Effect of solid particle size on the viscosity of a secondary copper smelting slag

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ABSTRACT

Viscosity is one of the most important physicochemical properties during pyrometallurgical operations. In the sub-liquidus regime, an important factor is the presence of suspended solid particles, yet its influence is not well-described in earlier literature, despite the significance of this factor. This project aims to determine the influence of spinel particles ($Zn(Al,Fe)_2O_4$) on the rheology of a multiphase synthetic PbO-SiO_2-ZnO-Fe_2O_3-CaO-Al_2O_3 slag system. Three data sets with a well-controlled methodology and three different spinel sizes (small (13 µm), medium (34 µm) and large particles (76 µm)) were published previously, using a custom-built high-temperature rheometer. This study presents an additional data set of slag viscosity measurements, performed using a different apparatus, the Anton Paar FRS 1800, to verify the consistency of the earlier determined viscosity behaviour. Within this data set, no consistent trend could be found between the predicted wt per cent spinel and the relative viscosity. Therefore, additional quenching experiments were conducted to identify the morphology and experimentally determined volume fraction of the spinel particles in the slag. These measurements revealed a difference in spinel size across the samples and corresponding viscosity behaviour, emphasizing the importance of spinel particle size on slag viscosity. Once the spinel size was taken into account, consistent viscosity results (relative apparent viscosity and flow index) were observed across the two devices. This study confirms that, once all parameters affecting slag viscosity are considered, the viscosity behaviour of a heterogeneous slag can be uniquely determined. The resulting optimised slag viscosity models can be used to predict viscosity before processing, addressing relevant phenomena such as slag tapping, slag foaming and copper droplet settlement.

INTRODUCTION

Viscosity is one of the key physicochemical parameters to control during pyrometallurgical processes. Nowadays, a large amount of viscosity models are available to predict the viscosity of the liquid slag phase. However, the rheology of partially crystallised slags (a suspension, ie a liquid slag matrix with small solid particles suspended in the melt) remains insufficiently understood and a large discrepancy exists across various published works (Sichen *et al*, 2022). Rheological aspects such as the non-Newtonian behaviour of slags containing suspended solid particles are poorly understood, resulting in a low reproducibility of the viscosity data across various studies. A key reason for the scatter on the obtained viscosity data is the lack of control/description of all parameters affecting the final viscosity of a heterogeneous slag. Liu *et al* (2018) reviewed a large number of viscosity studies regarding heterogeneous silicate melts and reported the following parameters of interest: solid particle volume fraction, particle shape and the shear rate. For the particle shape, both the aspect ratio, ie the ratio of the longest axis of the particle to the shortest perpendicular axis and the size were reported. In pyrometallurgical literature, the focus has mainly been on the aspect ratio of the particle as the main morphological parameter (Liu *et al*, 2018). Consequently, the main mode of shear thinning, ie the preferential re-orientation of the particles in the melt with respect to the flow direction, caused by a variation in the shear rate, was described in literature as individual particle orientation. This type of shear thinning has been visualised in Figure 1a. Initially, the particles are randomly oriented. Upon shearing the suspension with an increasing flow rate, the hydrodynamic

force acting on the particles increases, which causes the rotation of the particles around their axis perpendicular to the flow direction. Consequently, the flow lines of the melt are less disturbed, which causes a reduction in the apparent viscosity at large shear rates. Particles with a large aspect ratio can exhibit more of this type of shear thinning compared to equiaxed, symmetrical particles (Mueller, Llewellin and Mader, 2009).

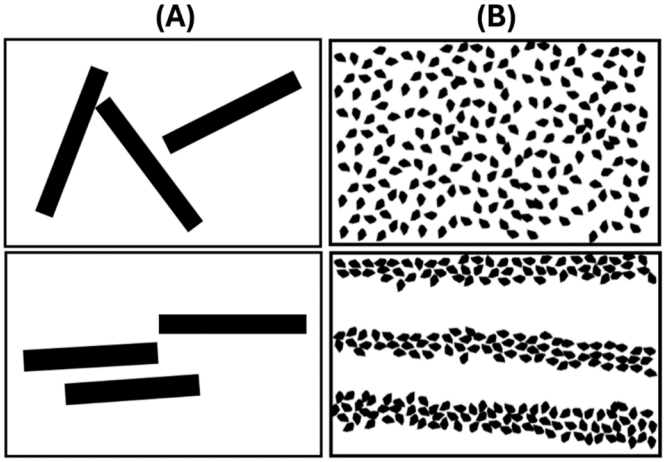

FIG 1 – Illustration of shear thinning, ie the re-orientation of the particles with respect to the flow direction. Top: random orientation, Bottom: preferential orientation with respect to the flow direction. (a): Individual particle orientation (b): Particle-particle orientation.

A second type of shear thinning is the particle-particle orientation, ie the re-orientation of the particles with respect to their closest neighbours. In Figure 1b, at low shear rates and the associated random orientation of the particles, the path of the melt flow lines is largely disturbed. Upon shearing, the particles may group in more closely packed clusters to decrease the disturbance of the melt flow lines (Caricchi *et al*, 2007). The elongated clusters have been observed experimentally by Lyon *et al* (2001) for cold suspensions. Suspensions for which the suspended particles have a larger number of closest neighbours can exhibit this type of shear thinning to a larger extent. Consequently, the particle size will influence the degree of shear thinning associated with particle-particle orientation. Moreover, this mode of shear thinning also explains the observed shear thinning for suspensions containing spherical/equiaxed particles, which cannot show individual particle orientation (Mueller, Llewellin and Mader, 2009; Saito *et al*, 2020).

For slag suspensions, literature commonly does not focus on the particle size. The work of Wright *et al* (2000) is one of the few studies which examined the effect of the spinel size on the viscosity of a CaO-MgO-Al_2O_3-SiO_2 slag. Suspensions with three different spinel sizes were examined: 100–210 μm, 210–440 μm and 440–990 μm. They noted that the quality of their data was insufficient to make conclusions on the effect of particle size on the viscosity.

In our previous work (Vergote *et al*, 2023), the effect of the spinel size was examined for three different spinel sizes: small (13 μm), medium (34 μm) and large particles (76 μm). By employing a custom-built rheometer with quenching possibilities, accurate microscopical examination of the slag as it was during high-temperature viscosity measurement was possible. As a result, three accurate data sets were obtained from which the following conclusions were obtained:

1. The viscosity increases for decreasing spinel size at similar solid phase fractions.
2. Fully liquid samples at the spinel saturation composition showed Newtonian behaviour. Therefore, it is confirmed that no additional spinel particles located at the interface of the crucible and spindle (Vergote *et al*, 2021) affected the bulk slag viscosity measurement.
3. All examined samples containing spinel particles, even at low vol per cent of 1.8 per cent, showed shear thinning behaviour. The amount of shear thinning increases for decreasing spinel size.

These conclusions were similar to the ones obtained from experiments with magmas containing solid particles (Del Gaudio, Guido and Taddeucci, 2013). Yet, additional viscosity data for slags relevant

for the copper recycling industry are required to further establish the accuracy of our previous study. Therefore, this work examines the viscosity for slags with a relevant composition, while employing a different slag preparation and viscosity apparatus. This cross-check is required due to the low availability of accurate relevant viscosity data in literature, for which all parameters are well-described.

METHODOLOGY

Slag selection and preparation

An earlier work by Vergote *et al* (2021) identified the interaction between the slag and the alumina labware as the main experimental error for slag viscosity measurements. In this work, liquid lead-silicate based slag compositions were reported which were compatible with alumina, ie resulted in a low degree of interaction with crucible and spindle. One such composition (Slag 1, Table 1) was used in this work as the liquid slag matrix to prepare the heterogeneous slag-spinel samples. For this slag composition, it was confirmed that the interaction of the alumina spindle and crucible during the viscosity measurement is negligible. This slag is predicted by FactSage™ 8.3 (Private database UQPY 2020) to be in equilibrium with spinel (with composition 'Spinel' in Table 1) at 1200°C (Bale *et al*, 2016). A similar tie line approach as described in Vergote *et al* (2023) was employed in this work. This approach includes a constant liquid viscosity of the slag matrix, with a composition fixed at the slag-spinel equilibrium, while uniquely varying the amount of spinel particles in the system across the various samples in the data set. Therefore, the influence of the solid particles on the overall slag viscosity can be determined more accurately.

TABLE 1

Bulk slag and predicted spinel composition (wt%) for the considered samples for the slag-spinel suspensions. Slag liquidus temperature (T_{liq}) and the corresponding amount equilibrium weight fraction spinel (Sp) particles at 1200°C were both calculated using FactSage (Private database UQPY 2020).

Sample	PbO	SiO_2	CaO	Al_2O_3	ZnO	Fe_2O_3	T_{liq} (°C)	wt% Sp
Slag 1	47.8	19.3	9.6	5.0	11.1	7.1	1200	0.0
Slag 2	46.8	18.9	9.4	4.9	11.6	8.2	1230	2.0
Slag 3	45.9	18.5	9.2	4.9	11.9	9.3	1258	3.8
Slag 4	44.8	18.1	9.0	4.8	12.5	10.7	1279	6.2
Slag 5	43.8	17.5	8.7	4.7	13.1	12.6	1321	9.4
Slag 6	40.5	16.3	8.1	4.5	14.4	16.0	1371	15.2
Spinel	0	0	0	1.5	32.5	66.0	/	100.0

The five other bulk slag compositions (Slag 2–6, Table 1) were determined by adding the desired wt per cent equilibrium spinel composition to the liquid slag composition. All viscosity experiments were performed at 1200°C in order to maintain slag-spinel equilibrium and a constant liquid slag viscosity across the various samples.

All samples were pre-melted using an induction furnace (Hüttinger TIG 20/100) using the methodology described earlier in (Vergote *et al*, 2021). First, at 1200°C, the slag subsystem (PbO-SiO_2-CaO-Al_2O_3-ZnO) was pre-melted for one hour. FactSage predictions indicated that for all samples, these slag subsystems were fully liquid at this temperature. As a result, low viscosity samples were obtained which enhanced mixing and melting of all powder chemicals. After the pre-melting, the required amount of Fe_2O_3 powder was added to the crucible. This resulted for slag samples 2–6 in the precipitation of spinel particles in the slag, where the Fe_2O_3 acted as a nucleating agent for these particles. The slag was further homogenised and mixed by blowing air in the bath through an alumina blowing tube for one hour to ensure homogeneity of the sample. Afterwards, the slag was quenched in water. Microscopical analysis indicated proper dissolution of all chemicals and

formation of spinel particles, ie no large Fe_2O_3 powder particles but all well-formed crystalline spinel particles. The obtained slag particles were used as starting material for the viscosity measurements.

Viscosity measurements

Viscosity measurements were performed using a Searle concentric cylinder set-up in an Anton Paar FRS 1800 rheometer, consisting of an alumina spindle and crucible. The details of this apparatus were described previously in Vergote *et al* (2021). The necessary amount of slag (±150 g) was determined based on the slag density to yield a 9 mm slag layer above and below the spindle, in order to minimise the effect of the spindle height on the obtained viscosity values (Chen and Zhao, 2013). The quenched slag particles from the pre-melting were directly heated to 1200°C at a heating rate of 5°C/min. Subsequently, the slag was homogenised for one hour in order to obtain thermal and chemical equilibrium. Afterwards, the spindle was inserted into the slag bath and the measurement sequency as described before (Vergote *et al*, 2021) was executed. Fully liquid slag samples behave Newtonian, ie the viscosity is independent of the shear rate, whereas slag samples containing solid particles show shear thinning behaviour, ie a decreasing viscosity with increasing shear rate. Therefore, it is necessary for slag samples containing solid particles to examine the viscosity at various shear rates ($\dot{\gamma}$ = 0.245–24.5 s^{-1}) to get a comprehensive understanding of the rheological behaviour of the sample. Once the measurements were finished, the slag was slowly cooled (5°C/min) to room temperature.

Several repetition viscosity experiments were performed in order to verify the consistency of the obtained results. For each experiment, a unique slag batch was prepared using the methodology described above.

To enable the comparison of the obtained viscosity data set with the previous viscosity data, the apparent viscosity data, ie measured at a specific shear rate, is converted to the apparent relative viscosity (η_{rel}):

$$\eta_{rel} = \frac{\eta_{app}}{\eta_{liq}}$$

With η_{app} the apparent viscosity and η_{liq} the viscosity of the liquid slag matrix. As a result, the effect of solid particles in suspensions on the overall viscosity can be examined across heterogeneous slag samples with a different liquid slag viscosity.

Quenching experiments and microscopical analysis

In contrast to custom-built rheometer from the previous work (Vergote *et al*, 2023), it is not possible to quench samples directly after viscosity measurement in the FRS 1800. Quenching experiments were performed using the slowly cooled slag from the viscosity measurement. Slag particles in between the spindle and crucible (ie the measurement gap) were removed from the sample. These particles were used as the material for the quenching experiment to examine the microstructure of the sample as it was at high-temperature. Only 20 g of slag was added to an alumina crucible which was suspended in the hot zone of a resistance tube furnace (Carbolite HTRV 1800). The sample was heated from room temperature at a heating rate of 5°C/min and held for one hour at 1200°C. Afterwards, the wire suspending the crucible was cut from above and the sample was rapidly quenched in a water bucket. The quenched crucible was cross-sectioned, cold embedded in Epofix resin and prepared for microscopical analysis.

The microstructure of the samples was examined using a scanning electron microscope (SEM, JEOL, JSM-7600, FEG-SEM). The SEM was operated in backscattered electron (BSE) mode to increase the contrast between the amorphous slag phase and the spinel particles. The volume fraction, size and aspect ratio of the spinel particles was determined using ImageJ. These parameters were determined using at least 20 SEM-BSE images randomly selected in the bulk of the quenched sample. For the size of the particles, the Sauter average diameter is reported, since this parameter was found to be more suitable to describe the rheology of slag suspensions (Vergote *et al*, 2023). It is defined as:

$$D_{sauter} = \frac{\sum_{i=1}^{n} D_i^3}{\sum_{i=1}^{n} D_i^2}$$

With D_{sauter} the Sauter average diameter, D_i the diameter of the spinel particles of a certain particle '*i*' and *n* the amount of considered spinel particles.

RESULTS AND DISCUSSION

This study

Slag 1 showed a Newtonian flow behaviour with a constant viscosity of 0.45 Pa.s over the entire shear rate range ($\dot{\gamma}$ = 0.245–24.5 s^{-1}). This viscosity was used to determine the relative viscosity for the other samples within this data set. All other samples showed shear thinning behaviour, therefore it is required to define the shear rate to report the apparent viscosity. Figure 2a shows the relative viscosity increase for the calculated spinel weight fractions (Table 1) for the various samples at $\dot{\gamma}$ = 24.5 s^{-1}. First of all, a large scatter on the relative viscosity can be seen for the repetition experiments of slags 3, 4, 5, eg both η_{rel} = 1.8 and 7.1 were measured for the similar intended slag composition slag 5.

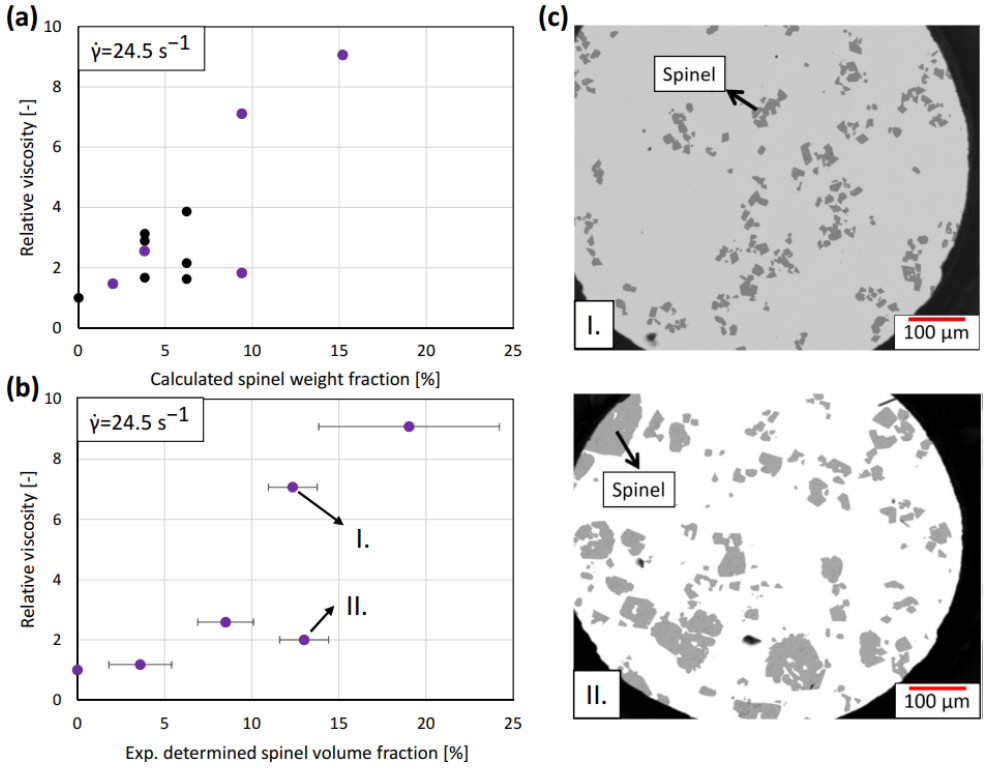

FIG 2 – (a): Relative viscosity (η_{liq}= 0.45 Pa.s, 1200°C) at $\dot{\gamma}$ = 24.5 s^{-1} for all samples in this data set, as a function of the calculated spinel weight fraction (Table 1). The purple markers indicate the samples for which additional quenching experiments were performed, (b): Relative viscosity at $\dot{\gamma}$ = 24.5 s^{-1} of the selected samples from (a), for which the volume fraction was experimentally determined, (c): scanning electron microscope – backscattered electron (SEM-BSE) images of samples I and II from (b).

As discussed in the introduction, there is a large number of parameters which affect the overall viscosity of a heterogeneous slag. Since every experiment in Figure 2a originates from an individual pre-melt, the consistency of the morphology of the spinel particles is not guaranteed. Therefore, additional quenching experiments were performed on selected samples (purple markers in Figure 2a) in order to determine the volume fraction of the spinel particles and their morphology.

Figure 2b shows the relative viscosity as a function of the experimentally determined spinel volume fraction for a selected number of samples. A first conclusion is that the volume fraction is higher for each sample compared to the predicted weight fraction, caused by the density difference between

the slag and spinel particles (Vergote *et al*, 2023). This observation highlights the importance of experimentally determined parameters instead of thermodynamic predictions to examine the rheological behaviour of slag samples. Moreover, quenching experiments were performed on the two repetition experiments of slag 5 (9.4 wt per cent spinel). For the two samples, a similar volume percentage of spinel particles was present in the slag, ie 12.4 and 13.0 vol per cent spinel. Therefore it can be concluded that the reproducibility of the pre-melting step is high. Yet, despite their similar volume percentage, a significantly different relative viscosity was obtained at $\dot{\gamma}$ = 24.5 s^{-1}. The microstructures of both repetition experiments of slag 5 (I and II) are shown in Figure 1c. First, the aspect ratio of all spinel particles was constant (±1.5) for all observed quenched samples. Second, the spinel particles for sample II are significantly larger (D_{sauter} = 78 µm) compared to the spinel particles of sample I (D_{sauter} = 30.2 µm). It was concluded before that large spinel particles cause a lower viscosity increase compared to small particles (Vergote *et al*, 2023). Lastly, the microstructures of the other samples which were microscopically studied (Slags 2, 3, 6) showed spinel particles with a size similar to sample I.

In the previous study, the size of the spinel particles was controlled by pre-sintering the spinel particles before adding them to the liquid melt. In this work, Fe_2O_3 powder was added to the liquid PbO-SiO_2-CaO-Al_2O_3-ZnO slag subsystem at 1200°C. This powder acted as a heterogeneous nucleating site for spinel particles. Using this methodology, the spinel size is largely affected by the Fe_2O_3 powder size and possible agglomeration of powder upon adding it to the liquid slag. Therefore, using this methodology, there is no control over the spinel size. The lack of control over this parameter, which is known to largely affect the slag viscosity, results in the observed scatter in Figure 2a and 2b for a constant intended amount of spinel particles.

Comparison to the previously obtained data sets

From the previous discussion, it is clear that for the samples for which the volume fraction was experimentally determined, all samples except repetition experiment II from slag 5 had an equal spinel size. Therefore, the data set in this work is divided in two sub data sets, the samples with a medium spinel size (Medium FRS 1800) and the one sample of slag 5 with the large spinel particles (Large FRS 1800). These two data sets can be compared with the three previously obtained data sets from (Vergote *et al*, 2023), where the spinel particle size was well-controlled. Figure 3b shows the distribution of the spinel particle size for the five data sets, the small, medium and large data set from the previous work (Vergote *et al*, 2023) and the medium and large FRS 1800 data set from this work. It is important to note that not only the number average spinel diameter should be considered (x-markers on Figure 3b) to define the size of the particles in a data set, but the entire distribution. The boxplots of the two medium data sets agree well and therefore their viscosity results can be compared against each other. The number average of the large FRS 1800 data set (36 µm) is significantly smaller compared to the previously obtained data set with large spinel particles (62 µm). Yet, based on their Sauter-average diameter, 61 and 78 µm for the FRS and the previous data set, respectively, the difference between both data sets is smaller, due to several large spinel particles in the FRS data set, seen by the large upper limit of the boxplot.

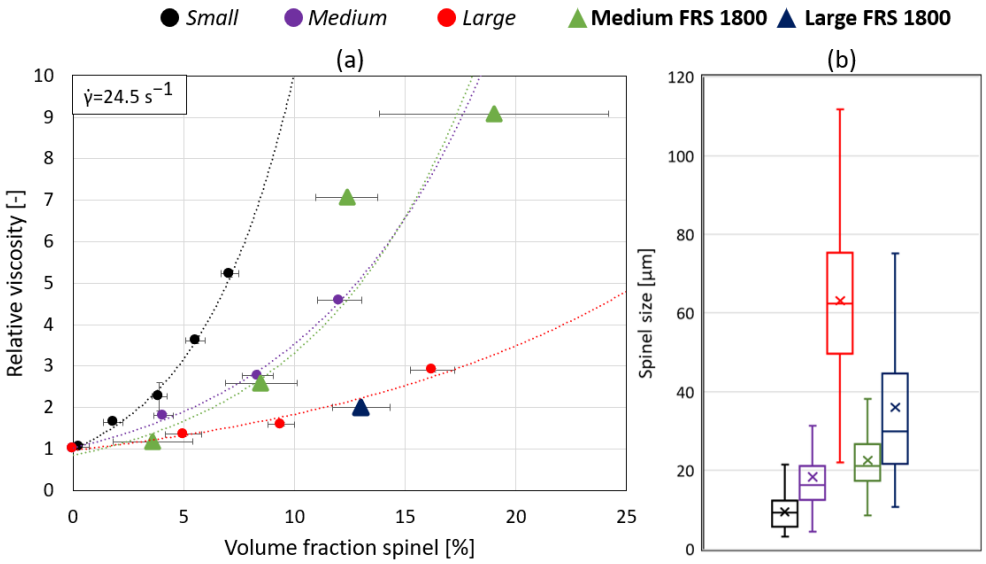

FIG 3 – (a): Comparison of the relative viscosity at $\dot{\gamma}$ = 24.5 s^{-1} for the samples in this work (triangles, medium and large FRS 1800) and the ones from the previous work (circles, small, medium and large, Vergote *et al*, 2023). The dotted lines represent optimisations of the Krieger-Dougherty equation for each data set, (b): Spinel particle size boxplots for all considered data sets, the number-average diameter is indicated with a x-marker on each boxplot.

The spinel volume fraction – relative viscosity trend at $\dot{\gamma}$ = 24.5 s^{-1}, reported in Figure 3a, agrees well for both medium data sets. In the previous data set, the maximal volume fraction was limited to 12.0 vol per cent whereas in the FRS 1800 this is extended to 19.2 vol per cent. To all data sets, Krieger-Dougherty equations were fitted to correlate the relative viscosity with the solid volume fraction (Krieger and Dougherty, 1959). The trend from the medium FRS 1800 data sets agrees well with the extrapolated trend from the previous data set. The one datapoint from the large FRS 1800 data set corresponds with the trend of the large data set from the previous study, despite the slightly smaller spinel particles in the FRS 1800 data set.

A second parameter to be able to compare the rheological behaviour across various data sets is the flow index. This parameter is fitted to the flow curves and reflects the degree of shear thinning (n = 1 reflects Newtonian behaviour, n < 1 reflects shear thinning behaviour). An Ostwald-de Waele equation is fitted to the flow curves:

$$\eta_{app} = K * \dot{\gamma}^{n-1}$$

Where K is a parameter which equals the viscosity at $\dot{\gamma}$ = 1 s^{-1} and n is the flow index, respectively. Similar to the previous work, the shear rate range 2.4–10 s^{-1} was considered in order to avoid the second Newtonian regime at large shear rates (Vergote *et al*, 2023). The resulting flow indices for various volume fractions are shown in Figure 4. First of all, all data sets show a decreasing flow index, ie more shear thinning, with increasing volume fraction of spinel particles. This observation can be explained by the increased number of particles with increasing volume fraction. As a result, the particles have more close neighbours in the melt to be influenced by (particle-particle orientation) and consequently the internal structure can be more affected by the shear rate (Vergote *et al*, 2023). Secondly, the large FRS 1800 data set show less shear thinning compared to the medium data set. This observation can be explained in a similar way: a decrease in particle size, for a constant volume fraction, result in a larger number of particles, hence more particle-particle orientation. Both rheological observations, a smaller relative viscosity (Figure 3a) and the lower degree of shear thinning, can be explained by the microstructural observation of the larger spinel particles.

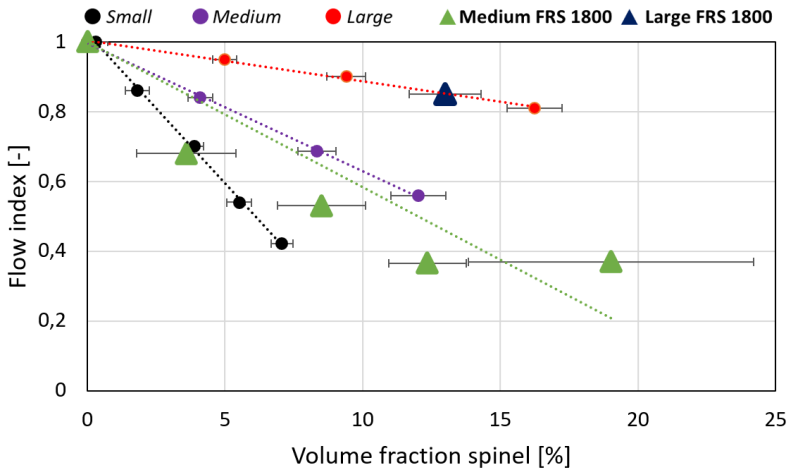

FIG 4 – Flow index as a function of the experimentally determined spinel volume fraction for all considered data sets. Linear trendlines (dotted lines) were fitted to all data sets.

Moreover, the flow indices of the medium FRS data set from this work are slightly smaller compared to previously obtained flow indices for the medium data set. Furthermore, it is observed that the flow index does not further decrease at larger spinel volume fractions. This flow index plateau is also commonly reported in literature (Mueller, Llewellin and Mader, 2009). Therefore, the applicability of the linear trendline may be limited at large volume fractions. For the large FRS data set, the flow index aligns with the previously determined trendline for the large spinel particles, despite the small difference in size between both data sets (Figure 3b).

CONCLUSION

The previous study largely focused on providing reliable data sets with a strong control overall parameters affecting the rheology of heterogeneous slag containing spinel particles. The methodology involved control over the spinel particle size via pre-sintering the spinel particles before adding them to the liquid melt. This study was performed to verify the consistency of the previously obtained insights in the viscosity behaviour of a slag containing spinel particles.

In this study's methodology, the size of the spinel particles was not well-controlled, which was reflected in the scatter on the relative viscosity for a constant intended amount of spinel particles. Microstructural analysis of quenched samples showed that the spinel size differed across various samples. Therefore, the samples were divided into two data sets, with medium and large spinel particles. Similar to the conclusions from the previous study, it was observed that the relative viscosity increase was larger for smaller spinel particles. Moreover, the samples with smaller spinel particles also showed stronger shear thinning behaviour, which was also previously concluded. The numerical values for the relative viscosity and the flow index were in the similar range as the one determined earlier.

This study further supports the importance of considering the particle size for viscosity studies and models regarding heterogeneous silicate melts. As a result, particle-particle orientation as a mode of shear thinning should also be considered. The initially obtained conclusions are further supported by this study, using an independent slag preparation and different high-temperature rheometer.

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