

# *Tabling as a Library with Delimited Control*

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## Abstract

Tabling is probably the most widely studied extension of Prolog. But despite its importance and practicality, tabling is not implemented by most Prolog systems. Existing approaches require substantial changes to the Prolog engine, which is an investment out of reach of most systems. To enable more widespread adoption, we present a new implementation of tabling in under 600 lines of Prolog code. Our lightweight approach relies on delimited control and provides reasonable performance.

*KEYWORDS:* tabling, tabulation, delimited continuations, Prolog, logic programming

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## 1 Introduction

Tabling is one of the most widely studied extensions to Prolog because it considerably raises the declarative nature of the language. Tabling takes away the sensitivity of SLD resolution to rule and goal ordering, and allows a larger class of programs to terminate. As an added bonus, the memoisation that is done by the tabling mechanism may drastically improve performance in exchange for more memory.

Given all these advantages, it may come as a surprise that many Prolog systems still do not support tabling. The reason for this is that existing implementations, such as those of Yap and XSB, require pervasive changes to the Prolog engine. This is a substantial engineering effort that is beyond most systems (Santos Costa et al. 2012).

Several works have already attempted to tackle this problem. Through the foreign function interface, Ramesh and Chen (1994) extend Prolog with tabling primitives implemented in C. A complicated program transformation introduces calls to these C routines at the appropriate points in tabled predicates. More recently, Guzmán et. al. (2008) have addressed the performance bottlenecks of Ramesh and Chen's approach. But while their improvement is successful in terms of performance, it does require lower-level C primitives, changes to the WAM's memory management, and an even more complicated program transformation. These changes further increase

the cost of porting and maintaining the mechanism, and the development effort cannot be amortised over other features. Hence, the approach does not lower the threshold for adopting tabling.

Extension tables (Fan and Dietrich 1992) provide a tabling mechanism that is implemented directly in Prolog. However, the approach cannot achieve satisfactory performance as suspended goals are always re-evaluated. The initial implementation used the `assert` and `retract` predicates for database manipulations. These predicates are notorious for their slow performance. A later version moved the data structures to C, but did not change the inherent recomputation behaviour.

Santos Costa et al. (2012) point out that “*Making it easy to change and control Prolog execution in a flexible way is a fundamental challenge for Prolog.*”. We argue that delimited control, a language construct for manipulating a program’s control flow, does exactly that. Schrijvers et. al. (2013) show that the impact of delimited control on the WAM is minimal. On top of that, the development effort of delimited control can be amortized over the range of high-level language features they enable, such as *effect handlers* (Plotkin and Pretnar 2013).

We show how delimited control can be used for a lightweight tabling mechanism. Both the tabling control flow and data structures are written entirely in Prolog enhanced with delimited control. It does not require deep custom changes to the Prolog engine, complicated program transformations, or meta-interpretation. As such our mechanism demystifies many aspects of implementing tabling.

Compared to existing state-of-the-art systems, our system needs more attention in terms of performance, but this does not outweigh the gain in flexibility: we bring tabling much closer to the masses. In contrast with extension tables, our approach does not require recomputation of suspended goals. Our tabling implementation is available at <http://users.ugent.be/~bdsouter/tabling/>.

## 2 Background: Delimited Continuations

Delimited control (Felleisen 1988; Danvy and Filinski 1990) is the key ingredient of our lightweight tabling approach. This technique originates in functional programming and was recently introduced in Prolog by Schrijvers et al. (2013; 2013) in the form of two built-ins: `reset/3` and `shift/1` for delimiting and capturing the continuation respectively.

- `reset(Goal, Cont, Term1)` executes `Goal`. If `Goal` calls `shift(Term2)`, its further execution is suspended and unified with continuation `Cont`. A continuation is an unspecified Prolog term, which can be resumed using `call/1`. It can be called, saved, copied and compared like any other term, but it is opaque: from its representation we cannot determine anything about the actual goals it represents.
- `shift(Term2)` unifies the remainder of `Goal` up to the nearest call to `reset/3` (i.e., the delimited continuation) with `Cont`, and its return value `Term2` with `Term1`. Finally, it returns control to just after the `reset/3` goal.

We start with an example that does not call the continuation.

```

p :-
  reset(q,Cont,Term1),
  writeln(Term1),
  writeln(Cont),
  writeln(end).
q :-
  writeln('before shift'),
  shift('return value'),
  writeln('after shift').
?- p.
before shift
return value
[$cont$(785488,[])]
end

```

This example shows that `shift/1` instantiates the last two arguments of `reset/3`. `Cont` represents the `writeln('after shift')` goal in the context of the activation of the clause for `q/0`. But since the continuation is not called, this goal has no effect. `Term1` is unified with the term `'return value'`. The execution continues after the `reset/3`.

The following example shows what happens if the continuation is called:

```

p :-
  reset(q,Cont,Term1),
  writeln(Term1),
  call(Cont),
  writeln(end).
q :-
  writeln('before shift'),
  shift('return value'),
  writeln('after shift').
?- p.
before shift
return value
after shift
end

```

### 3 Shallow Program Transformation

In our approach, tabled predicates require no special notation, nor any syntactic analysis of the predicates being tabled. Predicates are written in the usual way, and transformed by a shallow program transformation.

```

:- table p/2.

p(X,Y) :- p(X,Z), e(Z,Y).
p(X,Y) :- e(X,Y).

```

Fig. 1. Running example:  
transitive closure.

```

p(X,Y) :- table(p(X,Y),p_aux(X,Y)).

p_aux(X,Y) :- p(X,Z), e(Z,Y).
p_aux(X,Y) :- e(X,Y).

```

Fig. 2. Result of the transformation.

The use of tabling is illustrated in Figure 1. Predicate `p/2` computes the transitive closure of the `e/2` relation. The `table`-directive indicates that `p/2` will be tabled. Predicates without that directive are resolved using standard SLD-resolution.

The `table/1` directive performs a very shallow program transformation, the result of which is shown in Figure 2. This transformation introduces `p_aux/2`, which we call the *worker* predicate, and `p/2`, the *wrapper* predicate. The wrapper predicate is defined in terms of the tabling predicate `table/2`, which care of tabling that call fully dynamically. The next section explains how `table/2` can be implemented directly in Prolog.

### 4 Implementation of the Tabling Library

This section explains how we implement tabling as a library.

```

table(Wrapper,Worker) :-
  get_table_for_variant(Wrapper,Table),
  table_get_status(Table,Status)
  ( Status = complete ->
    get_answer_from_table(Table,Wrapper)
  ;
  ( exists_scheduling_component ->
    run_leader(Wrapper,Worker,Table),
    get_answer_from_table(Table,Wrapper)
  ;
  run_follower(Status,Wrapper,Worker,Table)
  )
).

```

Fig. 3. The `table/2` predicate.

#### 4.1 The `table/2` Predicate

Thanks to the shallow program transformation, the `table/2` predicate intercepts every call to a tabled predicate. Figure 3 shows that `table/2` retrieves the `Table` data structure for the given `Wrapper` call pattern. There is one table for every distinct call pattern encountered so far; if the current call pattern has not been encountered before, `get_table_for_variant/2` allocates a fresh data structure for it.

Then `table/2` switches on the `Table`'s status. If the status is `complete`, it means that all answers for the `Wrapper` call pattern are already available in the table. The call is then answered by consuming the answers with the `get_answer_from_table/2` predicate.

Otherwise, we either start collecting answers (`run_leader/3`), or we are already in the process of collecting answers and simply proceed (`run_follower/4`). The call that initiates answer collection is called the *leader*. A leader is a call to a tabled predicate that has only non-tabled ancestors in the dynamic call graph. Other calls to tabled predicates during answer collection are called *followers*. Every follower has a leader as its ancestor. The leader and its followers make up a *scheduling component*. Multiple scheduling components can occur during program execution.

##### Example 1

Consider the top-level call `?- p(X,Y).` for our running example. Then `p(X,Y)` clearly is the leader of a new scheduling component. The recursive call `p(X,Z)` in the first clause constitutes a follower in its scheduling component.

*The Leader* The leader, defined in Figure 4, takes responsibility for computing all the answers of its scheduling component. To quickly identify whether there currently is a leader, we use a global non-backtrackable variable. The predicates `exists_scheduling_component/0` and `create_scheduling_component/0` check and set this variable. The predicate `unset_scheduling_component/0` unsets it.

The job of the leader consists of two tasks: 1) it starts computing the answers of the scheduling component with `activate/3`, and 2) it computes the least fixpoint for the whole scheduling component with `completion/0`.

```
run_leader(Wrapper,Worker,Table) :-
  create_scheduling_component,
  activate(Wrapper,Worker,Table),
  completion,
  unset_scheduling_component.
```

Fig. 4. Handling the leader call.

```
run_follower(fresh,Wrapper,Worker,Table) :-
  activate(Wrapper,Worker,Table),
  shift(call_info(Wrapper,Table)).

run_follower(active,Wrapper,Worker,Table) :-
  shift(call_info(Wrapper,Table)).
```

Fig. 5. Handling a follower call.

*Followers* Followers, defined in Figure 5, have fewer responsibilities than the leader. If the table of the follower is `fresh`, i.e. it is the first time the call pattern occurs, then the follower `activates` the answer computation. Subsequently, it yields control with `shift/1`; this is explained in more detail in the next subsection. If the table is already `actively` collecting answers, the follower immediately yields control.

#### 4.2 Activation and Delimited Answer Computation

When a call pattern is encountered for the first time, the computation of its answers is activated with the predicate `activate/3`. This predicate, defined in Figure 6, alters the table status from `freshly` allocated to `active` and puts the `Worker` to work with the auxiliary `delim/3` predicate. Note that a failure driven loop is used to backtrack over all the alternatives of `Worker`.

```
activate(Wrapper,Worker,Table) :-
  table_set_status(Table,active),
  (
    delim(Wrapper,Worker,Table),
    fail
  ;
  true
  ).
```

Fig. 6. Activation.

The body of a tabled predicate  $p/n$  is actually executed by predicate `delim/3`, defined in Figure 7. This predicate runs  $p/n$ 's `Worker` in the context of a `reset/3`. If the `Worker` succeeds normally, the answer is added to the table with `store_answer/2`. However, if the `Worker` calls a tabled predicate  $q/m$  — with either the same or

```
delim(Wrapper,Worker,Table) :-
  reset(Worker,Continuation,SourceCall),
  ( Continuation == 0 ->
    store_answer(Table,Wrapper)
  ;
  SourceCall = call_info(_,SourceTable),
  TargetCall = call_info(Wrapper,Table),
  Dependency = dependency(SourceCall,Continuation,TargetCall),
  store_dependency(SourceTable,Dependency)
  ).
```

Fig. 7. Delimited execution.

a different call pattern as  $p/n$  — then `Worker` does not terminate normally. The reason is that the  $q/m$  call is a follower, and `run_follower/4` always ends in a `shift/1` without producing an answer. Instead the `Worker` suspends, capturing the remainder in `Continuation`.

*Example 2*

Consider the following clause from our running example:

```
p_aux(X,Y) :- p(X,Z), e(Z,Y).
```

The worker `p_aux(X,Y)` for the call `p(X,Y)` immediately suspends at the recursive call `p(X,Z)` with `Continuation = e(Z,Y)`.

Through this suspension, we bypass the regular depth-first execution mechanism of Prolog and avoid its potential non-termination. We replace the depth-first search by the least fixpoint computation of the `completion` phase. For this purpose, we record the suspended computation in the form of a `dependency/3` structure. This structure expresses that given an answer for the  $q/m$  call, one may obtain answers for the  $p/n$  call by resuming the suspended continuation. We name  $q/m$  the *source call* and  $p/n$  the *target call*. For the source call, it is sufficient to hold on to the `SourceTable` to be able to retrieve an answer later. For the target call, we need the `Wrapper` in addition to the table, as the `Wrapper` contains the partial answer that the continuation will instantiate. This explains the form of the `dependency/3` structure, which is stored in the table of the source call to be triggered whenever a new answer is added.

*Example 3*

The dependency for our example above expresses that, given an answer for `p(X,Z)`, we may obtain answers for `p(X,Y)` by executing `e(Z,Y)`. For instance, if we get the answer  $X = a$ ,  $Z = b$  for `p(X,Z)`, and we have the fact `e(b,c)` then we obtain the answer  $X = a$ ,  $Y = c$  for `p(X,Y)`.

*Example 4*

Assume that `e/2` is defined by the facts `e(a,b)` and `e(b,c)`. Then the query `?- p(X,Y)` yields not only the dependency on `p(X,Z)` through the first clause of `p_aux/2` but also the answers `p(a,b)` and `p(b,c)` through the second clause of `p_aux/2`. Since `p(X,Z)` is a variant of `p(X,Y)`, the dependency and the two answers are all associated with the same table.

### 4.3 Completion

The completion phase, defined in Figure 8, computes the fixpoint over all answers and dependencies of the scheduling component. Just like Datalog’s semi-naive approach (Ceri et al. 1989), our implementation tries to avoid unnecessary recomputation. More code details are available in Appendix C.

We maintain a worklist of all tables for which at least one associated answer has not been fed into at least one associated dependency. This worklist is updated whenever a new answer or new dependency is associated with a table.

Predicate `completion/0` is the driving loop of the completion phase. It repeatedly pops a table from the worklist and calls `completion_step/1` to process answer/dependency pairs that have not yet been combined. When the worklist is empty, the completion fixpoint has been reached. Then `set_all_complete/0` sets the status of every table in the scheduling component to `complete`. Finally `cleanup_tables/0` erases all the dependencies, as they are no longer necessary.

Predicate `completion_step/1` retrieves an unprocessed pair `Answer/Dependency` from the table by calling `table_get_work/3`. It instantiates the source of the dependency with the answer and resumes the dependency's continuation with `delim/3`, binding the variables in the partial answer `Wrapper` along the way. This process may lead to new answers or new dependencies that spur the fixpoint computation on. Here, a failure-driven loop is used to iterate over all answer/dependency pairs.

#### Example 5

Let us consider the completion that follows Example 4. There is one entry in the worklist: the table for call variant `p(X,Y)`. This table has two unprocessed pairs:<sup>1</sup>

$$\begin{aligned} & p(a,b) / \text{dependency}(p(X,Z), e(Z,Y), p(X,Y)) \\ & p(b,c) / \text{dependency}(p(X,Z), e(Z,Y), p(X,Y)) \end{aligned}$$

The first pair yields the new answer `p(a,c)` with the help of the fact `e(b,c)`. The second pair yields nothing. The production of a new answer reschedules the table for `p(X,Y)` in the worklist. Yet the second completion round yields no new answers or dependencies and the fixpoint computation terminates with answer set  $\{p(a,b), p(b,c), p(a,c)\}$  for call `p(X,Y)`.

### 4.4 The Table Data Structures

The central data structure used by the tabling control flow explained above is the *table*. We maintain one such table per call variant, which can be retrieved from a global repository of all tables. This global repository is implemented in the form of a trie data structure, also known as the call trie, that maps call patterns to tables.

There is a second global data structure, the global worklist, which maintains a simple queue of tables for the algorithm explained in the previous subsection.

<sup>1</sup> We have abbreviated the call information for the sake of clarity.

```

completion :-
  ( worklist_empty ->
    set_all_complete,
    cleanup_tables
  ;
  pop_worklist(Table),
  completion_step(Table),
  completion
  ).

completion_step(SourceTable) :-
  (
    table_get_work(SourceTable, Answer,
      dependency(Source, Continuation, Target)),
    Source = call_info(Answer, _),
    Target = call_info(Wrapper, TargetTable),
    delim(Wrapper, Continuation, TargetTable),
    fail
  ;
  true
  ).

```

Fig. 8. The completion fixpoint.

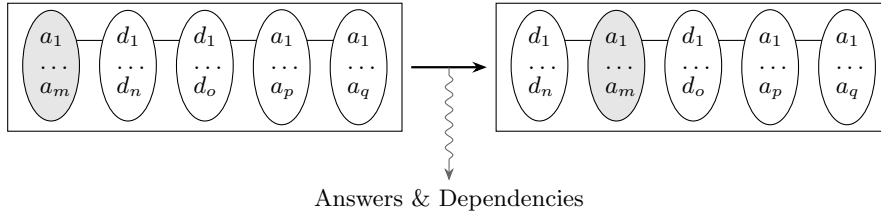


Fig. 9. Combining answers and dependencies in a local worklist.

The table itself consists of two parts: the answer trie and the local worklist:

- The answer trie is where `get_answer_from_table/2` finds its answers. Moreover, the trie allows `store_answer/2` to quickly check whether a newly produced answer has already been computed before, and to only store it in case it has not.
- The local worklist serves the `table_get_work/3` predicate. It retrieves pairs of answers and dependencies that have not been combined before. For this purpose we use a dequeue (i.e., a double-ended queue) that contains answers and dependencies.

The dequeue maintains the invariant that an answer is to the left of a dependency if and only if they have not been combined. New answers are added on the left, because they have not been combined with any dependency yet. New dependencies are added on the right.

For performance reasons, the dequeue batches consecutive answers into a single entry on insertion; the same happens to consecutive dependencies. Every batch contains homogeneous elements (either answers or dependencies) and is implemented as a list — the position of the elements in the list is insignificant. Batches of the same type are not merged if they become adjacent during the combination of answers and dependencies. Doing so would reduce the number of swaps, but at the cost of merging the lists.

The `table_get_work/3` predicate retrieves a batch of answers immediately to the left of a batch of dependencies, swaps their positions and yields the elements of their Cartesian products for processing. Dependencies and answers that are created by the combination are also sent to the appropriate tables. A single step of this process is illustrated in Figure 9. The solid arrow denotes the transformation of the local worklist. The wavy line denotes the emission of new answers and dependencies that are generated by the completion step. The answers in the gray ellipse have been added to the local worklist, and will eventually move to the right of all dependencies.

*Implementation Support* The key Prolog implementation support for these tables are mutable terms and non-backtrackable mutations (Appendix B). We also use a global variable for the table repository. These features are widely available. The non-backtrackable nature is essential to retain the collected answers and dependencies across disjunctions.



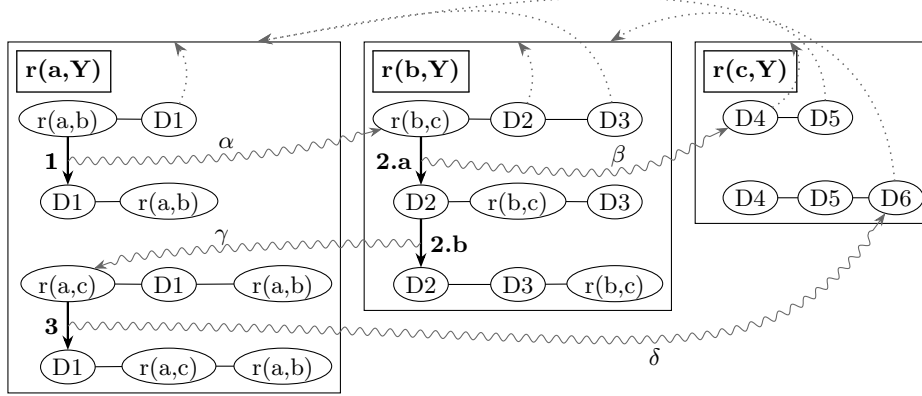


Fig. 10. Illustration of the computation of  $r(a,Y)$ .

#### 4.5 Completion of a Double Recursive Call

##### Example 6

Consider a variant of our running example where the recursive clause is replaced by:

$$r(X,Y) :- r(X,Z), r(Z,Y).$$

Figure 10 illustrates the computation of  $?- r(a,Y)$ . Each table is a rectangle. The consecutive states of its worklist are shown from top to bottom. A dotted arrow shows the target of a dependency. The solid and wavy lines are as in Figure 9. In the explanation, the labels of the completion steps in the figure are written between parentheses. The call  $?- r(a,Y)$  gives rise to the dependency  $D1 = \text{dependency}(r(a,Z), r(Z,Y), r(a,Y))$  and the answer  $r(a,b)$  (left rectangle).

*Iteration 1* In the first iteration of completion (1), the answer is fed into the dependency (wavy arrow  $\alpha$ ), hence  $D1$  and  $r(a,b)$  are swapped. This exposes the call  $r(b,Y)$  (middle rectangle). For this new call we immediately obtain the dependency  $D2 = \text{dependency}(r(b,Z1), r(Z1,Y), r(b,Y))$  and the answer  $r(b,c)$ . We also record dependency  $D3 = \text{dependency}(r(b,Y), \text{true}, r(a,Y))$  between  $r(b,Y)$  and  $r(a,Y)$ . The **true** in  $D3$  represents the empty continuation: finding an answer for  $r(b,Y)$  gives an answer for  $r(a,Y)$  for free!

*Iteration 2* During the second iteration, we feed the answer  $r(b,c)$  into the two dependencies  $D2$  (2.a, wavy arrow  $\beta$ ) and  $D3$  (2.b, wavy arrow  $\gamma$ ).

- $\beta$  In the  $D2$  case, we expose a new call  $r(c,Y)$  (right rectangle) yielding no direct answer, but a new dependency  $D4 = \text{dependency}(r(c,Z2), r(Z2,Y), r(c,Y))$  and a derived dependency  $D5 = \text{dependency}(r(c,Y), \text{true}, r(b,Y))$ .
- $\gamma$  In the  $D3$  case, we obtain the new answer  $r(a,c)$  for the top-level call.

*Iteration 3* During the third iteration (3), we feed the new answer into dependency D1 (wavy arrow  $\delta$ ). This yields the call  $r(c, Y)$  and the dependency  $D6 = \text{dependency}(r(c, Y), \text{true}, r(a, Y))$ .

*The fixpoint* Finally, there is no more work to be done: at the bottom of each rectangle, all  $D_i$  are left of all answers. Hence, the fixpoint comprises the answer table  $\{r(a, b), r(a, c)\}$  for the call pattern  $r(a, Y)$ , the answer table  $\{r(b, c)\}$  for the call pattern  $r(b, Y)$  and the empty answer table for  $r(c, Y)$ .

## 5 Evaluation

### 5.1 Implementation Effort

Table 1 summarizes the implementation effort in lines of Prolog (LoC). The control flow shown in this paper comprises 60 LoC, or less than 11% of the overall effort. The majority goes to the two kinds of data structures, the tries (40%) and the worklists (45%). Adding 25 lines of glue code, this amounts to an implementation for 577 Prolog LoC.

### 5.2 Performance

While raw efficiency is not the main objective of our lightweight implementation, it is nevertheless important to achieve a reasonable performance compared to the existing state-of-the-art tabling systems. In order to evaluate this, we compare our implementation in hProlog 3.2.38 against XSB 3.4.0 (Swift and Warren 2012), B-Prolog 8.1 (Zhou 2012), Yap 6.3.4 (Santos Costa et al. 2012) and Ciao 1.15-2731-g3749edd (Hermenegildo et al. 2012) on a number of benchmarks.<sup>2</sup> Table 2 summarizes the results (in ms) obtained on a Dell PowerEdge R410 server (2.4 GHz, 32 GB RAM) running Debian 7.6. In parentheses, we have indicated the maximum resident set size (RSS) in megabytes and the proportion of hProlog to XSB.

*Discussion* The XSB system is the reference system for tabling; it has invested most time and resources in the development of its tabling infrastructure. We see that it is 8 to 38 times faster than our implementation, but 45 to 78 times faster for two

<sup>2</sup> The description and code of the benchmarks can be found at <http://users.ugent.be/~bdsouter/tabling/>.

Category	LoC	Category	LoC
Control flow	60	Completion Worklists	259
Call and Answer Tries	233	Miscellaneous	25
Total	577		

Table 1. Code size in lines of code.

outliers (path right last: binary tree 18 and 10k pingpong). It has a maximum RSS that is up to 7 times as large, and 14 times for path double first 500. In general, standard trie-based structures overload the memory because representation sharing is poor. This has been addressed by Raimundo and Rocha (2011).

Since XSB does not support big integers, it was not meaningful to run the Fibonacci benchmark, recorded as O/F (for overflow). This is a case in point for wider tabling support in other systems: often we need both tabling and other non-standard features.

B-Prolog is only half as fast as XSB on many benchmarks, but is architecturally different: BProlog implements linear tabling and uses hash tables instead of tries. Moreover, in several cases B-Prolog is notably slower than XSB (i.e., n-reverse) and even much slower than our own implementation (recognize, shuttle, ping pong). Yet, unlike XSB, B-Prolog does support big integers and is substantially faster than our approach for the fib benchmark. All in all the results are mixed and point out several weaknesses in the B-Prolog implementation compared to our all Prolog implementation.

The Yap tabling implementation, which is based on that of XSB, is clearly the fastest: the underlying engine is much faster (Rocha et al. 2000). It outperforms our approach on all benchmarks, and the other systems on most. Many benchmarks take less than 1 ms, rounded down to 0 ms, hence the factor  $\infty$  in the table.

The performance of Ciao lies between that of XSB and B-Prolog. Performance of our implementation is within a factor 4 to 14 of Ciao, with reverse and path right last as outliers. Running the Fibonacci benchmarks is currently not possible, as tabling and bignums currently do not operate together<sup>3</sup>.

*Summary* We consider the performance results of our implementation very reasonable, especially if we take into account the stark contrast between our lightweight pure Prolog implementation and the complex integration in other systems. As part of future work, we think that advances in three areas may positively affect performance. Firstly, continuations are copied with `copy_term/2`. A special-purpose `copy_continuation/2` could do better by exploiting the known structure of these terms. Other applications using delimited control could benefit from this optimization as well. Secondly, we don't statically identify strongly connected components in the scheduling component. Doing so would allow the specialisation of completion. Finally, in contrast with state-of-the art implementations, our tries do not use substitution factoring.

## 6 Related Work

*Delimited Control* While delimited control is well-known in the functional programming world, it has not received much attention in the context of Prolog. Only recently have Schrijvers *et al.* provided an unobtrusive implementation in the WAM

<sup>3</sup> Personal email communication with Manuel Carro.

Benchmark	Size	hProlog	$\frac{\text{hProlog}}{\text{XSB}}$	$\frac{\text{hProlog}}{\text{B-Prolog}}$	$\frac{\text{hProlog}}{\text{Yap}}$	$\frac{\text{hProlog}}{\text{Ciao}}$
<b>fib<sup>a</sup></b>	500	24 (13)	O/F (—)	$\infty$	$\infty$	—
	750	33 (13)	O/F (—)	17	41	—
	1,000	46 (13)	O/F (—)	46	19	—
	10,000	982 (66)	O/F (—)	3	44	—
<b>recognize<sup>a</sup></b>	20,000	205 (73)	26 (1)	0.003	11	4
	50,000	503 (221)	30 (2)	0.001	14	4
<b>n-reverse<sup>a</sup></b>	500	767 (138)	38 (5)	11	15	45
	1,000	2,800 (537)	31 (6)	6	8	34
<b>shuttle<sup>b</sup></b>	2,000	44 (12)	$\infty$ (2)	0.1	$\infty$	9
	5,000	138 (14)	23 (2)	0.08	$\infty$	12
	20,000	582 (29)	24 (4)	0.02	$\infty$	10
	50,000	1,586 (72)	29 (6)	0.01	$\infty$	12
<b>ping pong</b>	10,000	271 (16)	45 (2)	0.07	$\infty$	14
	20,000	490 (28)	35 (4)	0.03	$\infty$	8
<b>path double first loop</b>	50	653 (14)	19 (2)	13	$\infty$	7
	100	4,638 (29)	17 (4)	10	$\infty$	6
<b>path double first</b>	50	162 (12)	27 (2)	15	$\infty$	14
	100	989 (16)	20 (3)	12	$\infty$	10
	200	6,785 (53)	18 (7)	16	$\infty$	10
	500	110,463 (267)	25 (14)	19	$\infty$	14
<b>path right last: pyramid 500</b>	500	1,914 (104)	35 (7)	29	$\infty$	27
<b>path right last: binary tree 18</b>	18	108,662 (4,120)	78 (5)	50	3,461	42
<b>test large joins 2<sup>c</sup></b>	12	3,001 (237)	10 (5)	4	$\infty$	12
<b>joins mondial</b>		6,444 (399)	8 (2)	7	224	6

Table 2. Results of the performance benchmarks.

Source: *a* (Fan and Dietrich 1992) *b* (Demoen and Sagonas 1998a) *c* Yap benchmark suite

(Schrijvers et al. 2013; Schrijvers et al. 2013). In the continuation-passing implementation (Tarau and Dahl 1994) of BinProlog (Tarau 2012) this is even easier. Schrijvers *et al.* also illustrate the power of delimited control by porting various effect handlers (Plotkin and Pretnar 2013) to Prolog. As far as we know, this paper shows the first Prolog-specific application.

*XSB* XSB is the best-known Prolog engine supporting tabling. Its foundation, SLG resolution, has been described by Chen and Warren (1996). Swift and Warren (2012) provide a recent survey. Implementing XSB has required nontrivial changes to the architecture of the WAM. XSB maintains a forest of SLD-trees for a tabled predicate. During the computation, the stack may be frozen several times.

*CAT and CHAT* The CAT is an alternative to the SLG-WAM used in XSB (Demoen and Sagonas 1998a). Rather than freezing memory areas, CAT uses incre-

mental copies to preserve the execution state of suspended computations. CAT’s advantage is that the speed of the underlying abstract machine is not affected for non-tabled execution. CHAT is an improved scheme incorporating some ideas from the SLG-WAM (Demoen and Sagonas 1998b). CAT and CHAT do require changes to the WAM, but acknowledge that the complexity and scope of these changes should be kept limited.

*Linear Tabling* Linear tabling mechanisms (Zhou et al. 2000), which implement the SLDT-resolution strategy, maintain a single execution tree, hence there is the need to steal choicepoints from a former variant call. Each tabled call can be both a producer and a consumer. Similar to our approach, there is no overhead for standard SLD-resolution, but the need for recomputation of subgoals cannot always be avoided. Although simpler than SLG resolution, implementing SLDT still requires the addition of 4 new specifically designed WAM-instructions, a new frame structure and a new data area. Unlike for suspension-based mechanisms, the cut operator works for a class of useful programs.

*DRA* The DRA (Guo and Gupta 2001; Guo and Gupta 2004) has a goal similar to our approach. The technique implements tabled evaluation without stack-freezing. It postpones clauses containing variant calls at runtime, which is similar to our suspension creation. But to implement this technique, Guo and Gupta introduced six new WAM instructions. Compared to XSB, Guo and Gupta’s implementation of DRA has a significantly better space performance, but a worse time performance. The authors cite as sources for XSB’s better time performance that XSB avoids reconstructing the execution environment for applying looping alternatives, and secondly that XSB includes tabling in the compiling stage. Both reasons are equally applicable to our approach.

## 7 Conclusion

In order to enable a more widespread adoption of tabling, we have presented a lightweight implementation of tabling on top of delimited control. In contrast to existing approaches, our approach is implemented entirely in Prolog and requires no deep modifications to the WAM or complex program transformations. While there is obviously a trade-off between the simplicity of the implementation and runtime performance, we believe that the current performance of our approach is reasonable. Of course, there is ample opportunity for improvement.

In the future we would also like to extend our approach with mode-directed tabling (Guo and Gupta 2008; Santos and Rocha 2013). Our initial exploration has shown that this would only require a small change to the trie structure.

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