as a feature and use what information is available from the past measurements for registration. Among other benefits, this also makes the system design feasible for real-time application. From the experimental runs of the vehicle and the acquired point clouds we can observe that the car is moving in a relatively flat environment (low absolute road grade compared to the range of the sensor). The change in elevation between two consecutive laser scans falls below the noise threshold of the sensor. This motivates us to assume that the occupancy of the environment can be modelled using a flat two dimensional map, an important simplification to the pose estimation problem which brings higher accuracy and fast execution times.

The algorithm starts by finding the ground plane, i.e. the 3D plane on which most of the road surface is laid on. The flat world assumption dictates that any difference of the estimated ground plane and the world plane ($z=0$) is due to sensor rotation. This can happen because of the dynamics of the vehicles' suspension during linear or lateral accelerations and most notably while passing speed bumps or potholes.

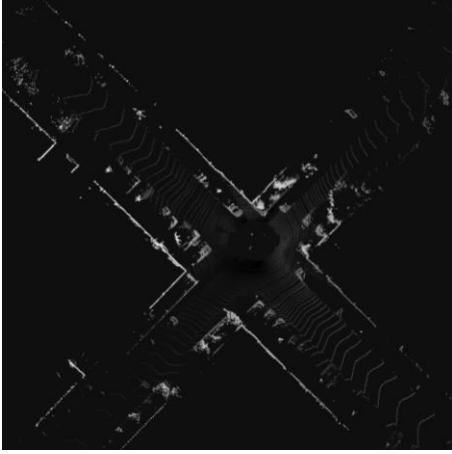


Figure 2. Example of the initial occupancy map, the black background is assumed to be free ($p=0$)

We use an iterative plane fitting algorithm on the raw point cloud data to select the three points that best explain the road surface. It is based on the paradigm of RANSAC in a way that in each iteration a random subsample of points is used to generate a plane equation for which the average distance of all other points is computed and the subset with the lowest average distance (highest number of inliers) is selected. From the list of inliers P_{in}^t of this optimal subset, a new plane is fitted in a least squares sense. The point cloud is then “rectified” relative to this ground plane by applying the inverse rotation relative to the estimated ground normal.

The next step is the projection of the rectified point cloud on the world plane to produce the initial occupancy map. We accumulate the height of each 3D point into the respective occupancy grid cell and produce a probability of occupancy based on the average height of points over that location. Points with height greater than 3m are assumed to have a probability of 1 and points in between are scaled respectively, Fig.2. Thus, we obtain an orthographic projection of the environment in a form of a top view. Vehicle rotation will produce rotation of the features on the map, and vehicle translation will shift the rows and columns of the map. One can clearly see the actual change in rotation and position of features on Fig.3. where the initial occupancy map is compared with the occupancy map produced after 500ms of driving.

We will focus on this domain of imagery to estimate the current pose of the vehicle using standard image registration techniques. The aim is to estimate the rotation and translation change between two occupancy maps built from the sensor data of two consecutive positions. We adopt the widely used technique of Phase-Only Correlation (POC) (Nagashima, 2007) which naturally decouples the

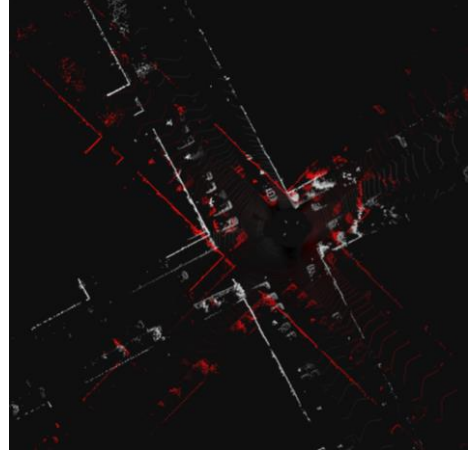


Figure 3. Comparison of two occupancy maps with temporal difference of 500ms (red colour now codes the past information, same as Fig.2)

rotation estimation from the translation estimation in a two step approach. The input occupancy maps are transformed using the 2D DFT

$$M_{u,v}(T) = \sum_{i,j} m_{i,j}(T) e^{-j2\pi(ui+vj)} \quad (9)$$

$$M_{u,v}(T-1) = \sum_{i,j} m_{i,j}(T-1) e^{-j2\pi(ui+vj)},$$

where their respective amplitude spectra $|M_{u,v}(T)|$ and $|M_{u,v}(T-1)|$ are shift-invariant and thus can be used for rotation estimation. In order to directly estimate the rotation change we further take the log of each spectra and transform it in polar coordinates ($M_T^{\rho,\theta}$), thus the rotation estimation boils down to shift estimation. This is easily computed using the 2D convolution of these two images using the normalized cross-power spectrum

$$R(k) = \frac{M_T^{\rho,\theta}(k) \overline{M_{T-1}^{\rho,\theta}(k)}}{|M_T^{\rho,\theta}(k) \overline{M_{T-1}^{\rho,\theta}(k)}|}, \quad (10)$$

where $\overline{M_{T-1}^{\rho,\theta}(k)}$ is the complex conjugate of the polar log spectrum of the occupancy map at time $T-1$. The phase-only correlation is defined by the inverse discrete Fourier transform of (10). If the two input images are the same, then the POC function is the Kronecker delta function and the more the two images differ the more the peak height reduces and there is an apparent shift in the actual position of the peak. Peak height in the POC function is a good measure of the similarity of the two images and the position of the peak is proportional to the angle of

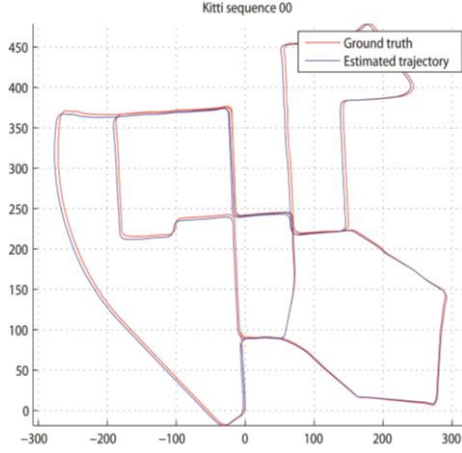


Figure 4. Estimated trajectory vs. trajectory recorded using GPS/IMU for KITTI sequence 00, scale in [m].

rotation in the pose of the vehicle. In our experiments we estimate the peak of the POC function by parabolic fitting and thus estimate the rotation of the vehicle with sub “pixel” accuracy. Once the rotation has been estimated, the old occupancy map is rotated to match the current. The remaining difference, the shift of the two maps, is due to the forward translation of the vehicle which is again estimated similarly using the POC function from equation (10). It is important to note that we use a weighting function in a form of a low pass filter for the Fourier coefficients in order to reduce the effect of lidar noise introduced in the measured points and the presence of moving objects in the scene.

The output of the spectral matching is the yaw angle delta of the vehicle between two consecutive sensor measurements and the magnitude of the translation vector in 2D space. In order to predict the actual X,Y position of the vehicle and its exact trajectory we multiply the translation magnitude by the cosine and sine of the yaw delta and accumulate the results over time

$$\theta_T = \sum_{i=1}^T \theta_i$$

$$\begin{aligned} x_T &= x_{T-1} + Trans * \cos(\theta_T) \\ y_T &= y_{T-1} + Trans * \sin(\theta_T), \end{aligned} \quad (11)$$

where Trans is the estimated translation change between two consecutive scans.

This information is fed back to the mapping equation (6) as part of the measurement z_T in order

to correctly project the lidar points on the global occupancy map of the environment. An example of a computed trajectory after several minutes of driving

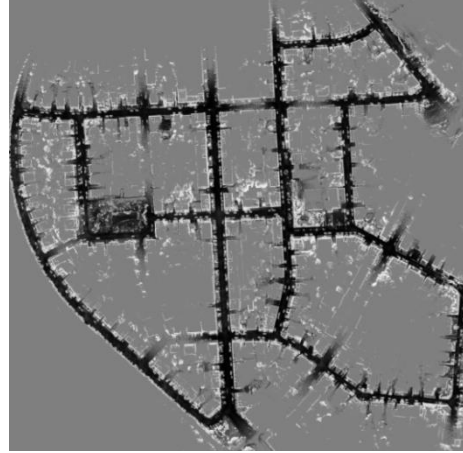


Figure 5. Estimated occupancy map for KITTI 00

a loop through a public road can be seen on Fig.4, and the resulting occupancy map that has been generated on fig.5.

4 EXPERIMENTS AND RESULTS

For validation we use the raw data streams provided by the lidar recordings from the KITTI dataset, and perform our mapping and registration analysis. We chose this particular dataset as it is currently the most comprehensive study about autonomous vehicles driving through public roads. The experimental dataset contains 21 recordings from driving the vehicle through urban, rural and highway roads. These recordings were made with the rotating lidar and two stereo camera pairs. We only used the data from the lidar which is rotating at 10Hz providing an aggregated point cloud every 100ms. Each point of the point cloud is defined with X,Y,Z Cartesian coordinates and a reflectance index. Additionally, a 6DOF pose matrix is given for each time instance. We will compare our trajectories to the GPS poses in order to measure the accuracy of the pose estimation, but since there is currently no ground truth data available for evaluating the occupancy mapping system, the map accuracy will only be measured qualitatively.

Our estimated odometry poses contain information for 3DOF changes of the vehicle. We use the method for evaluation suggested by the authors of the KITTI dataset in order to compare the accuracy of the estimated trajectories, i.e. we compute the average rotation and translation errors for every segment of length 100,200... 800m. For the sequences which have GPS ground truth data available, {0..10}, we report an average 3DOF rotation error of 0.00380 deg/m and average 3DOF translation error of 0.2904% measured as an average

differences between the starting and ending poses for each sub-segment of length 100m to 800m using the distance metrics as follows:

$$\begin{aligned} d(\theta_1, \theta_2) &= \min(2\pi - |\theta_1 - \theta_2|, |\theta_1 - \theta_2|) \\ \Delta\theta_i &= d(\theta_i, \theta_{i+offset}), \\ offset &\in \{100m, 200m, \dots, 800m\} \\ RotError &= \frac{1}{N} \sum_i^N d(\Delta\theta_{i,GT}, \Delta\theta_{i,EST}), \end{aligned} \quad (12)$$

where d is the smallest distance between two angles, i is the start of each sub-trajectory and N is the total number of sub-trajectories evaluated. For measuring the error in the Yaw angle, we extract the Yaw from each pose matrix of the ground truth and input it into equation (12). The 3DOF translation error is simply the average difference of the L_2 norms of each start and end position for the ground truth and estimated sub-trajectories.

We also uploaded our results on the test server provided by the authors of the dataset to evaluate how this approach compares against other 6DOF algorithms. The 6DOF pose errors measures the angular and translational difference of the start and end pose matrix P_i in 3D :

$$d(P_1, P_2) = P_2^{-1}P_1 \quad (13)$$

Our 6DOF pose matrices are constructed by transforming the three Euler angles and the 2D translation vector into a 3x4 matrix using the estimated Yaw angle and zeros for the roll and pitch, also, we use zero value for the height. Hence is the expected drop in accuracy measured using the test server of the KITTI dataset.

Table 1. holds a summary for the accuracy of the results obtained with our algorithm compared to the other methods. The entire table and other information about the methods can be found at (KITTI,2015), however, in this extract we included the top performing methods by means of translation error and one of the rare methods based solely on lidar point cloud data “pcl-ndt-gicp”. As expected, our approach has mediocre accuracy when tested on the full 6DOF benchmark with the missing non estimated data, scoring 1.89% average translation error and 0.0083 deg/m average rotation error. However, the 3DOF poses that we estimate score the highest accuracy on the list for translation error.

We further investigated the robustness of our method by adding two types of noise to the point clouds. In the first experiment, the data is polluted with additive white Gaussain noise in all of the three spatial dimensions. The standard deviation of the distribution is increased within reasonable ranges

Table 1: Average rotation and translation errors in 6DOF for the test sequences of the KITTI dataset

Method	Terr.	Rerr.	Exec. time	Environ.
V-LOAM	0.75%	0.0018	0.3s	4xCPU
LOAM	0.88%	0.0022	1s	2xCPU
SOFT	1.03%	0.0029	0.1s	2xCPU
Cv4xv1-sc	1.09%	0.0029	0.145s	GPU
...				
PROPOSED 3DOF	0.29%	0.0038	0.05s	GPU
PROPOSED 6DOF	1.89%	0.0083	0.05s	GPU
pcl-ndt-gicp	2.02%	0.0083	2s	10xCPU

[5-100cm] simulating point-clouds from a low-end laser scanner. In the second experiment we have kept the original points from the lidar intact only we adding new points which simulate erroneous data i.e. outliers which might be produced from other sensors. The rate of outlier pollution, again, was increased within reasonable ranges [2.5-90%].The resulting 3DOF rotation and translation errors for the KITTI dataset are measured as previously described. We observed that the proposed method is able to cope well with large amounts of both additive noise and the presence of outliers. The translation error seems to sharply increase once an additive error of more than 70cm is added to the lidar data or once there are more than 60% outlier points. This robustness is due to the nature of the spectral matching pose estimation.

Our GPU implementation has an execution time which can keep up with the lidar data. The algorithm is running at around 20fps on a mid-range graphics card. The registration of the occupancy maps consumes around 30-40ms and the rest is spent on the RANSAC and fitting for the ground plane estimation (10-20ms).

5 CONCLUSION

We proposed a feedback loop approach for SLAM by using the probabilistic occupancy map model. By simplifying the pose estimation problem in the 3DOF domain of the occupancy map we have managed to achieve high accuracies for both translation and rotation estimation. The resulting trajectories correspond very well to the orthographic projections of the path the vehicle is taking and the built maps accurately reflect the occupancy

situation. By avoiding the time consuming and often unreliable stereo video feature matching approach we managed to localize the vehicle using only the laser scanner point clouds in their entirety as a single feature.

However, the laser scanner produces point clouds that are oftentimes subjected to clearly visible rolling shutter effect. Few authors in the past have pointed out this problem when trying to use the raw point clouds as input for odometry, and different de-warping techniques have been used in order to produce an accurate image of the environment. This is done relying on additional sensors for motion prior which in our project were not fully available. We demonstrated that by using the warped point clouds provided by the KITTI dataset the occupancy map registration algorithm can produce accurate enough results for the purpose of mapping and later object detection of the autonomous vehicle. We point reader to observe a detailed crop from one of the built occupancy maps on Fig.1. and also to check the integrity of the built map shown on Fig.5. The main drawback of our method is an actual result of the simplification of the problem and can happen when the vehicle crosses its own path over a bridge. The method is currently unable to put the height difference into the occupancy map.

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